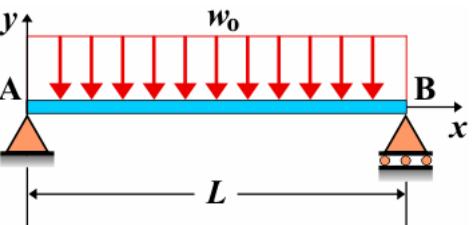
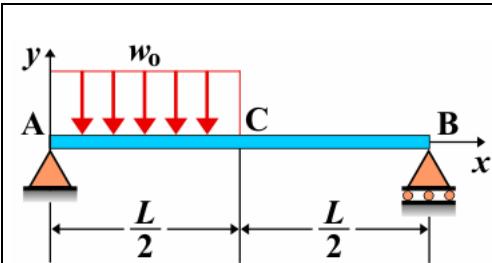


Simbolo	Magnitud	Unidades
$E \cdot I$	Rigidez a flexión	$\text{N} \cdot \text{m}^2, \text{Pa} \cdot \text{m}^4$
y	Deflexión, deformación, flecha	m
θ	Pendiente, giro	-
x	Posición del punto de estudio (distancia desde el origen)	m
L	Longitud de la viga (sin vano lateral)	m
M	Momento flector, flector, momento aplicado	$\text{N} \cdot \text{m}$
P	Carga puntual, carga concentrada	N
w	Carga distribuida	N/m
R	Reacción	N
V	Esfuerzo cortante, cortante	N

Viga simple apoyada - Carga uniforme en todo el vano

	<p>Deflexión $y_{AB} = \frac{-w_0 x}{24EI} (L^3 - 2Lx^2 + x^3)$</p> $y_{MAX} = \frac{-5w_0 L^4}{384EI}$ para $x = \frac{L}{2}$ <p>Pendiente $\theta_{AB} = \frac{-w_0}{24EI} (L^3 - 6Lx^2 + 4x^3)$</p> $\theta_A = -\theta_B = \frac{-w_0 L^3}{24EI}$ <p>Momento $M_{AB} = \frac{w_0 x}{2} (L - x)$</p> $M_{MAX} = \frac{w_0 L^2}{8}$ para $x = \frac{L}{2}$ <p>Cortante $V_{AB} = \frac{w_0}{2} (L - 2x)$</p> <p>Reacciones $R_A = R_B = \frac{w_0 L}{2}$</p>
---	---

Viga simple apoyada - Carga uniforme en la mitad del vano



$$\text{Deflexión} \quad y_{AC} = \frac{-w_0 x}{384EI} (9L^3 - 24Lx^2 + 16x^3)$$

$$y_{CB} = \frac{-w_0 L}{384EI} (8x^3 - 24Lx^2 + 17L^2x - L^3)$$

$$\text{Pendiente} \quad \theta_{AC} = \frac{-w_0}{384EI} (9L^3 - 72Lx^2 + 64x^3)$$

$$\theta_{CB} = \frac{-w_0 L}{384EI} (24x^2 - 48Lx + 17L^2)$$

$$\theta_A = \frac{-3wL^3}{128EI} \quad \theta_B = \frac{7wL^3}{384EI}$$

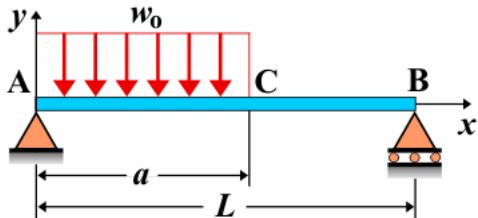
$$\text{Momento} \quad M_{AC} = \frac{w_0}{8} (3Lx - 4x^2) \quad M_{CB} = \frac{w_0}{8} (L^2 - Lx)$$

$$\text{Cortante} \quad V_{AC} = \frac{w_0}{8} (3L - 8x) \quad V_{CB} = \frac{-w_0 L}{8}$$

$$V_A = R_A \quad V_B = -R_B$$

$$\text{Reacciones} \quad R_A = \frac{3w_0 L}{8} \quad R_B = \frac{w_0 L}{8}$$

Viga simple apoyada - Carga uniforme parcial en un lado



Deflexión:

$$y_{AC} = \frac{-w_0 x}{24LEI} (a^4 - 4a^3L + 4a^2L^2 + 2a^2x^2 - 4aLx^2 + Lx^3)$$

$$y_{CB} = \frac{-w_0 a^2}{24LEI} (-a^2L + 4L^2x + a^2x - 6Lx^2 + 2x^3)$$

Pendiente:

$$\theta_{AC} = \frac{-w_0}{24LEI} (a^4 - 4a^3L + 4a^2L^2 + 6a^2x^2 - 12aLx^2 + 4Lx^3)$$

$$\theta_{CB} = \frac{-w_0 a^2}{24LEI} (4L^2 + a^2 - 12Lx + 6x^2)$$

Momento:

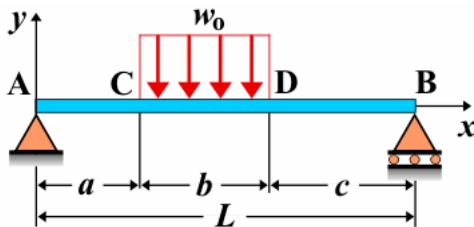
$$M_{AC} = \frac{-w_0}{2L} (a^2x - 2aLx + Lx^2) \quad M_{CB} = \frac{w_0 a^2}{2L} (L - x)$$

Cortante:

$$V_{AC} = \frac{-w_0}{2L} (a^2 - 2aL + 2Lx) \quad V_{CB} = V_C = V_B = \frac{-w_0 a^2}{2L}$$

$$\text{Reacciones} \quad R_A = \frac{w_0 a}{2L} (2L - a) \quad R_B = \frac{w_0 a^2}{2L}$$

Viga simple apoyada - Carga uniforme parcial



Deflexión $y_{AC} = \frac{R_A x^3}{6EI} + \alpha x$ $y_{CD} = \frac{R_A x^3}{6EI} - \frac{w_0}{24EI}(x-a)^4 + \alpha x$
 $y_{DB} = \frac{R_B(L-x)^3}{6EI} + \frac{\beta(L-x)}{L}$

Pendiente: $\theta_{AC} = \frac{R_A x^2}{2EI} + \alpha$ $\theta_{CD} = \frac{R_A x^2}{2EI} - \frac{w_0}{6EI}(x-a)^3 + \alpha$
 $\theta_{DB} = \frac{-R_B(L-x)^2}{2EI} - \frac{\beta}{L}$

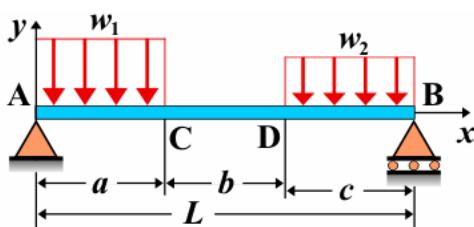
Momento $M_{AC} = R_A x$ $M_{CD} = R_A x - \frac{w_0}{2}(x-a)^2$
 $M_{DB} = R_B(L-x)$

Cortante $V_{AC} = V_A = V_C = R_A$ $V_{CD} = R_A - w_0(x-a)$
 $V_{DB} = V_D = V_B = -R_B$

Reacciones $R_A = \frac{w_0 b}{2L} (2c+b)$ $R_B = \frac{w_0 b}{2L} (2a+b)$

Siendo:
 $\alpha = \frac{w_0 b^3 L - 6EI\beta - 3R_B c^2 L - 3R_A L(a+b)^2}{6LEI}$
 $\beta = \frac{4w_0 ab^3 + 3w_0 b^4 - 8R_A (a+b)^3 - 12R_B c^2 L + 8R_B c^3}{24EI}$

Viga simple apoyada - Cargas uniformes parciales distintas a cada lado

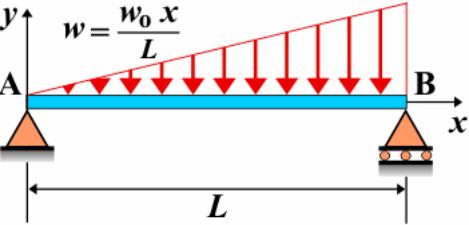


Momento $M_{AC} = R_A x - \frac{w_1 x^2}{2}$
 $M_{CD} = R_A x - \frac{w_1 a}{2}(2x-a)$ $M_{DB} = R_B(L-x) - \frac{w_2(L-x)^2}{2}$

