Exceptions

Motivation

Most programming languages provide some mechanism for interrupting the normal flow of control in a program to signal some exceptional condition.

Note that it is always *possible* to program without exceptions instead of raising an exception, we return None; instead of returning result x normally, we return Some(x). But now we need to wrap every function application in a case to find out whether it returned a result or an exception.

It is much more convenient to build this mechanism into the language.

Varieties of non-local control

There are many ways of adding "non-local control flow"

- exit(1)
- ► goto
- setjmp/longjmp
- raise/try (or catch/throw) in many variations
- callcc / continuations
- more esoteric variants (cf. many Scheme papers)

Let's begin with the simplest of these.

An "abort" primitive in λ_{\rightarrow}

First step: raising exceptions (but not catching them).

t ::= error	terms run-time error	
Evaluation		
	$\texttt{error} \ \texttt{t}_2 \longrightarrow \texttt{error}$	(E-AppErr1)
	$\mathtt{v}_1 \; \texttt{error} \longrightarrow \texttt{error}$	(E-AppErr2)

What if we had booleans and numbers in the language?

Typing

Typing



Typing errors

Note that the typing rule for error allows us to give it any type T.

```
\Gamma \vdash \text{error} : T (T-ERROR)
```

This means that both

if x>0 then 5 else error

and

if x>0 then true else error

will typecheck.

Aside: Syntax-directedness

Note that this rule

```
\Gamma \vdash \text{error} : T (T-ERROR)
```

has a problem from the point of view of implementation: it is not *syntax directed*.

This will cause the Uniqueness of Types theorem to fail.

For purposes of defining the language and proving its type safety, this is not a problem — Uniqueness of Types is not critical. Let's think a little, though, about how the rule might be fixed...

An alternative

Can't we just decorate the **error** keyword with its intended type, as we have done to fix related problems with other constructs?

 $\Gamma \vdash (\text{error as } T) : T$ (T-Error)

An alternative

Can't we just decorate the **error** keyword with its intended type, as we have done to fix related problems with other constructs?

```
\Gamma \vdash (\text{error as } T) : T (T-Error)
```

No, this doesn't work!

E.g. (assuming our language also has numbers and booleans):

succ (if (error as Bool) then 5 else 7) \longrightarrow succ (error as Bool)

Exercise: Come up with a similar example using just functions and error.

Another alternative

In a system with universal polymorphism (like OCaml), the variability of typing for error can be dealt with by assigning it a variable type!

```
\Gamma \vdash \text{error} : 'a (T-ERROR)
```

In effect, we are replacing the *uniqueness of typing* property by a weaker (but still very useful) property called *most general typing*.

I.e., although a term may have many types, we always have a compact way of *representing* the set of all of its possible types.

Yet another alternative

Alternatively, in a system with subtyping (which we'll discuss in the next lecture) and a minimal Bot type, we *can* give error a unique type:

```
\Gamma \vdash \text{error} : \text{Bot} (T-ERROR)
```

(Of course, what we've really done is just pushed the complexity of the old error rule onto the Bot type! We'll return to this point later.)



Let's stick with the original rule

```
\Gamma \vdash \text{error} : T (T-ERROR)
```

and live with the resulting nondeterminism of the typing relation.

Type safety

The *preservation* theorem requires no changes when we add error: if a term of type T reduces to error, that's fine, since error has every type T.

Type safety

The *preservation* theorem requires no changes when we add error: if a term of type T reduces to error, that's fine, since error has every type T.

Progress, though, requires a litte more care.

Progress

First, note that we do *not* want to extend the set of values to include **error**, since this would make our new rule for propagating errors through applications.

 $v_1 \text{ error} \longrightarrow \text{error}$ (E-APPERR2)

overlap with our existing computation rule for applications:

 $(\lambda x: T_{11}.t_{12}) v_2 \longrightarrow [x \mapsto v_2]t_{12}$ (E-APPABS)

e.g., the term

 $(\lambda x:Nat.0)$ error

could evaluate to either 0 (which would be wrong) or error (which is what we intend).

