

1. Coordenadas Cartesianas

1.1. Cantidades cinemáticas

Posición:	$\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$
Velocidad:	$\vec{v} = \dot{x}\hat{i} + \dot{y}\hat{j} + \dot{z}\hat{k}$
Aceleración:	$\vec{a} = \ddot{x}\hat{i} + \ddot{y}\hat{j} + \ddot{z}\hat{k}$

1.2. Elementos diferenciales

Línea:	$d\vec{l} = dx\hat{j} + dy\hat{j} + dz\hat{k}$
Superficie:	$d\vec{S} = dydz\hat{i} + dxdz\hat{j} + dydx\hat{k}$
Volumen:	$dV = dx dy dz$

1.3. Operadores vectoriales

Gradiente:	$\nabla\varphi = \frac{\partial\varphi}{\partial x}\hat{i} + \frac{\partial\varphi}{\partial y}\hat{j} + \frac{\partial\varphi}{\partial z}\hat{k}$
Rotor:	$\nabla \times \vec{F} = \left(\frac{\partial F_z}{\partial y} - \frac{\partial F_y}{\partial z} \right) \hat{i} + \left(\frac{\partial F_x}{\partial z} - \frac{\partial F_z}{\partial x} \right) \hat{j} + \left(\frac{\partial F_y}{\partial x} - \frac{\partial F_x}{\partial y} \right) \hat{k}$
Divergencia:	$\nabla \cdot \vec{F} = \frac{\partial F_x}{\partial x} + \frac{\partial F_y}{\partial y} + \frac{\partial F_z}{\partial z}$
Laplaciano:	$\nabla^2\varphi = \frac{\partial^2\varphi}{\partial x^2} + \frac{\partial^2\varphi}{\partial y^2} + \frac{\partial^2\varphi}{\partial z^2}$

2. Coordenadas Cilíndricas

2.1. Cantidades cinemáticas

Posición:	$\vec{r} = \rho\hat{\rho} + z\hat{k}$
Velocidad:	$\vec{v} = \dot{\rho}\hat{\rho} + \rho\dot{\phi}\hat{\phi} + \dot{z}\hat{k}$
Aceleración:	$\vec{a} = (\ddot{\rho} - \rho\dot{\phi}^2)\hat{\rho} + (2\dot{\rho}\dot{\phi} + \rho\ddot{\phi})\hat{\phi} + \ddot{z}\hat{k}$
Aceleración:	$\vec{a} = (\ddot{\rho} - \rho\dot{\phi}^2)\hat{\rho} + \frac{1}{\rho}\frac{d}{dt}(\rho^2\dot{\phi})\hat{\phi} + \ddot{z}\hat{k}$

2.2. Equivalencias con coordenadas cartesianas

$\hat{\rho} = \cos\phi\hat{i} + \sin\phi\hat{j}$	$\hat{i} = \cos\phi\hat{\rho} - \sin\phi\hat{\phi}$
$\hat{\phi} = -\sin\phi\hat{i} + \cos\phi\hat{j}$	$\hat{j} = \sin\phi\hat{\rho} + \cos\phi\hat{\phi}$

¹SI ENCUENTRAN ALGÚN ERROR O ECUACIÓN QUE VALGA LA PENA PONER, LES PIDO POR FAVOR QUE ME LO INFORMEN.

2.3. Elementos diferenciales

Línea:	$d\vec{l} = d\rho\hat{\rho} + \rho d\phi\hat{\phi} + dz\hat{k}$
Superficie:	$d\vec{S} = \rho d\phi dz\hat{\rho} + d\rho dz\hat{\phi} + \rho d\rho d\phi\hat{k}$
Volumen:	$dV = \rho d\rho d\phi dz$

2.4. Operadores vectoriales

Gradiente:	$\nabla\varphi = \frac{\partial\varphi}{\partial\rho}\hat{\rho} + \frac{1}{\rho}\frac{\partial\varphi}{\partial\phi}\hat{\phi} + \frac{\partial\varphi}{\partial z}\hat{k}$
Rotor:	$\nabla \times \vec{F} = \left[\frac{1}{\rho}\frac{\partial F_z}{\partial\phi} - \frac{\partial F_\phi}{\partial z} \right] \hat{\rho} + \left[\frac{\partial F_\rho}{\partial z} - \frac{\partial F_z}{\partial\rho} \right] \hat{\phi} + \frac{1}{\rho} \left[\frac{\partial(\rho F_\phi)}{\partial\rho} - \frac{\partial F_\rho}{\partial\phi} \right] \hat{k}$
Divergencia:	$\nabla \cdot \vec{F} = \frac{1}{\rho}\frac{\partial(\rho F_\rho)}{\partial\rho} + \frac{1}{\rho}\frac{\partial F_\phi}{\partial\phi} + \frac{\partial F_z}{\partial z}$
Laplaciano:	$\nabla^2\varphi = \frac{1}{\rho}\frac{\partial}{\partial\rho} \left(\rho \frac{\partial\varphi}{\partial\rho} \right) + \frac{1}{\rho^2}\frac{\partial^2\varphi}{\partial\phi^2} + \frac{\partial^2\varphi}{\partial z^2}$