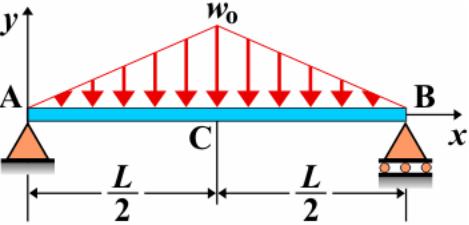
Cortante: $V_{AC} = R_A - w_1 x$ $V_{CD} = R_A - w_1 a$ $V_{DB} = -R_B + w_2(L-x)$

Reacciones:
 $R_A = \frac{w_1 a(2L-a) + w_2 c^2}{2L}$ $R_B = \frac{w_2 c(2L-c) + w_1 a^2}{2L}$

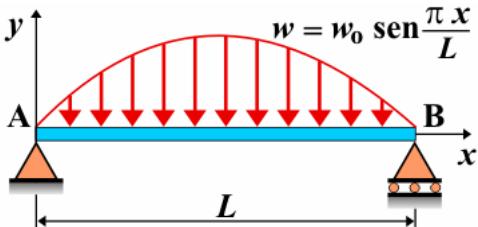
Viga simple apoyada - Carga uniformemente creciente en todo el vano

 $w = \frac{w_0 x}{L}$	<p>Deflexión $y_{AB} = \frac{-w_0 x}{360EI} (7L^4 - 10L^2x^2 + 3x^4)$</p> <p>$y_{MAX} = -0,00652 \frac{w_0 L^4}{EI}$ para $x = 0,5193L$</p> <p>Pendiente $\theta_{AB} = \frac{-w_0}{360EI} (7L^4 - 30L^2x^2 + 15x^4)$</p> <p>$\theta_A = \frac{-7w_0 L^3}{360EI}$ $\theta_B = \frac{w_0 L^3}{45EI}$</p> <p>Momento $M_{AB} = \frac{w_0}{6L} (L^2 x - x^3)$</p> <p>Cortante $V_{AB} = \frac{w_0}{6L} (L^2 - 3x^2)$</p> <p>Reacciones $R_A = \frac{w_0 L}{6}$ $R_B = \frac{2w_0 L}{6}$</p>
--	---

Viga simple apoyada - Carga uniformemente creciente hacia el centro

 w_0	<p>Deflexión $y_{AC} = \frac{-w_0 x}{960EI} (5L^2 - 4x^2)^2$</p> <p>$y_{CB} = \frac{-w_0 (L-x)}{960EI} (5L^2 - 4(L-x)^2)^2$</p> <p>$y_{MAX} = \frac{-w_0 L^4}{120EI}$ para $x = \frac{L}{2}$</p> <p>Pendiente $\theta_{AC} = \frac{-w_0}{192EI} (5L^2 - 4x^2)(L^2 - 4x^2)$</p> <p>$\theta_{CB} = \frac{w_0}{192LEI} (5L^2 - 4(L-x)^2)(L^2 - 4(L-x)^2)$</p> <p>$\theta_A = -\theta_B = \frac{-5w_0 L^3}{192EI}$</p> <p>Momento $M_{AC} = \frac{w_0}{12L} (3L^2 x - 4x^3)$</p> <p>$M_{CB} = \frac{w_0 (L-x)}{12L} (3L^2 - 4(L-x)^2)$</p> <p>Cortante $V_{AC} = \frac{w_0}{4L} (L^2 - 4x^2)$ $V_{CB} = \frac{-w_0}{4L} (L^2 - 4(L-x)^2)$</p> <p>Reacciones $R_A = R_B = \frac{w_0 L}{4}$</p>
---	---

Viga simple apoyada - Carga senoidalmente distribuida



$$\text{Deflexión } y_{AB} = \frac{-w_0 L^4}{\pi^4 EI} \operatorname{sen} \frac{\pi x}{L}$$

$$y_{\text{MAX}} = \frac{-w_0 L^4}{\pi^4 EI} \quad \text{para } x = \frac{L}{2}$$

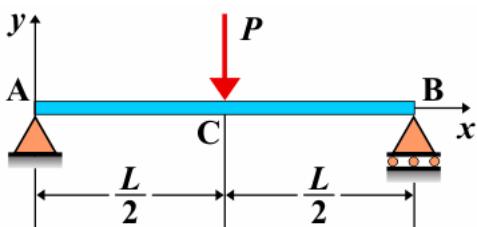
$$\text{Pendiente } \theta_{AB} = \frac{-w_0 L^3}{\pi^3 EI} \cos \frac{\pi x}{L} \quad \theta_A = -\theta_B = \frac{-w_0 L^3}{\pi^3 EI}$$

$$\text{Momento } M_{AB} = \frac{w_0 L^2}{\pi^2} \operatorname{sen} \frac{\pi x}{L}$$

$$\text{Cortante } V_{AB} = \frac{w_0 L}{\pi} \cos \frac{\pi x}{L} \quad V_A = -V_B = \frac{w_0 L}{\pi}$$

$$\text{Reacciones } R_A = R_B = \frac{w_0 L}{\pi}$$

Viga simple apoyada - Carga puntual en el centro



$$\text{Deflexión } y_{AC} = \frac{-Px}{48EI} (3L^2 - 4x^2)$$

$$y_{CB} = \frac{-P(L-x)}{48EI} (3L^2 - 4(L-x)^2)$$

$$y_{\text{MAX}} = y_C = \frac{-PL^3}{48EI} \quad \text{para } x = \frac{L}{2}$$

Pendiente:

$$\theta_{AC} = \frac{-P}{16EI} (L^2 - 4x^2) \quad \theta_{CB} = \frac{-P}{16EI} (4x^2 - 8Lx + 3L^2)$$

$$\theta_A = -\theta_B = \frac{PL^2}{16EI}$$

$$\text{Momento } M_{AC} = \frac{Px}{2} \quad M_{CB} = \frac{P(L-x)}{2}$$

$$\text{Cortante } V_{AC} = V_A = \frac{P}{2} \quad V_{CB} = V_B = -\frac{P}{2}$$

$$\text{Reacciones } R_A = R_B = \frac{P}{2}$$

Viga simple apoyada - Carga puntual en cualquier punto

	<p>Deflexión $y_{AC} = \frac{-Pbx}{6EI}(L^2 - b^2 - x^2)$ $y_{CB} = \frac{-Pa(L-x)}{6EI}[L^2 - a^2 - (L-x)^2]$</p> <p>Pendiente: $\theta_{AC} = \frac{-Pb}{6EI}(L^2 - b^2 - 3x^2)$ $\theta_{CB} = \frac{Pa}{6EI}[L^2 - a^2 - 3(L-x)^2]$</p> $\theta_A = \frac{-Pb(L^2 - b^2)}{6LEI}$ $\theta_B = \frac{Pa}{6LEI}(L^2 - a^2)$ <p>Momento $M_{AC} = \frac{Pbx}{L}$ $M_{CB} = \frac{Pa(L-x)}{L}$</p> <p>Cortante $V_{AC} = V_A = \frac{Pb}{L}$ $V_{CB} = V_B = \frac{-Pa}{L}$</p> <p>Reacciones $R_A = \frac{Pb}{L}$ $R_B = \frac{Pa}{L}$</p>
--	---

Viga simple apoyada - Dos cargas puntuales iguales situadas simétricamente

	<p>Deflexión $y_{AC} = \frac{-Px}{6EI}(3aL - 3a^2 - x^2)$ $y_{CD} = \frac{-Pa}{6EI}(3Lx - 3x^2 - a^2)$ $y_{DB} = \frac{-P(L-x)}{6EI}[3aL - 3a^2 - (L-x)^2]$</p> $y_{MAX} = \frac{-Pa}{24EI}(3L^2 - 4a^2)$ para $x = \frac{L}{2}$ <p>Pendiente $\theta_{AC} = \frac{-P}{2EI}(aL - a^2 - x^2)$ $\theta_{CD} = \frac{-Pa}{2EI}(L - 2x)$ $\theta_{DB} = \frac{P}{2EI}[aL - a^2 - (L-x)^2]$</p> $\theta_A = -\theta_B = \frac{-P(aL - a^2)}{2EI}$ <p>Momento $M_{AC} = Px$ $M_{CD} = Pa$ $M_{DB} = P(L-x)$</p> <p>Cortante $V_{AC} = P$ $V_{CD} = 0$ $V_{DB} = -P$</p> <p>Reacciones $R_A = R_B = P$</p>
--	---

Viga simple apoyada - Dos cargas puntuales iguales situadas asimétricamente

	<p>Momento $M_{AC} = R_A x$ $M_{CD} = R_A x - P(x-a)$ $M_{DB} = R_B(L-x)$</p> <p>Cortante $V_{AC} = R_A$ $V_{CD} = R_A - P$ $V_{DB} = -R_B$</p> <p>Reacciones $R_A = \frac{P(L-a+b)}{L}$ $R_B = \frac{P(L-b+a)}{L}$</p>
--	--

