

(II)

Problema 2

1) Comenzamos calculando los parámetros. No calculamos la tangente de perdidas porque no vamos a hacer aproximaciones.

$$V = 6 \cdot 10^{17} \text{ Hz}$$

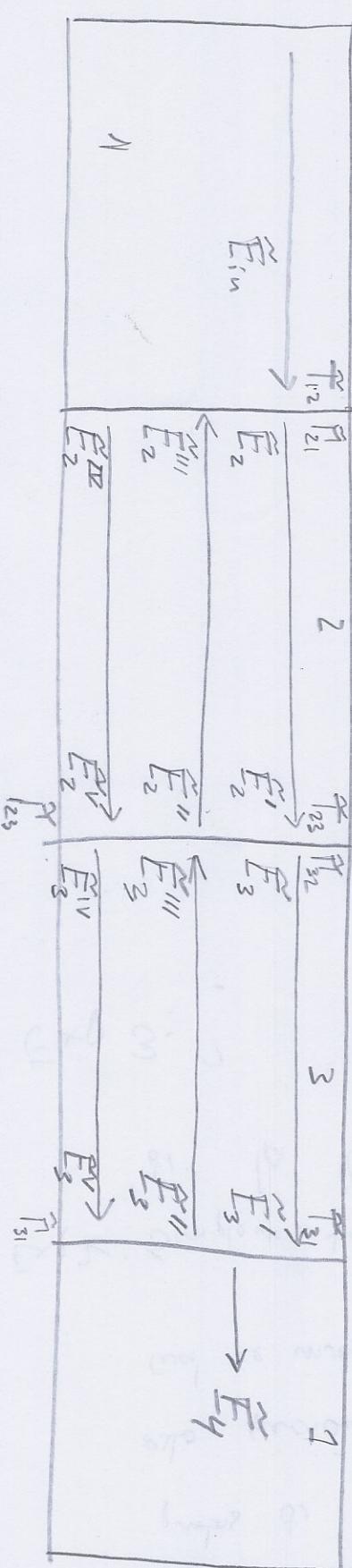
$$\omega = 2\pi V = 3.76991 \cdot 10^{18} \frac{\text{rad}}{\text{s}}$$

Vacio	Metal: Bronce	Vacio
ϵ_0	σ_2	ϵ_0
μ_0	μ_2	μ_0
ϵ_1	σ_1	ϵ_1
μ_1	τ_{12}	μ_1
Medio 1	Medio 2	Medio 3
		Medio 4
		Medio 1

$$d_2 = 2 \cdot 3 \cdot 10^{-2} \text{ m}$$

$$d_3 = 3 \cdot 10^{-3} \text{ m}$$

dónde parámetros necesitamos?



$$\begin{aligned}\tilde{E}_2 &= \tilde{E}'_{in} \tilde{T}_{12}^{\nu} ; \quad \tilde{E}'_2 = \tilde{E}_2' \tilde{e}^{-\alpha_2 d_2} = \tilde{E}'_{in} \tilde{T}_{12}^{\nu} e^{-\alpha_2 d_2}, \quad \tilde{E}_2'' = \tilde{E}_2' \tilde{T}_{23}^{\nu} = \tilde{E}'_{in} \tilde{T}_{12}^{\nu} \tilde{T}_{23}^{\nu} e^{-\alpha_2 d_2} \\ \tilde{E}_2''' &= \tilde{E}_2' \tilde{T}_{12}^{\nu} \tilde{T}_{23}^{\nu} \tilde{e}^{-\alpha_2 d_2} e^{\alpha_2 d_2}; \quad \tilde{E}_2^{IV} = \tilde{E}_2''' \tilde{T}_{21}^{\nu} = \tilde{E}'_{in} \tilde{T}_{12}^{\nu} \tilde{T}_{23}^{\nu} \tilde{T}_{21}^{\nu} e^{-\alpha_2 d_2} e^{\alpha_2 d_2}\end{aligned}$$

