

Evaluation strategies

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more readably: $id\ (id\ (\lambda z.id\ z))$

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three redexes:

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full beta-reduction (one possibility):

$$\begin{aligned} & id \ (id \ (\lambda z.\underline{id \ z})) \\ \rightarrow & id \ (id \ (\lambda z.z)) \\ \rightarrow & \frac{id \ (\lambda z.z)}{} \\ \rightarrow & \lambda z.z \end{aligned}$$

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normal order:

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call by name:

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call by value:

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