Viga simple apoyada - Dos cargas puntuales desiguales situadas asimétricamente

	<p>Momento $M_{AC} = R_A x \quad M_{CD} = R_A x - P_1(x-a)$ $M_{DB} = R_B(L-x)$</p> <p>Cortante $V_{AC} = R_A \quad V_{CD} = R_A - P_1 \quad V_{DB} = -R_B$</p> <p>Reacciones $R_A = \frac{P_1(L-a) + P_2 b}{L} \quad R_B = \frac{P_2(L-b) + P_1 a}{L}$</p>
--	---

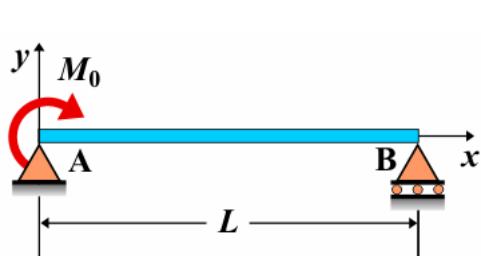
Viga simple apoyada - Momento antihorario en el lado derecho

	<p>Deflexión $y_{AB} = \frac{-M_0 x}{6EI} (L^2 - x^2)$</p> <p>Pendiente $\theta_{AB} = \frac{-M_0}{6EI} (L^2 - 3x^2)$ $\theta_A = \frac{-M_0 L}{6EI} \quad \theta_B = \frac{M_0 L}{3EI}$</p> <p>Momento $M_{AB} = \frac{M_0 x}{L}$</p> <p>Cortante $V_{AB} = \frac{M_0}{L}$</p> <p>Reacciones $R_A = \frac{M_0}{L} \quad R_B = \frac{-M_0}{L}$</p>
--	--

Viga simple apoyada - Momento antihorario en el lado izquierdo

	<p>Deflexión $y_{AB} = \frac{M_0 x}{6EI} (2L^2 - 3Lx + x^2)$ $y_{MAX} = \frac{M_0 L^2}{9\sqrt{3}EI} \quad \text{para } x = \left(\frac{3-\sqrt{3}}{3}\right)L$</p> <p>Pendiente $\theta_{AB} = \frac{M_0}{6EI} (2L^2 - 6Lx + 3x^2)$ $\theta_A = \frac{M_0 L}{3EI} \quad \theta_B = \frac{-M_0 L}{6EI}$</p> <p>Momento $M_{AB} = \frac{-M_0}{L} (L-x)$</p> <p>Cortante $V_{AB} = \frac{M_0}{L}$</p> <p>Reacciones $R_A = \frac{M_0}{L} \quad R_B = \frac{-M_0}{L}$</p>
--	---

Viga simple apoyada - Momento horario en el extremo izquierdo



Deflexión $y_{AB} = \frac{-M_0 x}{6EI} (2L^2 - 3Lx + x^2)$
 $y_{MAX} = \frac{-M_0 L^2}{9\sqrt{3}EI}$ para $x = \left(\frac{3-\sqrt{3}}{3}\right)L$

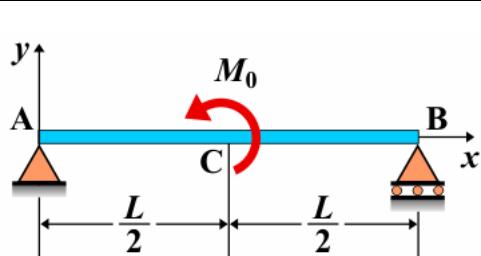
Pendiente $\theta_{AB} = \frac{-M_0}{6EI} (2L^2 - 6Lx + 3x^2)$
 $\theta_A = \frac{-M_0 L}{3EI}$ $\theta_B = \frac{M_0 L}{6EI}$

Momento $M_{AB} = \frac{M_0}{L} (L - x)$

Cortante $V_{AB} = \frac{-M_0}{L}$

Reacciones $R_A = \frac{-M_0}{L}$ $R_B = \frac{M_0}{L}$

Viga simple apoyada - Momento antihorario en el centro



Deflexión $y_{AC} = \frac{-M_0 x}{24LEI} (L^2 - 4x^2)$
 $y_{CB} = \frac{M_0 (L - x)}{24LEI} (L^2 - 4(L - x)^2)$

Pendiente $\theta_{AC} = \frac{-M_0}{24LEI} (L^2 - 12x^2)$
 $\theta_{CB} = \frac{M_0}{24LEI} (12(L - x)^2 - L^2)$

$\theta_A = \frac{-M_0}{6LEI} (L^2 - 3b^2)$ $\theta_B = \frac{M_0}{6LEI} (-L^2 + 3a^2)$

Momento $M_{AC} = \frac{M_0 x}{L}$ $M_{CB} = \frac{-M_0}{L} (L - x)$

Cortante $V_{AC} = \frac{M_0}{L}$ $V_{CB} = \frac{M_0}{L}$

Reacciones $R_A = \frac{M_0}{L}$ $R_B = \frac{-M_0}{L}$

Viga simple apoyada - Momento antihorario en cualquier punto

	<p>Deflexión $y_{AC} = \frac{-M_0 x}{6EI} (L^2 - 3b^2 - x^2)$</p> $y_{CB} = \frac{M_0(L-x)}{6EI} (L^2 - 3a^2 - (L-x)^2)$ <p>Pendiente $\theta_{AC} = \frac{-M_0}{6EI} (L^2 - 3b^2 - 3x^2)$</p> $\theta_{CB} = \frac{M_0}{6EI} (-L^2 + 3a^2 + 3(L-x)^2)$ <p>Momento $M_{AC} = \frac{M_0 x}{L}$ $M_{CB} = \frac{-M_0}{L} (L-x)$</p> <p>Cortante $V_{AC} = \frac{M_0}{L}$ $V_{CB} = \frac{M_0}{L}$</p> <p>Reacciones $R_A = \frac{M_0}{L}$ $R_B = \frac{-M_0}{L}$</p>
--	--

Viga simple apoyada - Dos momentos distintos antihorario + horario en los extremos

	<p>Deflexión $y_{AB} = \frac{-x(L-x)}{6EI} [(M_1 - M_2)x - (2M_1 + M_2)L]$</p> <p>Pendiente: $\theta_{AB} = \frac{1}{6EI} [(M_1 - M_2)(3x^2 - 2Lx) - (2M_1 + M_2)(2Lx - L^2)]$</p> <p>Momento $M_{AB} = \frac{1}{L} [(M_1 - M_2)x - LM_1]$</p> <p>Cortante $V_{AB} = \frac{M_1 - M_2}{L}$</p> <p>Reacciones $R_A = \frac{M_1 - M_2}{L}$ $R_B = \frac{M_2 - M_1}{L}$</p>
--	---

Viga simple apoyada - Dos momentos distintos antihorario en los extremos

	<p>Deflexión $y_{AB} = \frac{-x(L-x)}{6EI} [(M_1 + M_2)x - (2M_1 - M_2)L]$</p> <p>Pendiente: $\theta_{AB} = \frac{1}{6EI} [(M_1 + M_2)(3x^2 - 2Lx) - (2M_1 - M_2)(2Lx - L^2)]$</p> <p>Momento $M_{AB} = \frac{1}{L} [(M_1 + M_2)x - LM_1]$</p> <p>Cortante $V_{AB} = \frac{M_1 + M_2}{L}$</p> <p>Reacciones $R_A = \frac{M_1 + M_2}{L}$ $R_B = \frac{-M_1 - M_2}{L}$</p>
--	--

Viga simple apoyada - Dos momentos iguales horario + antihorario en los extremos

	<p>Deflexión $y_{AB} = \frac{-M_0x}{2EI}(L-x)$ $y_{MAX} = \frac{-M_0L^2}{8EI}$ para $x = \frac{L}{2}$</p> <p>Pendiente $\theta_{AB} = \frac{-M_0}{2EI}(L-2x)$ $\theta_A = -\theta_B = \frac{-M_0L}{2EI}$</p> <p>Momento $M_{AB} = M_0$</p> <p>Cortante $V_{AB} = 0$</p> <p>Reacciones $R_A = R_B = 0$</p>
--	--

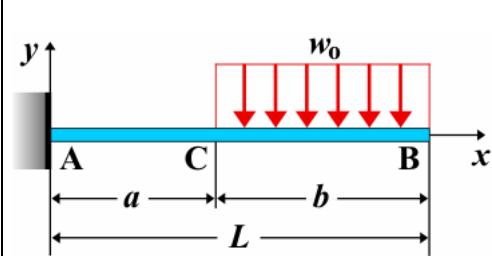
Viga en voladizo - Carga uniforme en todo el vano