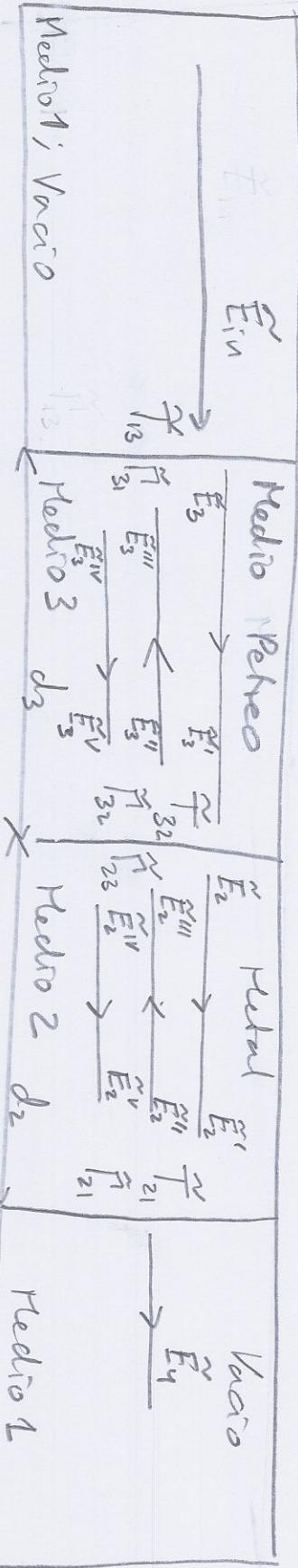
$$\begin{aligned}\tilde{E}_2^{\nu} &= \tilde{E}_2' \tilde{T}_{12}^{\nu} \tilde{e}^{-\alpha_2 d_2} = \tilde{E}'_{in} \tilde{T}_{12}^{\nu} \tilde{T}_{23}^{\nu} \tilde{T}_{21}^{\nu} \tilde{e}^{-\alpha_2 d_2} e^{\alpha_2 d_2} = \tilde{E}'_{in} \tilde{T}_{12}^{\nu} \tilde{T}_{23}^{\nu} \tilde{T}_{21}^{\nu} \tilde{e}^{-3\alpha_2 d_2} \\ \tilde{E}_3 &= (\tilde{E}_2' + \tilde{E}_2^{\nu}) \tilde{T}_{23}^{\nu} = \tilde{E}'_{in} \tilde{e}^{-\alpha_2 d_2} \tilde{T}_{12}^{\nu} (1 + \tilde{T}_{23}^{\nu} \tilde{T}_{21}^{\nu} \tilde{e}^{-2\alpha_2 d_2}) \tilde{T}_{23}^{\nu} \\ \tilde{E}_3' &= \tilde{E}_3^{\nu} \tilde{e}^{-\alpha_2 d_2}; \quad \tilde{E}_3'' = \tilde{E}_3' \tilde{T}_{31}^{\nu}; \quad \tilde{E}_3''' = \tilde{E}_3'' \tilde{e}^{\alpha_3 d_3}; \quad \tilde{E}_3^{\nu} = \tilde{E}_3''' \tilde{e}^{-\alpha_3 d_3}; \quad \tilde{E}_3 = \tilde{E}_3^{\nu} \tilde{e}^{-\alpha_3 d_3} \\ \tilde{E}_4 &= (\tilde{E}_2^{\nu} + \tilde{E}_3') \tilde{T}_{31}^{\nu} = (\tilde{E}'_{in} \tilde{e}^{-\alpha_2 d_2} \tilde{T}_{12}^{\nu} \tilde{T}_{23}^{\nu} (1 + \tilde{T}_{23}^{\nu} \tilde{T}_{21}^{\nu} \tilde{e}^{-2\alpha_2 d_2}) e^{-\alpha_3 d_3}) (1 + \tilde{T}_{31}^{\nu} \tilde{e}^{-2\alpha_3 d_3} \tilde{T}_{32}^{\nu}) \tilde{T}_{31}^{\nu} =\end{aligned}$$

$$= \tilde{E}'_{in} \tilde{T}_{31}^{\nu} \tilde{T}_{12}^{\nu} \tilde{T}_{23}^{\nu} \tilde{e}^{-\alpha_2 d_2 - \alpha_3 d_3} (1 + \tilde{T}_{23}^{\nu} \tilde{T}_{21}^{\nu} \tilde{e}^{-2\alpha_2 d_2}) (1 + \tilde{T}_{31}^{\nu} \tilde{T}_{32}^{\nu} \tilde{e}^{-2\alpha_3 d_3})$$

