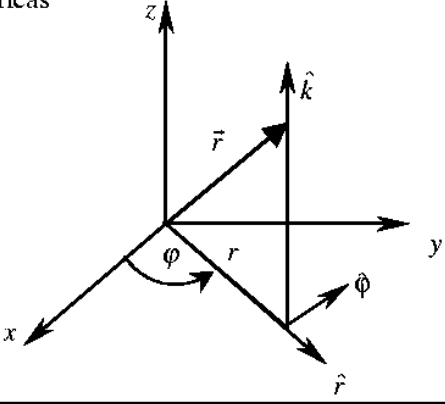
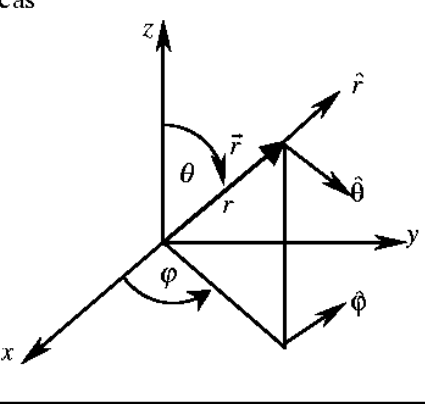


Formulario Matemático de Electromagnetismo

<p>C. Cilíndricas</p>  <p style="margin-top: 20px;"> $\vec{r} = r\hat{r} + z\hat{k}$ $x = r \cos \varphi$ $y = r \sin \varphi$ $z = z$ </p>	<p>C. Esféricas</p>  <p style="margin-top: 20px;"> $\vec{r} = r\hat{r}$ $x = r \sin \theta \cos \varphi$ $y = r \sin \theta \sin \varphi$ $z = r \cos \theta$ </p>
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1. Gradientes

<p>Cartesianas</p> $\nabla \phi = \frac{\partial \phi}{\partial x} \hat{i} + \frac{\partial \phi}{\partial y} \hat{j} + \frac{\partial \phi}{\partial z} \hat{k}$	<p>Cilíndricas</p> $\nabla \phi = \frac{\partial \phi}{\partial r} \hat{r} + \frac{1}{r} \frac{\partial \phi}{\partial \varphi} \hat{\varphi} + \frac{\partial \phi}{\partial z} \hat{k}$	<p>Esféricas</p> $\nabla \phi = \frac{\partial \phi}{\partial r} \hat{r} + \frac{1}{r} \frac{\partial \phi}{\partial \theta} \hat{\theta} + \frac{1}{r \sin \theta} \frac{\partial \phi}{\partial \varphi} \hat{\varphi}$
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2. Divergencias

<p>Cartesianas</p> $\nabla \cdot \vec{A} = \frac{\partial A_x}{\partial x} + \frac{\partial A_y}{\partial y} + \frac{\partial A_z}{\partial z}$	<p>Cilíndricas</p> $\nabla \cdot \vec{A} = \frac{1}{r} \frac{\partial (rA_r)}{\partial r} + \frac{1}{r} \frac{\partial A_\varphi}{\partial \varphi} + \frac{\partial A_z}{\partial z}$
<p>Esféricas</p> $\nabla \cdot \vec{A} = \frac{1}{r^2} \frac{\partial (r^2 A_r)}{\partial r} + \frac{1}{r \sin \theta} \frac{\partial (\sin \theta A_\theta)}{\partial \theta} + \frac{1}{r \sin \theta} \frac{\partial A_\varphi}{\partial \varphi}$	

3. Rotores

<p>Cartesianas</p> $\nabla \times \vec{A} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ A_x & A_y & A_z \end{vmatrix} = \left(\frac{\partial A_z}{\partial y} - \frac{\partial A_y}{\partial z} \right) \hat{i} + \left(\frac{\partial A_x}{\partial z} - \frac{\partial A_z}{\partial x} \right) \hat{j} + \left(\frac{\partial A_y}{\partial x} - \frac{\partial A_x}{\partial y} \right) \hat{k}$
<p>Cilíndricas</p> $\nabla \times \vec{A} = \frac{1}{r} \begin{vmatrix} \hat{r} & r\hat{\varphi} & \hat{k} \\ \frac{\partial}{\partial r} & \frac{\partial}{\partial \varphi} & \frac{\partial}{\partial z} \\ A_r & rA_\varphi & A_z \end{vmatrix} = \left(\frac{1}{r} \frac{\partial A_z}{\partial \varphi} - \frac{\partial A_\varphi}{\partial z} \right) \hat{\varphi} + \left(\frac{\partial A_r}{\partial z} - \frac{\partial A_z}{\partial r} \right) \hat{\varphi} + \frac{1}{r} \left(\frac{\partial (rA_\varphi)}{\partial r} - \frac{\partial A_r}{\partial \varphi} \right) \hat{k}$
<p>Esféricas</p> $\nabla \times \vec{A} = \frac{1}{r^2 \sin \theta} \begin{vmatrix} \hat{r} & r\hat{\theta} & r \sin \theta \hat{\varphi} \\ \frac{\partial}{\partial r} & \frac{\partial}{\partial \theta} & \frac{\partial}{\partial \varphi} \\ A_r & rA_\theta & r \sin \theta A_\varphi \end{vmatrix}$ $\nabla \times \vec{A} = \frac{1}{r \sin \theta} \left(\frac{\partial (A_\varphi \sin \theta)}{\partial \theta} - \frac{\partial A_\theta}{\partial \varphi} \right) \hat{r} + \frac{1}{r} \left(\frac{1}{\sin \theta} \frac{\partial A_r}{\partial \varphi} - \frac{\partial (rA_\varphi)}{\partial r} \right) \hat{\theta} + \frac{1}{r} \left(\frac{\partial (rA_\theta)}{\partial r} - \frac{\partial A_r}{\partial \theta} \right) \hat{\varphi}$