	<p>Deflexión $y_{AB} = \frac{-w_0}{24EI}(x^4 - 4Lx^3 + 6L^2x^2)$ $y_{MAX} = y_B = \frac{-w_0L^4}{8EI}$ para $x = L$</p> <p>Pendiente $\theta_{AB} = \frac{-w_0}{6EI}(x^3 - 3Lx^2 + 3L^2x)$ $\theta_B = \frac{-w_0L^3}{6EI}$</p> <p>Momento $M_{AB} = \frac{-w_0}{2}(L-x)^2$ $M_{MAX} = M_A = \frac{-w_0L^2}{2}$</p> <p>Cortante $V_{AB} = w_0(L-x)$</p> <p>Reacciones $R_A = w_0L$</p>
--	---

Viga en voladizo - Carga uniforme parcial en el lado empotrado

	<p>Deflexión $y_{AC} = \frac{-w_0}{24EI}(6a^2x^2 - 4ax^3 + x^4)$ $y_{CB} = \frac{-w_0a^3}{24EI}(4x - a)$ $y_{MAX} = y_B = \frac{-w_0a^3}{24EI}(4L - a)$</p> <p>Pendiente $\theta_{AC} = \frac{-w_0}{6EI}(3a^2x - 3ax^2 + x^3)$ $\theta_{CB} = \theta_C = \theta_B = \frac{-w_0a^3}{6EI}$</p> <p>Momento $M_{AC} = \frac{-w_0}{2}(a-x)^2$ $M_{CB} = M_C = M_B = 0$ $M_{MAX} = M_A = \frac{-w_0a^2}{2}$</p> <p>Cortante $V_{AC} = w_0(a-x)$ $V_{CB} = V_C = V_B = 0$</p> <p>Reacciones $R_A = w_0a$</p>
--	---

Viga en voladizo - Carga uniforme parcial en el lado libre

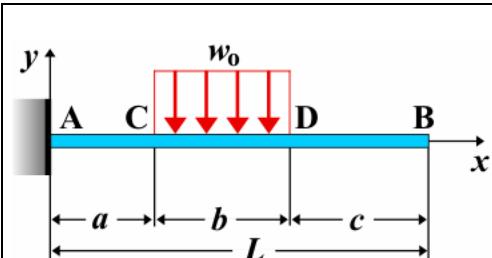


Deflexión $y_{AC} = \frac{-w_0bx^2}{12EI}(3L+3a-2x)$
 $y_{CB} = \frac{-w_0}{24EI}(x^4 - 4Lx^3 + 6L^2x^2 - 4a^3x + a^4)$

Pendiente $\theta_{AC} = \frac{-w_0bx}{2EI}(L+a-x)$
 $\theta_{CB} = \frac{-w_0}{6EI}(x^3 - 3Lx^2 + 3L^2x - a^3)$
 $\theta_B = \frac{-w_0}{6EI}(L^3 - a^3)$

Momento $M_{AC} = \frac{-w_0b}{2}(L+a-2x) \quad M_{CB} = \frac{-w_0}{2}(L-x)^2$
 Cortante $V_{AC} = V_A = V_C = w_0b \quad V_{CB} = w_0(L-x)$
 Reacciones $R_A = w_0b$

Viga en voladizo - Carga uniforme parcial



Deflexión $y_{AC} = \frac{-w_0bx^2}{12EI}(6a+3b-2x)$
 $y_{CD} = \frac{-w_0}{24EI}(x^4 - 4(a+b)x^3 + 6(a+b)^2x^2 - 4a^3x + a^4)$
 $y_{DB} = \frac{-w_0}{24EI}(4x[(a+b)^3 - a^3] - (a+b)^4 + a^4)$

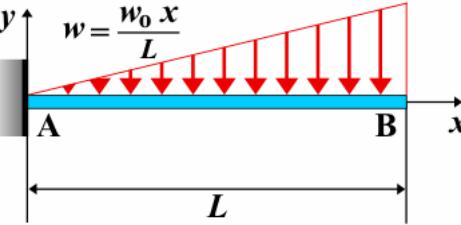
Pendiente $\theta_{AC} = \frac{-w_0bx}{2EI}(2a+b-x)$
 $\theta_{CD} = \frac{-w_0}{6EI}(x^3 - 3(a+b)x^2 + 3(a+b)^2x - a^3)$
 $\theta_{DB} = \frac{-w_0}{6EI}((a+b)^3 - a^3)$

Momento $M_{AC} = \frac{-w_0b}{2}(2a+b-2x)$
 $M_{CD} = \frac{-w_0}{2}(a+b-x)^2 \quad M_{DB} = M_D = M_B = 0$

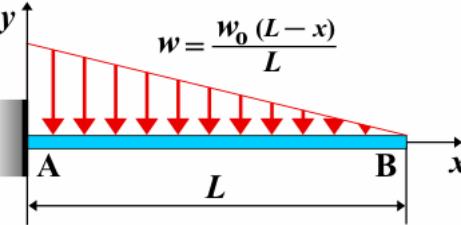
Cortante $V_{AC} = V_A = V_C = w_0b \quad V_{CD} = w_0(a+b-x)$
 $V_{DB} = V_D = V_B = 0$

Reacciones $R_A = w_0b$

Viga en voladizo - Carga uniformemente creciente hacia el lado libre en todo el vano

	<p>Deflexión $y_{AB} = \frac{-w_0 x^2}{120EI} (20L^3 - 10L^2x + x^3)$</p> <p>$y_{MAX} = \frac{-11w_0 L^4}{120EI}$ para $x = L$</p> <p>Pendiente $\theta_{AB} = \frac{-w_0 x}{24EI} (8L^3 - 6L^2x + x^3)$</p> <p>$\theta_B = \frac{-w_0 L^3}{8EI}$</p> <p>Momento $M_{AB} = \frac{-w_0}{6L} (2L^3 - 3L^2x + x^3)$</p> <p>Cortante $V_{AB} = \frac{w_0}{2L} (L^2 - x^2)$</p> <p>Reacciones $R_A = \frac{w_0 L}{2}$</p>
---	---

Viga en voladizo - Carga uniformemente creciente hacia el lado empotrado en todo el vano

	<p>Deflexión $y_{AB} = \frac{-w_0 x^2}{120EI} (10L^3 - 10L^2x + 5Lx^2 - x^3)$</p> <p>$y_{MAX} = \frac{w_0 L^4}{30EI}$ para $x=L$</p> <p>Pendiente $\theta_{AB} = \frac{-w_0 x}{24EI} (4L^3 - 6L^2x + 4Lx^2 - x^3)$</p> <p>$\theta_B = \frac{-w_0 L^3}{24EI}$</p> <p>Momento $M_{AB} = \frac{-w_0}{6L} (L-x)^3$</p> <p>Cortante $V_{AB} = \frac{w_0}{2L} (L-x)^2$</p> <p>Reacciones $R_A = \frac{w_0 L}{2}$</p>
--	---

Viga en voladizo - Carga cosenoidalmente decreciente hacia el lado libre en todo el vano

	<p>Deflexión $y_{AB} = \frac{-w_0 L}{3\pi^4 EI} \left(48L^3 \cos \frac{\pi x}{2L} - 48L^3 + 3\pi^3 Lx^2 - \pi^3 x^3 \right)$</p> $y_{MAX} = \frac{-2w_0 L^4}{3\pi^4 EI} (\pi^3 - 24) \text{ para } x = L$ <p>Pendiente $\theta_{AB} = \frac{-w_0 L}{\pi^3 EI} \left(2\pi^2 Lx - \pi^2 x^2 - 8L^2 \sin \frac{\pi x}{2L} \right)$</p> $\theta_B = \frac{-w_0 L^3}{\pi^3 EI} (\pi^2 - 8)$ <p>Momento $M_{AB} = \frac{-2w_0 L}{\pi^2} \left(\pi L - \pi x - 2L \cos \frac{\pi x}{2L} \right)$</p> <p>Cortante $V_{AB} = \frac{2w_0 L}{\pi} \left(1 - \sin \frac{\pi x}{2L} \right)$</p> <p>Reacciones $R_A = \frac{2w_0 L}{\pi}$</p>
--	---