$$|\tilde{E}_{in}| \cdot |\tilde{T}_{31}^{\nu} \tilde{T}_{12}^{\nu} \tilde{T}_{23}^{\nu} \tilde{e}^{-\alpha_2 d_2 - \alpha_3 d_3} (1 + \tilde{T}_{23}^{\nu} \tilde{T}_{21}^{\nu} \tilde{e}^{-2\alpha_2 d_2}) (1 + \tilde{T}_{31}^{\nu} \tilde{T}_{32}^{\nu} \tilde{e}^{-2\alpha_3 d_3})| = \text{Fumbral} = \frac{|\mu V|}{m}$$

$$|\tilde{E}_{in}|_{T_0} = \frac{\text{Fumbral}}{|\tilde{T}_{31}^{\nu} \tilde{T}_{12}^{\nu} \tilde{T}_{23}^{\nu} \tilde{e}^{-\alpha_2 d_2 - \alpha_3 d_3} (1 + \tilde{T}_{23}^{\nu} \tilde{T}_{21}^{\nu} \tilde{e}^{-2\alpha_2 d_2}) (1 + \tilde{T}_{31}^{\nu} \tilde{T}_{32}^{\nu} \tilde{e}^{-2\alpha_3 d_3})|}$$

$$|\tilde{S}_{in, \sigma}|_{T_0} = \frac{|\tilde{E}_{in}|_{T_0}^2}{2 \cdot \text{Re}(\gamma_i^*)}$$



$$\tilde{E}_3 = \tilde{E}_{in}^{\sim} \tilde{T}_{13}^{\sim}; \quad \tilde{E}_3' = \tilde{E}_3^{\sim} e^{\alpha_3(-d_3)}; \quad \tilde{E}_3'' = \tilde{E}_3^{\sim} \tilde{T}_{32}^{\sim}; \quad \tilde{E}_3''' = \tilde{E}_3^{\sim} e^{\alpha_3 d_3}; \quad \tilde{E}_3'''' = \tilde{T}_{31}^{\sim} \tilde{E}_3^{\sim},$$

$$\tilde{E}_3^{\text{II}} = \tilde{E}_3^{\text{I}} e^{\alpha_3(-d_3)}; \quad \tilde{E}_2 = (\tilde{E}_3^{\sim} + \tilde{E}_3^{\text{I}}) \tilde{T}_{32}^{\sim};$$

$$\tilde{E}_2 = \tilde{T}_{32}^{\sim} \tilde{E}_{in}^{\sim} \tilde{T}_{13}^{\sim} e^{-\alpha_3 d_3} (1 + \tilde{T}_{32}^{\sim} \tilde{T}_{31}^{\sim} e^{-2\alpha_3 d_3})$$

Vemos la simetría en los cálculos luego:

$$|\tilde{E}_{in}| = \frac{E_{in}^{\text{ampl}}}{|\tilde{T}_{13}^{\sim} \tilde{T}_{32}^{\sim} \tilde{T}_{21}^{\sim} e^{-\alpha_2 d_2 - \alpha_3 d_3} (1 + \tilde{T}_{32}^{\sim} \tilde{T}_{21}^{\sim} e^{-2\alpha_2 d_2})|}$$

$$|\tilde{S}_{in, \text{II}}| = \frac{|\tilde{E}_{in}|^2}{2 \operatorname{Re}(Y_2^*)}$$

Necesitamos $\tilde{T}_{12}^{\sim}, \tilde{T}_{23}^{\sim}, \tilde{T}_{31}^{\sim}, \tilde{T}_{13}^{\sim}, \tilde{T}_{32}^{\sim}, \tilde{T}_{21}^{\sim}, \tilde{T}_{23}^{\sim}, \tilde{T}_{32}^{\sim}, \tilde{T}_{31}^{\sim}, \alpha_2, \alpha_3$

$$\left. \begin{array}{l} \tilde{Y}_1, \tilde{Y}_2, \tilde{Y}_3, Y_1, Y_2, Y_3 \\ \tilde{Z}_1, \tilde{Z}_2, \tilde{Z}_3, Z_1, Z_2, Z_3 \end{array} \right\}$$

Obligatoriamente

Cálculo Simplificado sin considerar reflexiones

II

$$|\tilde{E}_{in}|_{\partial\Gamma} = \frac{E_{in}}{|T_{13}\tilde{T}_{12}\tilde{T}_{21}e^{(k_2d_2+\alpha_3d_3)}|}$$

$$\left| \tilde{S}_{in,AR} \right|_{\partial\Gamma} = \frac{\left| \tilde{E}_{in} \right|^2}{2R(\tilde{\rho}_1^*)}$$

