

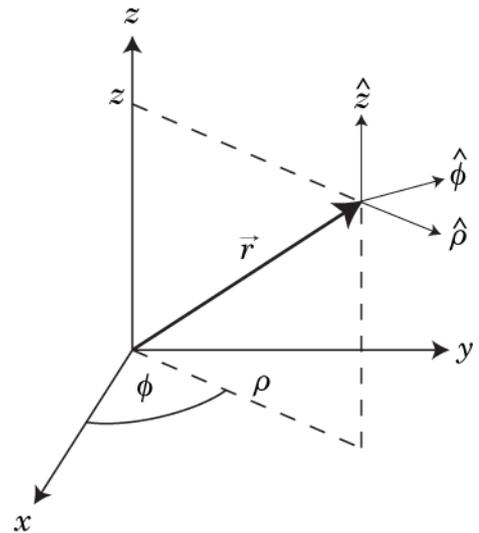
## Coordenadas Cilíndricas

$$\vec{r} = \rho \hat{\rho} + z \hat{z}$$

$$\vec{v} = \dot{\rho} \hat{\rho} + \rho \dot{\phi} \hat{\phi} + \dot{z} \hat{z}$$

$$\vec{a} = (\ddot{\rho} - \rho \dot{\phi}^2) \hat{\rho} + (2\dot{\rho} \dot{\phi} + \rho \ddot{\phi}) \hat{\phi} + \ddot{z} \hat{z}$$

$$\frac{d\hat{\rho}}{dt} = \dot{\phi} \hat{\phi}, \quad \frac{d\hat{\phi}}{dt} = -\dot{\phi} \hat{\rho}$$



## Coordenadas Esféricas

$$\vec{r} = r \hat{r}$$

$$\vec{v} = \dot{r} \hat{r} + r \dot{\theta} \hat{\theta} + r \dot{\phi} \sin(\theta) \hat{\phi}$$

$$\begin{aligned} \vec{a} = & (\ddot{r} - r \dot{\phi}^2 \sin^2(\theta) - r \dot{\theta}^2) \hat{r} \\ & + (r \ddot{\theta} - r \dot{\phi}^2 \sin(\theta) \cos(\theta) + 2\dot{r} \dot{\theta}) \hat{\theta} \\ & + (2\dot{r} \dot{\phi} \sin(\theta) + r \ddot{\phi} \sin(\theta) + 2r \dot{\theta} \dot{\phi} \cos(\theta)) \hat{\phi} \end{aligned}$$

$$\frac{d\hat{r}}{dt} = \dot{\theta} \hat{\theta} + \dot{\phi} \sin(\theta) \hat{\phi}$$

$$\frac{d\hat{\theta}}{dt} = -\dot{\theta} \hat{r} + \dot{\phi} \cos(\theta) \hat{\phi}$$

$$\frac{d\hat{\phi}}{dt} = -\dot{\phi} \sin(\theta) \hat{r} - \dot{\phi} \cos(\theta) \hat{\theta}$$