Viga en voladizo - Carga puntual en el extremo libre

	<p>Deflexión $y_{AB} = \frac{-P}{6EI} (3Lx^2 - x^3)$</p> $y_{MAX} = y_B = \frac{-PL^3}{3EI}$ <p>Pendiente $\theta_{AB} = \frac{-P}{2EI} (2Lx - x^2)$</p> $\theta_{MAX} = \theta_B = \frac{-PL^2}{2EI}$ <p>Momento $M_{AB} = -P(L - x)$</p> $M_{MAX} = M_A = -PL$ <p>Cortante $V_{AB} = V_A = V_B = P$</p> <p>Reacciones $R_A = P$</p>
--	--

Viga en voladizo - Carga puntual en cualquier punto

	<p>Deflexión $y_{AC} = \frac{-P}{6EI} (3ax^2 - x^3)$</p> $y_{CB} = \frac{-Pa^2}{6EI} (3x - a)$ $y_{MAX} = y_B = \frac{-Pa^2}{6EI} (3L - a)$ <p>Pendiente $\theta_{AC} = \frac{-P}{2EI} (2ax - x^2)$</p> $\theta_{CB} = \theta_C = \theta_B = \frac{-Pa^2}{2EI}$ <p>Momento $M_{AC} = -P(a - x)$</p> $M_{CB} = M_C = M_B = 0$ $M_{MAX} = M_A = -Pa$ <p>Cortante $V_{AC} = V_A = V_C = P$</p> $V_{CB} = V_C = V_B = 0$ <p>Reacciones $R_A = P$</p>
--	---

Viga en voladizo - Momento horario en el extremo libre

	<p>Deflexión $y_{AB} = \frac{-M_0 x^2}{2EI}$ $y_{MAX} = \frac{-M_0 L^2}{2EI}$ para $x = L$</p> <p>Pendiente $\theta_{AB} = \frac{-M_0 x}{EI}$</p> <p>Momento $M_{AB} = M_A = M_B = -M_0$</p> <p>Cortante $V_{AB} = V_A = V_B = 0$</p> <p>Reacciones $R_A = 0$</p>
--	--

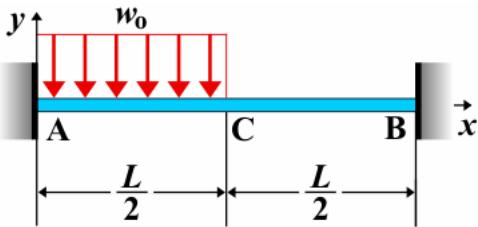
Viga en voladizo - Momento horario en cualquier punto

	<p>Deflexión $y_{AC} = \frac{-M_0 x^2}{2EI}$ $y_{CB} = \frac{-M_0 a}{2EI}(2x-a)$ $y_{MAX} = \frac{-M_0 a}{2EI}(2L-a)$ para $x = L$</p> <p>Pendiente $\theta_{AC} = \frac{-M_0 x}{EI}$ $\theta_{CB} = \theta_C = \theta_B = \frac{-M_0 a}{EI}$</p> <p>Momento $M_{AC} = M_A = -M_0$ $M_{CB} = M_B = 0$</p> <p>Cortante $V_{AC} = V_A = V_C = 0$ $V_{CB} = V_C = V_B = 0$</p> <p>Reacciones $R_A = 0$</p>
--	--

Viga empotrada - Carga uniforme en todo el vano

	<p>Deflexión $y_{AB} = \frac{-w_0 x^2}{24EI}(L-x)^2$</p> <p>Pendiente $\theta_{AB} = \frac{-w_0 x}{12EI}(L^2 - 3Lx + 2x^2)$</p> <p>Momento $M_{AB} = \frac{-w_0}{12}(L^2 - 6Lx + 6x^2)$</p> <p>Cortante $V_{AB} = \frac{w_0}{2}(L-2x)$</p> <p>Reacciones $R_A = R_B = \frac{w_0 L}{2}$</p>
--	--

Viga empotrada - Carga uniforme en la mitad del vano



$$\text{Deflexión } y_{AC} = \frac{-x^2}{24EI} (w_0 x^2 - 4R_A x - 12M_A)$$

$$y_{CB} = \frac{3(M_B + LR_B)x^2 - R_B x^3}{6EI} +$$

$$+ \frac{L^2(3M_B + LR_B) - 3(2M_B + LR_B)Lx}{6EI}$$

$$\text{Pendiente } \theta_{AC} = \frac{-x}{6EI} (w_0 x^2 - 3R_A x - 6M_A)$$

$$\theta_{CB} = \frac{-1}{2EI} [R_B x^2 - 2(M_B + LR_B)x + L(2M_B + LR_B)]$$

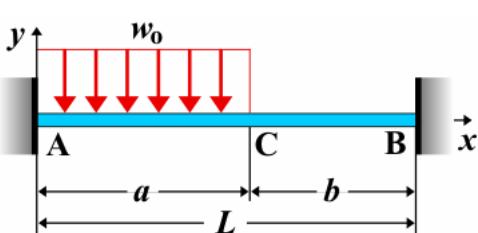
$$\text{Momento } M_{AC} = R_A x + M_A - \frac{w_0 x^2}{2} \quad M_{CB} = R_B(L-x) + M_B$$

$$\text{Cortante } V_{AC} = R_A - w_0 x \quad V_{CB} = -R_B$$

$$\text{Reacciones } R_A = \frac{3w_0 L}{8} - \frac{M_A - M_B}{L} \quad R_B = \frac{w_0 L}{8} + \frac{M_A - M_B}{L}$$

$$\text{Siendo } M_A = \frac{-11w_0 L^2}{192} \quad M_B = \frac{-5w_0 L^2}{192}$$

Viga empotrada - Carga uniforme parcial en un lado



$$\text{Deflexión } y_{AC} = \frac{-x^2}{24EI} (w_0 x^2 - 4R_A x - 12M_A)$$

$$y_{CB} = \frac{3(M_B + LR_B)x^2 - R_B x^3}{6EI} +$$

$$+ \frac{L^2(3M_B + LR_B) - 3(2M_B + LR_B)Lx}{6EI}$$

$$\text{Pendiente } \theta_{AC} = \frac{-x}{6EI} (w_0 x^2 - 3R_A x - 6M_A)$$

$$\theta_{CB} = \frac{-1}{2EI} [R_B x^2 - 2(M_B + LR_B)x + L(2M_B + LR_B)]$$

$$\text{Momento } M_{AC} = R_A x + M_A - \frac{w_0 x^2}{2} \quad M_{CB} = R_B(L-x) + M_B$$

$$\text{Cortante } V_{AC} = R_A - w_0 x \quad V_{CB} = -R_B$$

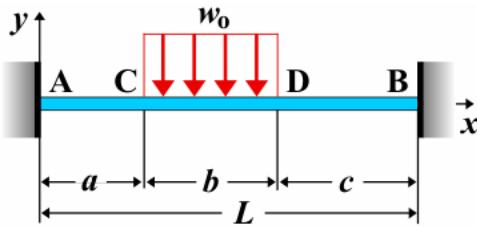
$$\text{Reacciones } R_A = \frac{w_0(L+b)a}{2L} - \frac{M_A - M_B}{L}$$

$$R_B = \frac{w_0 a^2}{2L} + \frac{M_A - M_B}{L}$$

$$\text{Siendo } M_A = \frac{-w_0 a^2}{12L^2} (6L^2 - 8La + 3a^2)$$

$$M_B = \frac{-w_0 a^3}{12L^2} (4L - 3a)$$

Viga empotrada - Carga uniforme parcial



$$\text{Deflexión } y_{AC} = \frac{x^2}{6EI} (3M_A + R_A x)$$

$$y_{CD} = \frac{-1}{24EI} [w_0(x-a)^4 - 4R_A x^3 - 12M_A x^2]$$

$$y_{DB} = \frac{3(M_B + LR_B)x^2 - R_B x^3}{6EI} +$$

$$+ \frac{L^2(3M_B + LR_B) - 3(2M_B + LR_B)Lx}{6EI}$$

$$\text{Pendiente } \theta_{AC} = \frac{x}{2EI} (2M_A + R_A x)$$

$$\theta_{CD} = \frac{-1}{6EI} [w_0(x-a)^3 - 3R_A x^2 - 6M_A x]$$

$$\theta_{DB} = \frac{-1}{2EI} [R_B x^2 - 2(M_B + LR_B)x + L(2M_B + LR_B)]$$

$$\text{Momento } M_{AC} = M_A + R_A x \quad M_{CD} = R_A x + M_A - \frac{w_0(x-a)^2}{2}$$

$$M_{DB} = M_B + R_B(L-x)$$

$$\text{Cortante } V_{AC} = R_A \quad V_{CD} = R_A - w_0(x-a) \quad V_{DB} = -R_B$$

