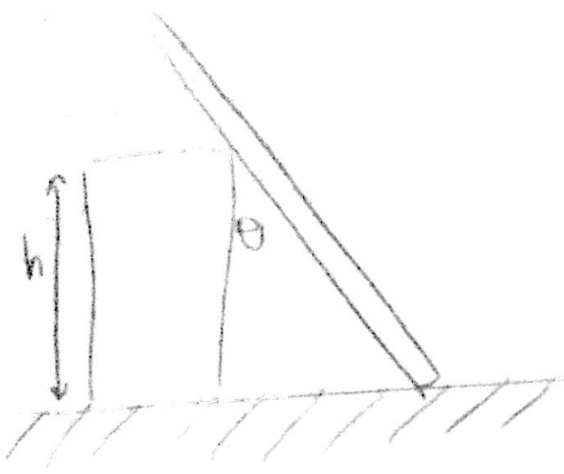
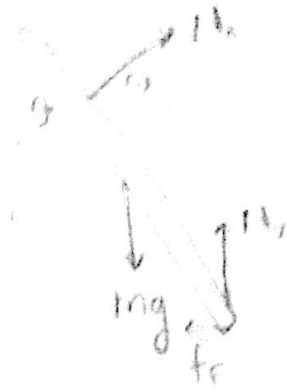




a)



$$\Sigma F_y = N_1 \sin \theta + N_2 - mg = 0 \quad (1)$$

$$\Sigma F_x = -f_r + N_1 \cos \theta = 0 \quad (2)$$

De (2) encontramos N_1

$$N_1 = \frac{f_r}{\sin \theta} = \frac{\mu N_2}{\sin \theta} \quad (3)$$

Reemplazando (3) en (1)

$$\frac{\mu N_2}{\sin \theta} + N_2 - mg = 0.$$

$$N_2 \left(\frac{\mu}{\sin \theta} + 1 \right) = mg$$

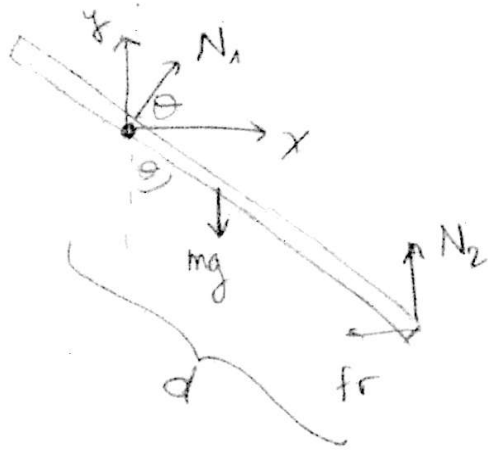
$$N_2 = \frac{mg}{\frac{\mu}{\sin \theta} + 1}$$

De (3) obtenemos entonces

$$N_1 = \left(\frac{\mu mg}{\frac{\mu}{\sin \theta} + 1} \right) \frac{1}{\sin \theta}$$

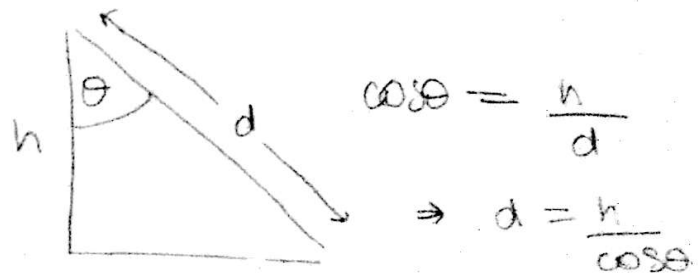
$$\Rightarrow f_r = \frac{\mu mg}{\frac{\mu}{\sin \theta} + 1}$$

b) Para esto usamos la otra condición de estática.
 $\Sigma \vec{\tau} = 0$.



$$\vec{\tau}_{N_1} = 0$$

$$\vec{\tau}_{N_2} = \vec{d} \times \vec{N}_2$$



$$\begin{aligned} \vec{\tau}_{N_2} &= \frac{h}{\cos \theta} (-\cos \theta \hat{y} + \sin \theta \hat{x}) \times N_2 \hat{z} \\ &= \frac{h}{\cos \theta} \sin \theta N_2 \hat{z} \end{aligned}$$

$$\begin{aligned} \vec{\tau}_{fr} &= d(-\cos \theta \hat{y} + \sin \theta \hat{x}) \times fr(-\hat{x}) \\ &= -d \cos \theta - fr \hat{z} = -h fr \hat{z} \end{aligned}$$

$$\Rightarrow \frac{h}{\cos \theta} \sin \theta N_2 + \left(\frac{L}{2} - d\right) \sin \theta mg - h fr = 0$$

$$\left(\frac{L}{2} - d\right) \sin \theta mg = h fr - \frac{h \sin \theta N_2}{\cos \theta}$$

$$\frac{L}{2} - d = \frac{h}{mg \sin \theta} \left(fr - \frac{\sin \theta N_2}{\cos \theta} \right)$$

$$\Rightarrow L = 2 \left(\frac{h}{mg \sin \theta} \left(fr - \frac{\sin \theta N_2}{\cos \theta} \right) + d \right)$$