

# Comparison of European bearing capacity calculation methods for shallow foundations

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■ The aim of this paper is to compare the methods used by the European countries to evaluate the bearing capacity of shallow foundations. Comparisons of several formulations of bearing capacity factors, depth and shape factors, load inclination and eccentricity factors, as well as values of these factors, are presented. This study has deliberately been restricted to methods using the bearing capacity factors  $N_c$ ,  $N_q$  and  $N_\gamma$ ; other methods exist and are used, but few of them are in common use in all European countries (for example, the pressiometric method is used almost exclusively in France), and consequently the comparison would be awkward. The most important conclusion is that the evaluated bearing capacity depends highly on the country. Therefore, bearing capacity needs to be better understood using new parametric and numerical analyses.

**Keywords:** codes of practice and standards; European Union (EU); foundations

## Notation

|       |                              |
|-------|------------------------------|
| $A$   | foundation surface area      |
| $a$   | base adhesion of the footing |
| $B$   | foundation width             |
| $B'$  | reduced width                |
| $c$   | soil cohesion                |
| $c_u$ | undrained soil cohesion      |
| $e$   | load eccentricity            |

|                      |   |
|----------------------|---|
| $i_\gamma, i_c, i_q$ | load inclination factors  |
| $L$                  | foundation length   |
| $N_\gamma, N_c, N_q$ | bearing capacity factors  |
| $\bar{q}$            | surcharge per unit area   |
| $q_u$                | ultimate bearing capacity                                       |
| $s_\gamma, s_c, s_q$ | shape factors   |
| $V_u$                | ultimate vertical load  |
| $w$                  | foundation vertical displacement                                |
| $\gamma$             | unit weight   |
| $\delta$             | load inclination  |
| $\theta$             | load inclination including adhesion between soil and foundation |
| $\phi$               | angle of internal friction                                      |

## Introduction

This work was carried out with the support of members of the European Action COST C7 'Soil-Structure Interaction in Urban Civil Engineering'. Countries which are not directly mentioned in the current paper have not sent information concerning the standards used. The information transmitted by Belgium could not easily be integrated into this analysis. At the end, we have information concerning 17 countries, some countries using foreign regulations or standards. The 12 countries directly concerned with this comparative analysis are listed in Table 1: we note that only four countries have a standard and two have regulations.

## Generalities

2. The basic formulation concerns strip footings loaded vertically in the plane of

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Table 1. Standard, regulation or practice

| Countries            | Standard, regulation or practice  |
|----------------------|---|
| Austria (A)          | ÖNORM B 4432 <sup>1</sup>   |
| Czech Republic (CZ)  | Czech Standard 731001   |
| Germany (D)          | DIN V 4017-100 <sup>2</sup>   |
| France (F)           | DTU 13.12 <sup>3</sup>  |
| Finland (FIN)        | Design practice   |
| Greece (G)           | German standard or US regulation  |
| Ireland (IRL)        | (UK) design practice <sup>4</sup>   |
| Norway (N)           | Design practice: Danish Brinch Hansen values or Janbu's procedure (only Hansen's method will be considered here for Norway) |
| Portugal (P)         | Design practice: Terzaghi, Meyerhof, Hansen, or Vesic's values  |
| United Kingdom (UK)* | Standard for Foundations BS 8004  |
| Sweden (S)           | Design practice   |
| Slovenia (SLO)†      | Serbian regulation, UL SFRJ 15/90 <sup>5</sup>  |

\*Many British designers also use Eurocode 7 and the associated British NAD.

†Slovenia uses the regulation established before the splitting of ex-Yugoslavia.

symmetry (Fig. 1). One of the first formulations of this problem was given by Terzaghi<sup>6</sup> as

$$q_u = 0.5B\gamma N_\gamma + \bar{q}N_q + cN_c \quad (1)$$

in which  $q_u$  is the ultimate bearing pressure,  $\gamma$  is the unit weight of the soil under the foundation,  $B$  is the foundation width,  $N_\gamma$  is the bearing capacity factor concerning a cohesionless soil (internal friction angle  $\phi$ ),  $N_q$  is the bearing capacity factor concerning the embedment  $D$ , and  $N_c$  is the bearing capacity factor concerning the cohesion  $c$ .

3. Three countries use another form for equation (1). Germany and Austria incorporate the coefficient 0.5 in  $N_b$ :

$$q_u = B\gamma N_b + \bar{q}N_q + cN_c \quad (2)$$

Slovenia uses explicitly only two bearing capacity factors:

$$q_u = 0.5B\gamma N_\gamma + \bar{q} + (c + \bar{q} \tan \phi)N_c \quad (3)$$

4. For more complicated cases (rectangular footing, eccentric load, etc.), each bearing capacity factor is multiplied by correction factors

- (a) the shape factor for a rectangular footing
- (b) the eccentricity correction factor for an eccentric load
- (c) the inclination factor for an inclined load.