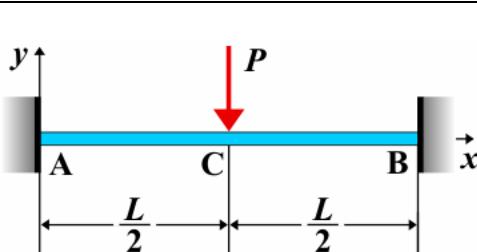
$$\text{Reacciones } R_A = \frac{w_0(2c+b)b - 2M_A + 2M_B}{2L}$$

$$R_B = \frac{w_0(2a+b)b + 2M_A - 2M_B}{2L}$$

$$\text{Siendo } M_A = \frac{-w_0b}{24L^2} [b^2(2L-6c-3b) + (6a+3b)(2c+b)^2]$$

$$M_B = \frac{-w_0b}{24L^2} [b^2(2L-6a-3b) + (6c+3b)(2a+b)^2]$$

Viga empotrada - Carga puntual en el centro



$$\text{Deflexión } y_{AC} = \frac{-Px^2}{48EI} (3L-4x) \quad y_{CB} = \frac{-P(L-x)^2}{48EI} (4x-L)$$

$$\text{Pendiente } \theta_{AC} = \frac{-Px}{8EI} (L-2x) \quad \theta_{CB} = \frac{-P}{8EI} (L^2 - 3Lx + 2x^2)$$

$$\text{Momento } M_{AC} = \frac{-P}{8} (L-4x) \quad M_{CB} = \frac{P}{8} (3L-4x)$$

$$\text{Cortante } V_{AC} = \frac{P}{2} \quad V_{CB} = \frac{-P}{2}$$

$$\text{Reacciones } R_A = R_B = \frac{P}{2}$$

Viga empotrada - Carga puntual en cualquier punto

<p style="margin-top: 20px;">y</p> <p style="margin-top: 20px;">x</p>	<p>Deflexión $y_{AC} = \frac{-Pb^2x^2}{6EIL^3}(3aL - 3ax - bx)$</p> $y_{CB} = \frac{-Pa^2(L-x)^2}{6EIL^3}(3bx - aL + ax)$ <p>Pendiente $\theta_{AC} = \frac{-Pb^2x}{2EIL^3}(2aL - 3ax - bx)$</p> $\theta_{CB} = \frac{Pa^2(L-x)}{2EIL^3}[x(3b+a) - L^2]$ <p>Momento $M_{AC} = \frac{-Pb^2x}{L^3}(aL - 3ax - bx)$</p> $M_{CB} = \frac{Pa^2}{L^3}(L^2 + bL - Lx - 2bx)$ <p>Cortante $V_{AC} = \frac{Pb^2}{L^3}(L + 2a)$ $V_{CB} = \frac{-Pa^2}{L^3}(L + 2b)$</p> <p>Reacciones $R_A = \frac{Pb^2}{L^3}(L + 2a)$ $R_B = \frac{Pa^2}{L^3}(L + 2b)$</p>
---	---

Viga empotrada - Dos cargas puntuales iguales situadas simétricamente

<p style="margin-top: 20px;">y</p> <p style="margin-top: 20px;">x</p>	<p>Deflexión $y_{AC} = \frac{-Px^2}{6EIL}(3aL - 3a^2 - Lx)$</p> $y_{CD} = \frac{-Pa^2}{6EIL}(3Lx - 3x^2 - aL)$ $y_{DB} = \frac{-P(L-x)^2}{6EIL}(3aL - 3a^2 - L(L-x))$ <p>Pendiente $\theta_{AC} = \frac{-Px}{2EIL}(2aL - 2a^2 - Lx)$ $\theta_{CD} = \frac{-Pa^2}{2EIL}(L - 2x)$</p> $\theta_{DB} = \frac{P(L-x)}{2EIL}[2aL - 2a^2 - L(L-x)]$ <p>Momento $M_{AC} = \frac{P}{L}(Lx - aL + a^2)$</p> $M_{CD} = \frac{Pa^2}{L}$ $M_{DB} = \frac{P}{L}(L^2 - Lx - La + a^2)$ <p>Cortante $V_{AC} = P$ $V_{CD} = 0$ $V_{DB} = -P$</p> <p>Reacciones $R_A = R_B = P$</p>
---	--

Viga empotrada - Momento antihorario en el centro

<p>Deflexión $y_{AC} = \frac{M_0 x^2}{8LEI} (2x - L)$ $y_{CB} = \frac{-M_0}{8LEI} (5Lx^2 - 2x^3 - 4L^2x + L^3)$</p> <p>Pendiente $\theta_{AC} = \frac{M_0 x}{4LEI} (3x - L)$ $\theta_{CB} = \frac{-M_0}{8LEI} (10Lx - 6x^2 - 4L^2)$</p> <p>Momento $M_{AC} = \frac{M_0}{4L} (6x - L)$ $M_{CB} = \frac{-M_0}{4L} (5L - 6x)$</p> <p>Cortante $V_{AB} = \frac{3M_0}{2L}$</p> <p>Reacciones $R_A = \frac{3M_0}{2L}$ $R_B = \frac{-3M_0}{2L}$</p>
--

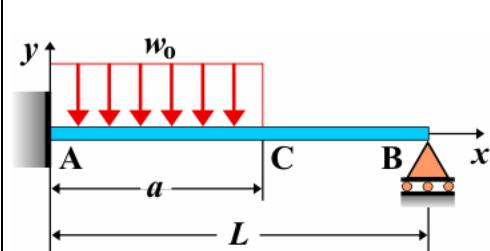
Viga empotrada - Momento antihorario en cualquier punto

<p>Deflexión:</p> $y_{AC} = \frac{-M_0 bx^2}{2L^3 EI} (2aL - 2ax - bL)$ $y_{CB} = \frac{M_0 a(L-x)^2}{2L^3 EI} (2bx - aL)$ <p>Pendiente:</p> $\theta_{AC} = \frac{-M_0 bx}{L^3 EI} (2aL - 3ax - bL)$ $\theta_{CB} = \frac{M_0 a(L-x)}{L^3 EI} (L^2 - 3bx)$ <p>Momento:</p> $M_{AC} = \frac{-M_0 b}{L^3} (2aL - 6ax - bL)$ $M_{CB} = \frac{M_0 a}{L^3} (6bx - 4bL - aL)$ <p>Cortante $V_{AB} = \frac{6M_0 ab}{L^3}$</p> <p>Reacciones $R_A = \frac{6M_0 ab}{L^3}$ $R_B = \frac{-6M_0 ab}{L^3}$</p> <p>Siendo $M_A = \frac{-M_0 b}{L^2} (2a - b)$ $M_B = \frac{M_0 a}{L^2} (2b - a)$</p>
--

Viga empotrada / apoyada - Carga uniforme en todo el vano

<p>Deflexión $y_{AB} = \frac{-w_0 x^2}{48EI} (3L^2 - 5Lx + 2x^2)$</p> <p>Pendiente $\theta_{AB} = \frac{-w_0 x}{48EI} (6L^2 - 15Lx + 8x^2)$</p> <p>Momento $M_{AB} = \frac{-w_0}{8} (L^2 - 5Lx + 4x^2)$</p> <p>Cortante $V_{AB} = \frac{w_0}{8} (5L - 8x)$</p> <p>Reacciones $R_A = \frac{5w_0 L}{8}$ $R_B = \frac{3w_0 L}{8}$</p>
--

Viga empotrada / apoyada - Carga uniforme parcial en el lado empotrado



Deflexión:

$$y_{AC} = \frac{8R_B L(L-x)^3 - 2w_0 L(a-x)^4 - w_0 a^3 (L-x)(L+3b)}{48EI L}$$

$$y_{CB} = \frac{8R_B L(L-x)^3 - w_0 a^3 (L-x)(L+3b)}{48EI L}$$

Pendiente:

$$\theta_{AC} = \frac{-24R_B L(L-x)^2 + 8w_0 L(a-x)^3 + w_0 a^3 (L+3b)}{48EI L}$$

$$\theta_{CB} = \frac{-24R_B L(L-x)^2 + w_0 a^3 (L+3b)}{48EI L}$$

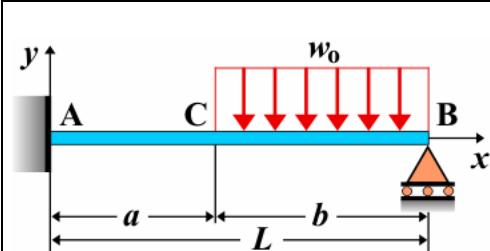
Momento $M_{AC} = \frac{2R_B(L-x) - w_0(a-x)^2}{2}$ $M_{CB} = R_B(L-x)$