4. Laplacianos

Cartesianas $\nabla^2 \phi = \frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} + \frac{\partial^2 \phi}{\partial z^2}$	Cilíndricas $\nabla^2 \phi = \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial \phi}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 \phi}{\partial \varphi^2} + \frac{\partial^2 \phi}{\partial z^2}$
Esféricas $\nabla^2 \phi = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial \phi}{\partial r} \right) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial \phi}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2 \phi}{\partial \varphi^2}$	

5. Elementos diferenciales

De línea		
Cartesianas $d\vec{l} = dx\hat{i} + dy\hat{j} + dz\hat{k}$	Cilíndricas $d\vec{l} = dr\hat{r} + r d\varphi\hat{\varphi} + dz\hat{k}$	Esféricas $d\vec{l} = dr\hat{r} + r d\theta\hat{\theta} + r \sin \theta d\varphi\hat{\varphi}$
De superficie		
Cartesianas $d\vec{s} = dydz\hat{i} + dx dz\hat{j} + dx dy\hat{k}$	Cilíndricas $d\vec{s} = r d\varphi dz\hat{r} + dr dz\hat{\varphi} + r dr d\varphi\hat{k}$	Esféricas $d\vec{s} = r^2 \sin \theta d\theta d\varphi\hat{r} + r \sin \theta dr d\varphi\hat{\theta} + r d\theta dr\hat{\varphi}$
De volumen		
Cartesianas $dv = dx dy dz$	Cilíndricas $dv = r dr d\varphi dz$	Esféricas $dv = r^2 \sin \theta dr d\varphi d\theta$

donde:

en cartesianas $\vec{A} = A_x \hat{x} + A_y \hat{y} + A_z \hat{z}$

en cilíndricas $\vec{A} = A_r \hat{r} + A_\varphi \hat{\varphi} + A_z \hat{k}$

en esféricas $\vec{A} = A_r \hat{r} + A_\theta \hat{\theta} + A_\varphi \hat{\varphi}$

6. Identidades Vectoriales

$$\nabla \times (\nabla \phi) = 0$$

$$\nabla \cdot (\nabla \times \vec{A}) = 0$$

$$\nabla \times (\nabla \times \vec{A}) = \nabla(\nabla \cdot \vec{A}) - \nabla^2 \vec{A}$$

$$\nabla(\phi \psi) = \phi \nabla \psi + \psi \nabla \phi$$

$$\nabla \cdot (\phi \vec{A}) = \phi \nabla \cdot \vec{A} + \vec{A} \cdot \nabla \phi$$

$$\nabla \cdot (\phi \nabla \psi) = \phi \nabla^2 \psi + \nabla \psi \cdot \nabla \phi$$

$$\nabla \times (f(\vec{r}) \vec{r}) = 0$$

$$\nabla \left(\frac{1}{r} \right) = -\frac{\vec{r}}{r^3} \quad (|\vec{r}| = r)$$

$$\nabla \cdot (\vec{A} \times \vec{B}) = \vec{B} \cdot (\nabla \times \vec{A}) - \vec{A} \cdot (\nabla \times \vec{B})$$

$$\nabla \cdot \vec{r} = 3 \quad \nabla \times \vec{r} = 0$$

$$\nabla(\vec{A} \cdot \vec{r}) = \vec{A}$$

$$\nabla \times (\phi \vec{A}) = \phi (\nabla \times \vec{A}) - \vec{A} \times \nabla \phi$$

$$\nabla(r^n) = nr^{n-2} \vec{r}$$

$$\nabla^2 \left(\frac{1}{r} \right) = -4\pi \delta(\vec{r})$$

$$\nabla^2 \left(\frac{1}{r} \right) = 0 \quad (\text{para } r \neq 0)$$

$$\nabla \times (\vec{A} \times \vec{B}) = (\vec{B} \cdot \nabla) \vec{A} - (\vec{A} \cdot \nabla) \vec{B} + \vec{A} \nabla \cdot \vec{B} - \vec{B} \nabla \cdot \vec{A}$$

$$\nabla(\vec{A} \cdot \vec{B}) = \vec{A} \times (\nabla \times \vec{B}) + \vec{B} \times (\nabla \times \vec{A}) + (\vec{B} \cdot \nabla) \vec{A} + (\vec{A} \cdot \nabla) \vec{B}$$