Progress

Instead, we keep **error** as a non-value normal form, and refine the statement of progress to explicitly mention the possibility that terms may evaluate to **error** instead of to a value.

THEOREM [PROGRESS]: Suppose t is a closed, well-typed normal form. Then either t is a value or t = error.

Catching exceptions

t ::= ... terms try t with t trap errors Evaluation (E-TRYV) try v_1 with $t_2 \longrightarrow v_1$ try error with $t_2 \longrightarrow t_2$ (E-TRYERROR) $t_1 \longrightarrow t'_1$ (E-TRY) try t_1 with $t_2 \longrightarrow try t'_1$ with t_2 Typing $\Gamma \vdash t_1 : T \quad \Gamma \vdash t_2 : T$ (T-TRY) $\Gamma \vdash try t_1$ with $t_2 : T$

Exceptions carrying values

t ::= ... raise t terms raise exception

Evaluation

(E-APPRAISE1) (raise v_{11}) $t_2 \longrightarrow$ raise v_{11} v_1 (raise v_{21}) \longrightarrow raise v_{21} (E-APPRAISE2) $t_1 \longrightarrow t'_1$ (E-RAISE) raise $t_1 \longrightarrow$ raise t'_1 raise (raise v_{11}) \rightarrow raise v_{11} (E-RAISERAISE) (E-TRYV) try v_1 with $t_2 \longrightarrow v_1$ try raise v_{11} with $t_2 \longrightarrow t_2 v_{11}$ (E-TRYRAISE) $t_1 \longrightarrow t'_1$ (E-TRY) try t_1 with $t_2 \longrightarrow try t'_1$ with t_2

Typing

To typecheck raise expressions, we need to choose a type — let's call it T_{exn} — for the values that are carried along with exceptions.

$$\frac{\Gamma \vdash t_1 : T_{exn}}{\Gamma \vdash raise \ t_1 : T}$$
(T-Exn)

$$\frac{\vdash t_1 : T \quad I \vdash t_2 : T_{exn} \to T}{\Gamma \vdash try \ t_1 \ with \ t_2 : T}$$
(T-TRY)

To complete the story, we need to decide what type to use as T_{exn} . There are several possibilities.

1. Numeric error codes: $T_{exn} = Nat$ (as in C)

To complete the story, we need to decide what type to use as T_{exn} . There are several possibilities.

- 1. Numeric error codes: $T_{exn} = Nat$ (as in C)
- 2. Error messages: $T_{exn} = String$

To complete the story, we need to decide what type to use as T_{exn} . There are several possibilities.

- 1. Numeric error codes: $T_{exn} = Nat$ (as in C)
- 2. Error messages: $T_{exn} = String$
- 3. A predefined variant type:

T _{exn}	=	<dividebyzero:< th=""><th>Unit,</th></dividebyzero:<>	Unit,
		overflow:	Unit,
		fileNotFound:	String,
		fileNotReadable:	String,
		>	_

To complete the story, we need to decide what type to use as T_{exn} . There are several possibilities.

- 1. Numeric error codes: $T_{exn} = Nat$ (as in C)
- 2. Error messages: $T_{exn} = String$
- 3. A predefined variant type:

T _{exn}	=	<dividebyzero:< th=""><th>Unit,</th></dividebyzero:<>	Unit,
		overflow:	Unit,
		fileNotFound:	String,
		fileNotReadable:	String,
		>	

4. An extensible variant type (as in OCaml)

To complete the story, we need to decide what type to use as T_{exn} . There are several possibilities.

- 1. Numeric error codes: $T_{exn} = Nat$ (as in C)
- 2. Error messages: $T_{exn} = String$
- 3. A predefined variant type:

Γ _{exn}	=	<dividebyzero:< th=""><th>Unit,</th></dividebyzero:<>	Unit,
		overflow:	Unit,
		fileNotFound:	String,
		fileNotReadable:	String,
		>	

- 4. An extensible variant type (as in OCaml)
- 5. A class of "throwable objects" (as in Java)