Cortante $V_{AC} = -R_B + w_0(a-x)$ $V_{CB} = -R_B$

Reacciones $R_A = \frac{w_0(L+b)a - 2M_A}{2L}$ $R_B = \frac{w_0a^2 + 2M_A}{2L}$

Siendo $M_A = \frac{-w_0(L+b)^2 a^2}{8L^2}$

Viga empotrada / apoyada - Carga uniforme parcial en el lado apoyado



Deflexión $y_{AC} = \frac{x^2}{6EI} (R_A x + 3M_A)$

$$y_{CB} = \frac{4R_B L(L-x)^3 - w_0 L(L-x)^4}{24EI L} + \\ + \frac{-w_0 b^2 (L-x)(bL+3ab+6a^2)}{48EI L}$$

Pendiente $\theta_{AC} = \frac{x}{2EI} (R_A x + 2M_A)$

$$\theta_{CB} = \frac{-3R_B L(L-x)^2 + w_0 L(L-x)^3}{6EI L} + \frac{w_0 b^2 (bL+3ab+6a^2)}{48EI L}$$

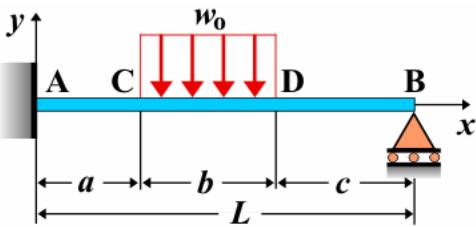
Momento $M_{AC} = R_A x + M_A$ $M_{CB} = \frac{2R_B(L-x) - w_0(L-x)^2}{2}$

Cortante $V_{AC} = R_A$ $V_{CB} = -R_B + w_0(L-x)$

Reacciones $R_A = \frac{w_0 b^2 - 2M_A}{2L}$ $R_B = \frac{w_0(2a+b)b + 2M_A}{2L}$

Siendo $M_A = \frac{-w_0 b^2}{16L^2} [(2L+b)(L+a) - b^2]$

Viga empotrada / apoyada - Carga uniforme parcial



Deflexión

$$y_{AC} = \frac{x^2}{6EI} (R_A x + 3M_A)$$

$$y_{CD} = \frac{4R_B(L-x)^3 - w_0(L-x-c)^4}{24EI} +$$

$$+ \frac{-w_0b(L-x)[2b^2L - 3b^2(2a+b) + 3(2c+b)(2a+b)^2]}{96EIL}$$

$$y_{DB} = \frac{R_B(L-x)^3}{6EI} +$$

$$+ \frac{-w_0b(L-x)[2b^2L - 3b^2(2a+b) + 3(2c+b)(2a+b)^2]}{96EIL}$$

Pendiente

$$\theta_{AC} = \frac{x}{2EI} (R_A x + 2M_A)$$

$$\theta_{CD} = \frac{-3R_B(L-x)^2 + w_0(L-x-c)^3}{6EI} +$$

$$+ \frac{w_0b[2b^2L - 3b^2(2a+b) + 3(2c+b)(2a+b)^2]}{96EIL}$$

$$\theta_{DB} = \frac{-R_B(L-x)^2}{2EI} +$$

$$+ \frac{w_0b[2b^2L - 3b^2(2a+b) + 3(2c+b)(2a+b)^2]}{96EIL}$$

Momento

$$M_{AC} = R_A x + M_A$$

$$M_{CD} = \frac{2R_B(L-x) - w_0(L-x-c)^2}{2} \quad M_{DB} = R_B(L-x)$$

Cortante

$$V_{AC} = R_A \quad V_{CD} = w_0(L-x-c) - R_B \quad V_{DB} = -R_B$$

Reacciones

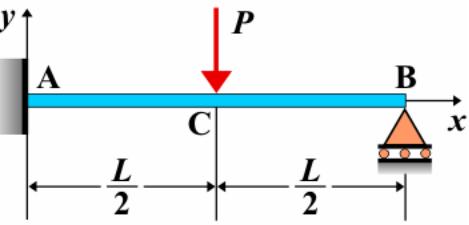
$$R_A = \frac{w_0b(2c+b) - 2M_A}{2L}$$

$$R_B = \frac{w_0(2a+b)b + 2M_A}{2L}$$

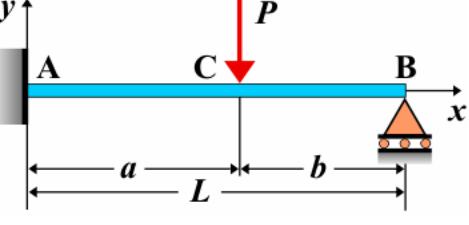
Siendo

$$M_A = \frac{-w_0(2c+b)(2a+b)b[(2L+2c+b)(2a+b) - b^2]}{16L^2}$$

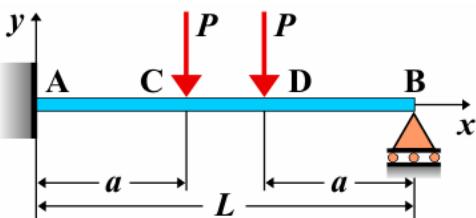
Viga empotrada / apoyada - Carga puntual en el centro

 <p>Deflexión:</p> $y_{AC} = \frac{-Px^2}{96EI} (9L - 11x) \quad y_{CB} = \frac{-P(L-x)}{96EI} (3L^2 - 5(L-x)^2)$ <p>Pendiente:</p> $\theta_{AC} = \frac{-Px}{32EI} (6L - 11x) \quad \theta_{CB} = \frac{-P}{32EI} (4L^2 - 10Lx + 5x^2)$ <p>Momento</p> $M_{AC} = \frac{-P}{16} (3L - 11x) \quad M_{CB} = \frac{5P}{16} (L - x)$ <p>Cortante</p> $V_{AC} = \frac{11P}{16} \quad V_{CB} = \frac{-5P}{16}$ <p>Reacciones</p> $R_A = \frac{11P}{16} \quad R_B = \frac{5P}{16}$
--

Viga empotrada / apoyada - Carga puntual en cualquier punto

 <p>Deflexión</p> $y_{AC} = \frac{-Pbx^2}{12EIL^3} (3L^3 - 3b^2L - 3L^2x + b^2x)$ $y_{CB} = \frac{-Pa^2(L-x)}{12EIL^3} (3bL^2 - (2L+b)(L-x)^2)$ <p>Pendiente</p> $\theta_{AC} = \frac{-Pbx}{4EIL^3} (2L^3 - 2b^2L - 3L^2x + b^2x)$ $\theta_{CB} = \frac{-Pa^2}{4EIL^3} (2L^3 - 4L^2x - 2bLx + 2Lx^2 + bx^2)$ <p>Momento:</p> $M_{AC} = \frac{-Pb}{2L^3} (L^3 - b^2L - 3L^2x + b^2x) \quad M_{CB} = \frac{Pa^2}{2L^3} (L - x)(2L + b)$ <p>Cortante</p> $V_{AC} = \frac{Pb}{2L^3} (3L^2 - b^2) \quad V_{CB} = \frac{-Pa^2}{2L^3} (2L + b)$ <p>Reacciones</p> $R_A = \frac{Pb}{2L^3} (3L^2 - b^2) \quad R_B = \frac{Pa^2}{2L^3} (2L + b)$
--

Viga empotrada / apoyada - Dos cargas puntuales iguales situadas simétricamente



Deflexión:

$$y_{AC} = \frac{Px^2}{12EI L^2} [(3a^2 - 3aL - 2L^2)(L-x) + 2L(3a^2 - 3aL + L^2)]$$

$$y_{CD} = \frac{-Pa(3(L-a)(L-x)^3 - 6L^2(L-x)^2)}{12EI L^2} +$$

$$+ \frac{-Pa[3L^2(L+a)(L-x) - 2L^2a^2]}{12EI L^2}$$

$$y_{DB} = \frac{-P(L-x)}{12EI L^2} [(3aL - 3a^2 - 2L^2)(L-x)^2 + 3aL^2(L-a)]$$

Pendiente:

$$\theta_{AC} = \frac{Px}{12EI L^2} [(3a^2 - 3aL - 2L^2)(2L - 3x) + 4L(3a^2 - 3aL + L^2)]$$

