

$$\hat{T} = \frac{d\vec{r}}{ds} / \left\| \frac{d\vec{r}}{ds} \right\| \quad \text{pero } \left\| \frac{d\vec{r}}{ds} \right\| = 1$$

$$\Rightarrow \boxed{\hat{T} = \frac{d\vec{r}}{ds} = -\frac{a}{c} \sin\left(\frac{s}{c}\right) \hat{i} + \frac{a}{c} \cos\left(\frac{s}{c}\right) \hat{j} + \frac{b}{c} \hat{k}} \quad [0,2 \text{ pts}]$$

$$\hat{N} = \frac{d\hat{T}}{ds} / \left\| \frac{d\hat{T}}{ds} \right\|$$

$$\frac{d\hat{T}}{ds} = -\frac{a}{c^2} \cos\left(\frac{s}{c}\right) \hat{i} - \frac{a}{c^2} \sin\left(\frac{s}{c}\right) \hat{j} + 0 \hat{k}$$

$$\left\| \frac{d\hat{T}}{ds} \right\| = \frac{a}{c^2} \sqrt{\cos^2\left(\frac{s}{c}\right) + \sin^2\left(\frac{s}{c}\right)} = \frac{a}{c^2}$$

$$\Rightarrow \boxed{\hat{N} = -\cos\left(\frac{s}{c}\right) \hat{i} - \sin\left(\frac{s}{c}\right) \hat{j}} \quad [0,2 \text{ pts}]$$

$$\hat{B} = \hat{T} \times \hat{N} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -\frac{a}{c} \sin\left(\frac{s}{c}\right) & \frac{a}{c} \cos\left(\frac{s}{c}\right) & \frac{b}{c} \\ -\cos\left(\frac{s}{c}\right) & -\sin\left(\frac{s}{c}\right) & 0 \end{vmatrix}$$

$$\boxed{\hat{B} = \frac{b}{c} \sin\left(\frac{s}{c}\right) \hat{i} - \frac{b}{c} \cos\left(\frac{s}{c}\right) \hat{j} + \frac{a}{c} \hat{k}} \quad [0,2 \text{ pts}]$$

Ahora basta probar que $\hat{T} \cdot \hat{k} = \text{cte}$

$$\hat{T} \cdot \hat{k} = \frac{b}{c}$$

\Rightarrow Las rectas tangentes a C forman un ángulo constante con vector unitario \hat{k} .

$$\boxed{0.3 \text{ pts}]}$$