Medio 1:	Medio 2:
$\sigma_1 = 0$	$\sigma_2 = 0$
$\tilde{\epsilon}_1 = \epsilon_0$	$\tilde{\epsilon}_2 = \epsilon_0(-9.95 \cdot 10^{-9})$
$\mu_1 = \mu_0$	$\mu_2 = \mu_0$

$$\left| \tilde{E}_{in} \right|_{\partial\Gamma} = \frac{E_{in}}{\left| T_{13}\tilde{T}_{12}\tilde{T}_{21}e^{(k_2d_2+\alpha_3d_3)} \right|}$$

$$\left| \tilde{S}_{in,AR} \right|_{\partial\Gamma} = \frac{\left| \tilde{E}_{in} \right|^2}{2R(\tilde{\rho}_1^*)}$$

$$\begin{aligned} \sigma_3 &= 10^{-2} \\ \epsilon_3 &= 3\epsilon_0 \\ \mu_3 &= \mu_0 \end{aligned}$$

$$Solución: Máximo \left| \tilde{S}_{in,AR} \right|_{\partial\Gamma}, \left| \tilde{S}_{in,AR} \right|_{\partial\Gamma}$$

Cada pixel es por $2.5 \mu\text{m}^2$ luego como cabe esperar es un número muy pequeño.

$$\tilde{\delta}_1 = \sqrt{\nu\omega\mu_1(\sigma_1 + j\omega\epsilon_1)} = 1.2575 \cdot 10^{10} \text{ J}$$

$$\alpha_1 = 0^\circ$$

$$\tilde{\delta}_1 = \frac{\delta\omega\mu_1}{\delta_1^2} = 376.73$$

$$\tilde{\delta}_2 = \sqrt{\nu\omega\mu_2(\sigma_2 + j\omega\epsilon_2)} = 625.61 + 1.2575 \cdot 10^{10} \text{ J}; \alpha_2 = 625.61 \text{ m}^{-1}$$

$$\tilde{\delta}_2 = \frac{\delta\omega\mu_2}{\delta_2^2} = 376.73 + 1.08753 \cdot 10^{-5} \text{ J}$$

$$\tilde{\delta}_3 = \sqrt{\nu\omega\mu_3(\sigma_3 + j\omega\epsilon_3)} = 1.08753 + 2.178 \cdot 10^{10} \text{ J}; \alpha_3 = 1.08753$$

$$\tilde{\delta}_3 = 217.505 + 1.08602 \cdot 10^{-8} \text{ J}$$

$$\tilde{T}_{12} = \frac{2\tilde{\delta}_2}{\tilde{\delta}_1 + \tilde{\delta}_2} = 1 + 2.4875 \cdot 10^{-8} \text{ J} \quad \tilde{T}_{13} = 0.732051 + 2.3173 \cdot 10^{-11} \text{ J} = \frac{2\tilde{\delta}_3}{\tilde{\delta}_2 + \tilde{\delta}_3}$$

$$\tilde{T}_{21} = \frac{2\tilde{\delta}_1}{\tilde{\delta}_2 + \tilde{\delta}_1} = 1 - 2.4875 \cdot 10^{-8} \text{ J} \quad \tilde{T}_{31} = 1.26795 - 2.3173 \cdot 10^{-11} \text{ J} = \frac{2\tilde{\delta}_2}{\tilde{\delta}_1 + \tilde{\delta}_2}$$

$$\tilde{T}_{23} = (2\tilde{\delta}_2) / (2\tilde{\delta}_1 + \tilde{\delta}_3) = 0.732051 - 2.30659 \cdot 10^{-8} \text{ J} \quad \tilde{T}_{32} = 1.26795 + 2.30659 \cdot 10^{-8} \text{ J}$$