3. Coordenadas Esféricas

3.1. Cantidades cinemáticas

Posición:	$\vec{r} = r\hat{r}$
Velocidad:	$\vec{v} = \dot{r}\hat{r} + r\dot{\theta}\hat{\theta} + r\dot{\phi}\sin\theta\hat{\phi}$
Aceleración:	$\vec{a} = (\ddot{r} - r\dot{\theta}^2 - r\dot{\phi}^2\sin^2\theta)\hat{r} + (r\ddot{\theta} + 2\dot{r}\dot{\theta} - r\dot{\phi}^2\sin\theta\cos\theta)\hat{\theta} + (r\ddot{\phi}\sin\theta + 2\dot{r}\dot{\phi}\sin\theta + 2r\dot{\phi}\dot{\theta}\cos\theta)\hat{\phi}$
Aceleración:	$\vec{a} = (\ddot{r} - r\dot{\theta}^2 - r\dot{\phi}^2\sin^2\theta)\hat{r} + (r\ddot{\theta} + 2\dot{r}\dot{\theta} - r\dot{\phi}^2\sin\theta\cos\theta)\hat{\theta} + \frac{1}{r\sin\theta}\frac{d}{dt}(r^2\dot{\phi}\sin^2\theta)$

3.2. Equivalencias con cartesianas

$\hat{r} = (\cos\phi\hat{i} + \sin\phi\hat{j})\sin\theta + \hat{k}\cos\theta$	$\hat{i} = \sin\theta\cos\phi\hat{r} + \cos\theta\cos\phi\hat{\theta} - \sin\phi\hat{\phi}$
$\hat{\theta} = (\cos\phi\hat{i} + \sin\phi\hat{j})\cos\theta - \hat{k}\sin\theta$	$\hat{j} = \sin\theta\sin\phi\hat{r} + \cos\theta\sin\phi\hat{\theta} + \cos\phi\hat{\phi}$
$\hat{\phi} = -\hat{i}\sin\phi + \hat{j}\cos\phi$	$\hat{k} = \hat{r}\cos\theta - \hat{\theta}\sin\theta$

3.3. Elementos diferenciales

Línea:	$d\vec{l} = dr\hat{r} + rd\theta\hat{\theta} + r\sin\theta d\phi\hat{\phi}$
Superficie:	$d\vec{S} = r^2\sin\theta d\theta d\phi\hat{r} + r\sin\theta dr d\phi\hat{\theta} + rd\theta dr\hat{\phi}$
Volumen:	$dV = r^2\sin\theta dr d\phi d\theta$

3.4. Operadores vectoriales

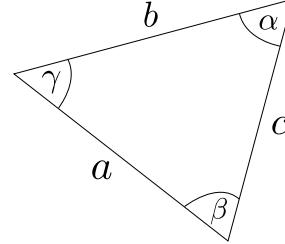
Gradiente: $\nabla\varphi = \frac{\partial\varphi}{\partial r}\hat{r} + \frac{1}{r}\frac{\partial\varphi}{\partial\theta}\hat{\theta} + \frac{1}{r\sin\theta}\frac{\partial\varphi}{\partial\phi}\hat{\phi}$

Rotor: $\nabla \times \vec{F} = \frac{1}{r\sin\theta} \left[\frac{\partial(\sin\theta F_\phi)}{\partial\theta} - \frac{\partial F_\theta}{\partial\phi} \right] \hat{r} + \frac{1}{r} \left[\frac{1}{\sin\theta} \frac{\partial F_r}{\partial\phi} - \frac{\partial(rF_\phi)}{\partial r} \right] \hat{\theta} + \frac{1}{r} \left[\frac{\partial(rF_\theta)}{\partial r} - \frac{\partial F_r}{\partial\theta} \right] \hat{\phi}$

Divergencia: $\nabla \cdot \vec{F} = \frac{1}{r^2} \frac{\partial(r^2 F_r)}{\partial r} + \frac{1}{r\sin\theta} \frac{\partial(\sin\theta F_\theta)}{\partial\theta} + \frac{1}{r\sin\theta} \frac{\partial F_\phi}{\partial\phi}$

Laplaciano: $\nabla^2\varphi = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial\varphi}{\partial r} \right) + \frac{1}{r^2 \sin\theta} \frac{\partial}{\partial\theta} \left(\sin\theta \frac{\partial\varphi}{\partial\theta} \right) + \frac{1}{r^2 \sin^2\theta} \frac{\partial^2\varphi}{\partial\phi^2}$

4. Geometría



Teo. seno: $\frac{\sin\alpha}{a} = \frac{\sin\beta}{b} = \frac{\sin\gamma}{c}$

Teo. coseno: $c^2 = a^2 + b^2 - 2ab\cos\gamma$.

5. Cálculo Vectorial

5.1. Teoremas de cálculo vectorial

Teo. Gauss: $\iint_D \vec{F} \cdot d\vec{S} = \iiint_U (\nabla \cdot \vec{F}) dV$

Teo. Stokes: $\iint_D (\nabla \times \vec{F}) \cdot d\vec{S} = \int_{\partial D} \vec{F} \cdot d\vec{l}$

5.2. Identidades vectoriales útiles

- $\nabla \times (\nabla\varphi) = 0$.
- $\nabla \cdot (\nabla \times \vec{F}) = 0$.
- $\nabla \times (\nabla \times \vec{F}) = \nabla (\nabla \cdot \vec{F}) - \nabla^2 \vec{F}$.
- $\nabla \times (f(r)\hat{r}) = 0$.
- $\nabla \left(\frac{1}{r} \right) = -\frac{\vec{r}}{r^3}$.
- $\nabla^2 \left(\frac{1}{r} \right) = \delta(\vec{r}), r \neq 0$.
- $\vec{a} \times (\vec{b} \times \vec{c}) = \vec{b}(\vec{a} \cdot \vec{c}) - \vec{c}(\vec{a} \cdot \vec{b})$.

6. Ecuaciones de Maxwell

Ley de Gauss: $\nabla \cdot \vec{E} = \frac{\rho}{\varepsilon_0}$

$\nabla \cdot \vec{B} = 0$

Ley de Faraday: $\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$

Ley de Ampère generalizada: $\nabla \times \vec{B} = \mu_0 \vec{J} + \mu_0 \varepsilon_0 \frac{\partial \vec{E}}{\partial t}$