$$\theta_{CD} = \frac{-Pa}{4EI L^2} [-3(L-a)(L-x)^2 + 4L^2(L-x) - L^2(L+a)]$$

$$\theta_{DB} = \frac{P}{4EI L^2} [(3aL - 3a^2 - 2L^2)(L-x)^2 + aL^2(L-a)]$$

Momento $M_{AC} = \frac{P}{2L^2} [3a^2L - 3aL^2 + x(2L^2 + 3aL - 3a^2)]$

$$M_{CD} = \frac{-Pa}{2L^2} [3(L-a)(L-x) - 2L^2]$$

$$M_{DB} = \frac{-P(L-x)}{2L^2} (3aL - 3a^2 - 2L^2)$$

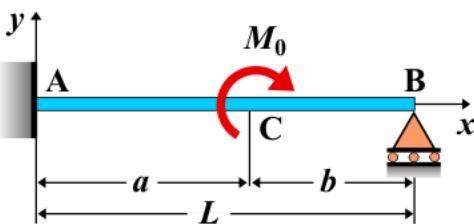
Cortante $V_{AC} = \frac{P}{2L^2} (2L^2 + 3aL - 3a^2) \quad V_{CD} = \frac{3Pa(L-a)}{2L^2}$

$$V_{DB} = \frac{P}{2L^2} (3aL - 3a^2 - 2L^2)$$

Reacciones $R_A = \frac{P}{2L^2} (2L^2 + 3aL - 3a^2)$

$$R_B = \frac{P}{2L^2} (3a^2 + 2L^2 - 3aL)$$

Viga empotrada / apoyada - Momento horario en cualquier punto



Deflexión: $y_{AC} = \frac{-M_0 x^2}{4EI L^3} [2b^2 L - (L-x)(L^2 - b^2)]$
 $y_{CB} = \frac{-M_0 a(L-x)}{4EI L^3} [-4L^3 - ((L-x)^2 - 3L^2)(L+b)]$

Pendiente $\theta_{AC} = \frac{-M_0 x}{4EI L^3} [4b^2 L - (2L-3x)(L^2 - b^2)]$
 $\theta_{CB} = \frac{-M_0 a}{4EI L^3} [4L^3 - 3(L+b)(x^2 - 2Lx)]$

Momento $M_{AC} = \frac{-M_0}{2L^3} [2b^2 L - (L-3x)(L^2 - b^2)]$
 $M_{CB} = \frac{3M_0 a}{2L^3} (L+b)(L-x)$

Cortante $V_{AB} = \frac{-3M_0 a}{2L^3} (L+b)$

Reacciones $R_A = \frac{-3M_0 a}{2L^3} (L+b)$ $R_B = \frac{3M_0 a}{2L^3} (L+b)$

Viga empotrada / apoyada - Momento horario en el lado apoyado



Deflexión $y_{AB} = \frac{M_0 x^2 (L-x)}{4EI L}$

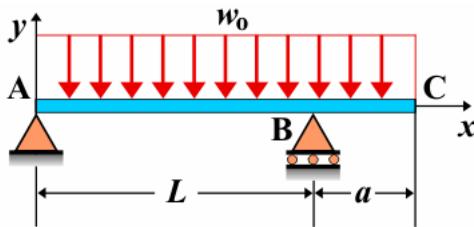
Pendiente $\theta_{AB} = \frac{M_0 x (2L-3x)}{4EI L}$

Momento $M_{AB} = \frac{M_0 (L-3x)}{2L}$

Cortante $V_{AB} = \frac{-3M_0}{2L}$

Reacciones $R_A = \frac{-3M_0}{2L}$ $R_B = \frac{3M_0}{2L}$

Viga con vano lateral - Carga uniforme en todo el vano



Deflexión $y_{AB} = \frac{-w_0 x}{24EI} (L^4 - 2L^2x^2 + Lx^3 - 2a^2L^2 + 2a^2x^2)$

$$y_{BC} = \frac{-w_0 x_1}{24EI} (4a^2L - L^3 + 6a^2x_1 - 4ax_1^2 + x_1^3)$$

Pendiente $\theta_{AB} = \frac{-w_0}{24EI} (L^4 - 6L^2x^2 + 4Lx^3 - 2a^2L^2 + 6a^2x^2)$

$$\theta_{BC} = \frac{-w_0}{24EI} (4a^2L - L^3 + 12a^2x_1 - 12ax_1^2 + 4x_1^3)$$

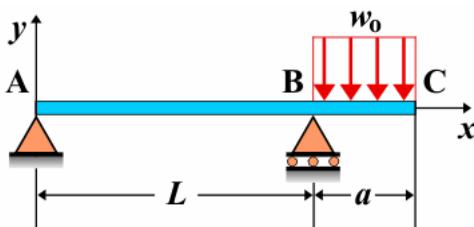
Momento $M_{AB} = \frac{w_0 x}{2L} (L^2 - Lx - a^2) \quad M_{BC} = \frac{-w_0}{2} (a - x_1)^2$

Cortante $V_{AB} = \frac{w_0}{2L} (L^2 - 2Lx - a^2) \quad V_{BC} = w_0(a - x_1)$

Reacciones $R_A = \frac{w_0}{2L} (L^2 - a^2) \quad R_B = \frac{w_0}{2L} (L + a)^2$

Siendo $x_1 = x - L$

Viga con vano lateral - Carga uniforme sobre el saliente



Deflexión $y_{AB} = \frac{w_0 a^2 x}{12EI} (L^2 - x^2)$

$$y_{BC} = \frac{-w_0 x_1}{24EI} (4a^2L + 6a^2x_1 - 4ax_1^2 + x_1^3)$$

Pendiente $\theta_{AB} = \frac{w_0 a^2}{12EI} (L^2 - 3x^2)$

$$\theta_{BC} = \frac{-w_0}{6EI} (a^2L + 3a^2x_1 - 3ax_1^2 + x_1^3)$$

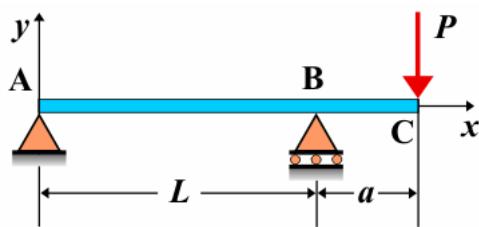
Momento $M_{AB} = \frac{-w_0 a^2 x}{2L} \quad M_{BC} = \frac{-w_0}{2} (a - x_1)^2$

Cortante $V_{AB} = \frac{-w_0 a^2}{2L} \quad V_{BC} = w_0(a - x_1)$

Reacciones $R_A = \frac{-w_0 a^2}{2L} \quad R_B = \frac{w_0(2L+a)a}{2L}$

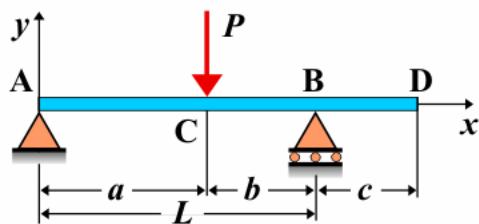
Siendo $x_1 = x - L$

Viga con vano lateral - Carga puntual en el extremo saliente



Deflexión $y_{AB} = \frac{Pax}{6LEI}(L^2 - x^2)$ $y_{BC} = \frac{-Px_1}{6EI}(2aL + 3ax_1 - x_1^2)$
 Pendiente $\theta_{AB} = \frac{Pa}{6LEI}(L^2 - 3x^2)$ $\theta_{BC} = \frac{-P}{6EI}(2aL + 6ax_1 - 3x_1^2)$
 Momento $M_{AB} = \frac{-Pax}{L}$ $M_{BC} = -P(a - x_1)$
 Cortante $V_{AB} = \frac{-Pa}{L}$ $V_{BC} = P$
 Reacciones $R_A = \frac{-Pa}{L}$ $R_B = \frac{P(L+a)}{L}$
 Siendo $x_1 = x - L$

Viga con vano lateral - Carga puntual entre los apoyos



Deflexión $y_{AC} = \frac{-Pbx}{6LEI}(L^2 - b^2 - x^2)$
 $y_{CB} = \frac{-Pa(L-x)}{6LEI}(2Lx - a^2 - x^2)$
 $y_{BD} = \frac{Pabx_1}{6LEI}(L + a)$
 Pendiente $\theta_{AC} = \frac{-Pb}{6LEI}(L^2 - b^2 - 3x^2)$
 $\theta_{CB} = \frac{-Pa}{6LEI}(2L^2 - 6Lx + a^2 + 3x^2)$ $\theta_{BD} = \frac{Pab(L+a)}{6LEI}$
 Momento $M_{AC} = \frac{Pbx}{L}$ $M_{CB} = \frac{Pa}{L}(L-x)$ $M_{BD} = 0$
 Cortante $V_{AC} = \frac{Pb}{L}$ $V_{CB} = \frac{-Pa}{L}$ $V_{BD} = 0$
 Reacciones $R_A = \frac{Pb}{L}$ $R_B = \frac{Pa}{L}$
 Siendo $x_1 = x - L$