II

Calculo con reflexiones

$$\begin{aligned} \tilde{P}_{21} &= \frac{\tilde{V}_1 - \tilde{V}_2}{\tilde{V}_1 + \tilde{V}_2} = 1.019187 \cdot 10^{-15} - 2.4875 \cdot 10^{-8} j \\ \tilde{P}_{23} &= \frac{\tilde{V}_1 - \tilde{V}_3}{\tilde{V}_1 + \tilde{V}_3} = -0.267949 - 2.30659 \cdot 10^{-8} j \end{aligned}$$

$$|\tilde{E}_{in}|_{DI} = -\tilde{P}_{23}$$

$$|\tilde{E}_{in}|_{DI} = 4.025 \frac{mW}{m^2}$$

$$\text{Expresado en pixels} \\ 4.025 \frac{mW}{m^2} \left(\frac{1m}{10^6 \mu m} \right)^2 \frac{2.5 \mu m^2}{\text{pixel}} = 10^{-11} \frac{mW}{\text{pixel}}$$

$$\tilde{P}_{31} = \frac{\tilde{V}_1 - \tilde{V}_3}{\tilde{V}_1 + \tilde{V}_3} = 0.267949 - 2.3173 \cdot 10^{-11} j$$

$$|\tilde{E}_{in}|_{DI} = 1.79029 \frac{V}{m}$$

Identico, por definición de medios, una dirección era suficiente

Cálculo simple, sin reflexiones

$$|\tilde{E}_{in}|_{DI}^{SIM} = 1.918 \frac{V}{m}$$

$\left. \begin{array}{l} \frac{2k}{E_{in}} \sin = 1.918 \frac{V}{m} \\ |\tilde{E}_{in}|_{DI} = 1.918 \frac{V}{m} \end{array} \right\} \text{LAS REFLEXIONES NO SE PUEDEN DESPRECiar}$

Los números no se evaluan sólo el enfoque analítico

Problema 3

a) Vemos que $\tilde{\epsilon} = \epsilon' + \epsilon'' j$, luego tenemos de ver como es la tangente de perdidas en este caso.

Partimos de la ecuación de Ampere-Harwell

$$\nabla \times \vec{H}(F) = \vec{J}(F) + j \mu \vec{B}(F), \text{ sumamos masas } LHF$$

$$\nabla \times \vec{H}(F) = \sigma \vec{E}(F) + j \mu \vec{E}(F) = (\sigma + j \mu (\epsilon' + \epsilon'' j)) \vec{E}(F) \Rightarrow$$

$$\nabla \times \vec{H}(F) = (\sigma - \mu \epsilon'' + j \mu \epsilon') \vec{E}(F) \Rightarrow \vec{J}_c(F) = (\sigma - \mu \epsilon'') \vec{E}(F)$$

$$\vec{J}_d(F) = j \mu \epsilon' \vec{E}(F)$$

$$\tan \theta_E = \frac{|\vec{J}_d(F)|}{|\vec{J}_d(F)|} = \mu \epsilon'$$

Medio 1:

$$\left\{ \begin{array}{l} \mu_1 = 1/\mu_0 \\ \epsilon_1'' = 0.05\epsilon_0 \end{array} \right.$$

Sustituimos

$$\text{Medio 1: } \tan \theta_{E1} = \frac{\sigma_1 - \mu \epsilon_1''}{\mu \epsilon_1'} = 0.0194 > 0.01$$

$$\text{Medio 2: } \left\{ \begin{array}{l} \sigma_2 = 6.6 \cdot 10^{-4} \\ \epsilon_2' = 1.05\epsilon_0 \\ \epsilon_2'' = 0 \end{array} \right.$$

$$\tan \theta_{E2} = \frac{\sigma_2 - \mu \epsilon_2''}{\mu \epsilon_2'} = 0.01986 > 0.01$$



No son ni buenos dielectricos ni buenos conductores

(VII)

Medio 1
Fibra de
carbono
 $\tilde{\epsilon}_1, \mu_1, \sigma$

Medio 2
Aire humedo
 $\tilde{\epsilon}_2, \mu_2, \sigma$

$$\tilde{\gamma} = \sqrt{j\omega\mu(\sigma + j\omega\tilde{\epsilon})} = \sqrt{\omega\mu((\sigma - \tilde{\epsilon}'\omega) - \tilde{\epsilon}''\omega)}$$

b)

$$\tilde{\gamma}_1 = \sqrt{j\omega\mu_1((\sigma_1 - \omega\tilde{\epsilon}_1'')j - \tilde{\epsilon}_1''\omega)} = \sqrt{j\omega\mu_1(\sigma_1 + j\omega\tilde{\epsilon}_1')} = 0.306254 + 31.3913j$$

$$\tilde{\gamma}_2 = \sqrt{j\omega\mu_2((\sigma_2 - \omega\tilde{\epsilon}_2'')j - \tilde{\epsilon}_2''\omega)} = \sqrt{j\omega\mu_2(\sigma_2 + j\omega\tilde{\epsilon}_2')} = 0.121352 + 21.686j$$

