

a) ultrasonic waves travel Δt_{sp} : $v_p = 6 \text{ km/s}$

$$\cdot (T_s - T_p)_A = 9,95 \text{ s}$$

$$\cdot (T_s - T_p)_B = 8,12 \text{ s}$$

• Rayon position:

$$v_p = \sqrt{3} v_s$$

$$v_s \approx 3,5 \text{ km/s}$$

$$\Rightarrow v = \frac{d}{t} \Rightarrow t = \frac{d}{v}$$

$$\underline{A}: (T_s - T_p) = \left(\frac{d}{v_s} - \frac{d}{v_p} \right)$$

$$= d \left(\frac{1}{3,5 \text{ km/s}} - \frac{1}{6 \text{ km/s}} \right) = d \cdot 0,119 \text{ s/km}$$

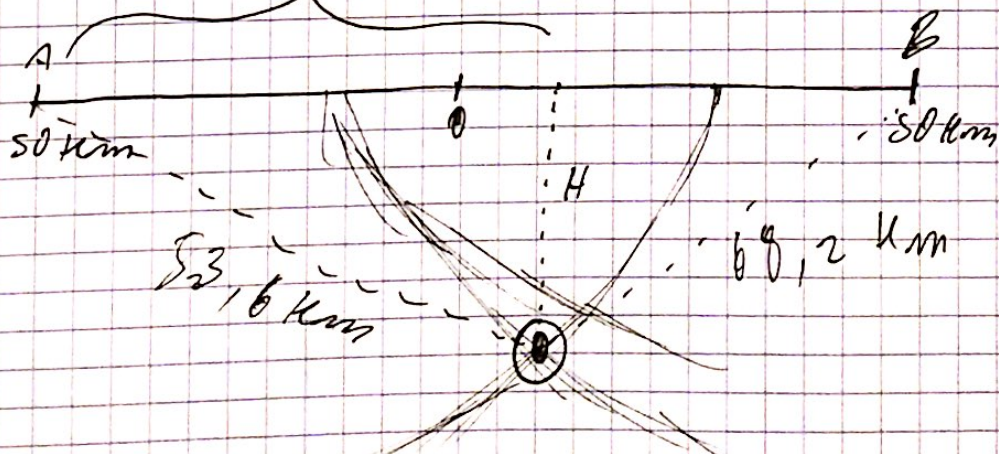
$$\Rightarrow \frac{9,95 \text{ s}}{0,119 \text{ s/km}} = 83,6 \text{ km} = d_A$$

$$\underline{B}: d_B = \frac{8,12 \text{ s}}{0,119 \text{ s/km}} = 68,2 \text{ km}$$

Pythagorean

$$67,68 \text{ km}$$

$$\Rightarrow H = 56,42 \text{ km}$$



b) Calcular T_p y T_s para A y B:

$$v = \frac{d}{t} \Rightarrow t = \frac{d}{v}$$

A:

$$T_p = \frac{83,6 \text{ km}}{6 \text{ km/s}} = 13,9 \text{ s}$$

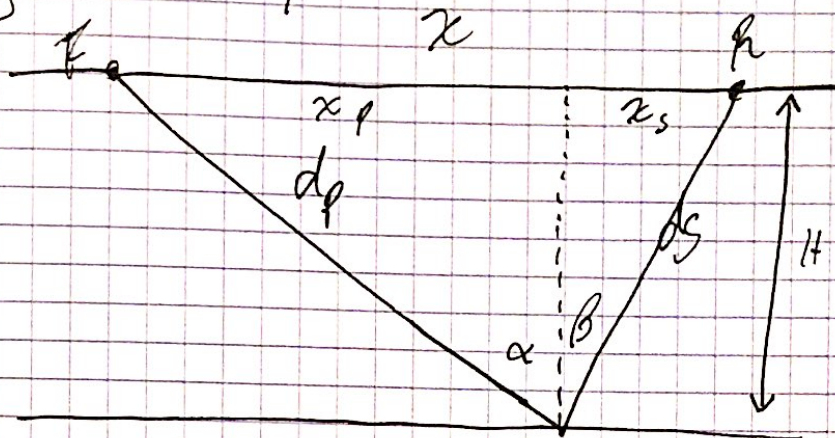
$$T_s = \frac{83,6 \text{ km}}{3,5 \text{ km/s}} = 23,9 \text{ s}$$

B:

$$T_p = \frac{68,2 \text{ km}}{6 \text{ km/s}} = 11,4 \text{ s}$$

$$T_s = \frac{68,2 \text{ km}}{3,5 \text{ km/s}} = 19,5 \text{ s}$$

$P_2 \quad v_s < v_p$



$$T_R = \frac{d_p}{v_p} + \frac{d_s}{v_s}$$

$$d_p = \sqrt{(x - x_p)^2 + H^2}$$

$$d_s = \sqrt{(x - x_s)^2 + H^2}$$

$$T_R = \frac{\sqrt{(x - x_p)^2 + H^2}}{v_p} + \frac{\sqrt{(x - x_s)^2 + H^2}}{v_s}$$

* Principiu de Fermat: trajectoria que segue uma onda sobre um medio e aquela que minimiza T .

$$\Rightarrow \frac{dT}{dx} = 0$$

$$\Rightarrow \frac{dT_R}{dx} = \frac{1}{x} \frac{x(x - x_p)}{\sqrt{(x - x_p)^2 + H^2}} v_p + \frac{1}{x} \frac{x(x - x_s)}{\sqrt{(x - x_s)^2 + H^2}} v_s = 0$$

$$\Rightarrow v_p \frac{x - x_p}{d_p} = \frac{x - x_s}{v_s d_s}$$

$$\Rightarrow \frac{\sin \alpha}{v_p} = \frac{\sin \beta}{v_s}$$

$$\Delta: \chi \gg H \quad \Rightarrow \quad \alpha \Rightarrow \frac{\pi}{2} \quad \text{and} \quad \beta \Rightarrow \frac{\pi}{2}$$

$$\Rightarrow \quad v_f = v_s$$