$$\alpha_1 = \operatorname{Re}(\tilde{\gamma}_1) = 0.306252$$

$$\beta_1 = \operatorname{Im}(\tilde{\gamma}_1) = 31.3913$$

$$\alpha_2 = \operatorname{Re}(\tilde{\gamma}_2) = 0.121352$$

$$\beta_2 = \operatorname{Im}(\tilde{\gamma}_2) = 21.686$$

$$\tilde{\gamma}_1 = \frac{j\omega\mu_1}{\tilde{\gamma}_2} = 2.79.417 + 2.72599j$$

$$\tilde{\gamma}_2 = \frac{j\omega\mu_2}{\tilde{\gamma}_1} = 367.721 + 2.05771j$$

$$b) \left| \vec{S}_{AV} (\vec{F}_{\text{Antena}}) \right| = \frac{|\vec{E}_{\text{Drone}} (\vec{F}_{\text{Antena}})|}{2 \operatorname{Re}(\tilde{\gamma}_2^*)} |\vec{E}_{\text{DRONE}} (\vec{F}_{\text{Antena}})| = \sqrt{2 \operatorname{Re}(\tilde{\gamma}_1^*)} \left| \vec{S}_{AV} (\vec{F}_{\text{Antena}}) \right| \quad (\text{VII})$$

$$= 1398.54$$

$$c) \left| \vec{E}_{\text{OPERADOR}} (\vec{F}_{\text{Antena}}) \right| = \sqrt{2 \operatorname{Re}(\tilde{\gamma}_2^*)} \left| \vec{S}_{AV} (\vec{F}_{\text{Antena}}) \right| = 1917.6$$

$$d) \quad \tilde{T}_{12} = \frac{2\tilde{\gamma}_2}{\tilde{\gamma}_1 + \tilde{\gamma}_2} = 1.13644 - 0.00204124j$$

$$e) \quad \tilde{T}_{21} = \frac{2\tilde{\gamma}_1}{\tilde{\gamma}_1 + \tilde{\gamma}_2} = 0.863562 + 0.00204124j$$

$$f) \quad E_{\text{Umbral, Drone}} \leq \left| \vec{E}_{\text{OPERANDO}} (\vec{F}_{\text{Antena, operador}}) \right| \cdot e^{\alpha_2 (-X_2)} \left| \tilde{T}_{21} \right| e^{\alpha_1 (-d_1)}$$

$$d_1 = 5 \cdot 10^{-3} m$$

$$X_2^{op} \leq -\frac{1}{\alpha_2} \ln \left(\frac{E_{\text{Umbral, Drone}}}{\left| \vec{E}_{\text{OPERANDO}} (\vec{F}_{\text{Antena, operador}}) \right| \left| \tilde{T}_{21} \right| e^{-\alpha_1 d_1}} \right) = 182.465 m$$

$$g) \quad X_2^{op} \leq -\frac{1}{\alpha_2} \left(\frac{E_{\text{Umbral, OPERADOR}}}{\left| \vec{E}_{\text{DRONE}} (\vec{F}_{\text{Antena}}) \right| \left| \tilde{T}_{12} \right| e^{-\alpha_1 d_1}} \right) = 186 m$$

b)

Si $X_2^{00} > X_2^{D0} \Rightarrow$ Canal 1 es el limitante

Si $X_2^{00} < X_2^{D0} \Rightarrow$ Canal 2 es el limitante

Numeros dicen que el Canal 2 es el canal limitante

i) Para saber si se logra o no se comprueba

$$\text{Mínimo } \{X_2^{00}, X_2^{D0}\} > 160 \text{ m se logra}$$

Otro caso no se logra. Numeros dicen

$$\text{que se logra } 182.465 \text{ m} > 160 \text{ m}$$

Nota a ayudantes: Se evaluará solo el enfoque analítico

(IV)

P2

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#cXVlcmlcz1udSUzRDYqMTAINUUoMTcpJnF1ZXJpZXM9dyUzRDIqUGkqbnUmcXVlcmlcz1OJ
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P3

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#cXVlcmlcz1udSUzRDEuMDEqMTA1NUUoOSklMEF3JTNEMipQaSpudSUwQWUwJTNEOC44N
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