### Bearing capacity factors

5. Only the case of a strip footing loaded by a vertically centred force will be considered in this section.

#### Classical formulae

6. Most of the presented formulations are summarized by Bowles<sup>7</sup> (Table 2).

#### Methods used by each country

7. The methods used by each country are listed in Table 3. Some countries provide

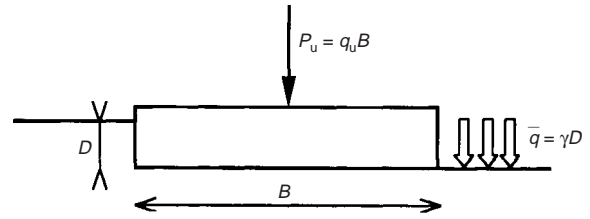


Fig. 1. Basic diagram

information on the bearing capacity factors using analytical formulae, and others with curves or tables.

#### Specific formulations

8. A few countries use specific values.

9. *Germany and Austria.* Germany and Austria include the coefficient 0.5 in the factor  $N_b$  and use specific formulations as indicated above. To allow a comparison between the full values, the factor  $N_\gamma$ —which has the same formulation as in the German edition of Eurocode 7—will be used instead of factor  $N_b$ , as follows.

10. For both countries

$$N_\gamma = 2N_b \quad (4)$$

with

$$N_b = (N_q - 1) \tan \phi \quad (5)$$

in Germany and  $N_b$  given in tables and curves in Austria.

11. *France.* France uses Giroud's values for  $N_\gamma$  (given in a table).

12. *Sweden.* The formulation used by Sweden is similar to Hansen's:

$$N_\gamma = F(\phi) \left[ \tan^2 \left( \frac{\pi}{4} + \frac{\phi}{2} \right) \exp(1.5\pi \tan \phi) - 1 \right] \quad (6)$$

in which

$$F(\phi) = 0.08705 + 0.3231 \sin 2\phi - 0.04836 \sin^2 2\phi$$

13. *Slovenia.* It was explained previously

Table 2. Classical formulae of bearing capacity factors

| Author                   | $N_\gamma$   | $N_c$                 | $N_q$   |
|--------------------------|--|-----------------------|---|
| Terzaghi <sup>6</sup>    | $\frac{\tan \phi}{2} \left( \frac{K_{p\gamma}}{\cos^2 \phi} - 1 \right)$<br>$K_{p\gamma}$ is given in tables | $(N_q - 1) \cot \phi$ | $\frac{a^2}{2 \cos^2[(\pi/4) + (\phi/2)]}$<br>with $a = \exp \left[ \left( \frac{3\pi}{4} - \frac{\phi}{2} \right) \tan \phi \right]$ |
| Meyerhof <sup>8</sup>    | $(N_q - 1) \tan(1.4\phi)$  | $(N_q - 1) \cot \phi$ | $\tan^2 \left( \frac{\pi}{4} + \frac{\phi}{2} \right) \exp(\pi \tan \phi)$  |
| Hansen <sup>9</sup>      | $1.5(N_q - 1) \tan \phi$   | $(N_q - 1) \cot \phi$ | $\tan^2 \left( \frac{\pi}{4} + \frac{\phi}{2} \right) \exp(\pi \tan \phi)$  |
| Vesic <sup>10,11</sup>   | $2(N_q + 1) \tan \phi$   | $(N_q - 1) \cot \phi$ | $\tan^2 \left( \frac{\pi}{4} + \frac{\phi}{2} \right) \exp(\pi \tan \phi)$  |
| Eurocode 7 <sup>12</sup> | $2(N_q - 1) \tan \phi$   | $(N_q - 1) \cot \phi$ | $\tan^2 \left( \frac{\pi}{4} + \frac{\phi}{2} \right) \exp(\pi \tan \phi)$  |

Table 3. Methods used to estimate the bearing capacity factors

| Countries           | $N_q$                | $N_c$                | $N_\gamma$                              | Formulae | Curves         | Tables |
|---------------------|----------------------|----------------------|---|----------|----------------|--------|
| Austria (A)         | Specific             | Specific             | Specific                                | No       | Yes            | Yes    |
| Czech Republic (CZ) | Meyerhof             | Meyerhof             | Hansen                                  | Yes      | Yes            | No     |
| Germany (D)         | Meyerhof             | Meyerhof             | E7                                      | Yes      | Yes            | Yes    |
| France (F)          | Meyerhof             | Meyerhof             | Giroud <sup>13</sup>                    | No       | No             | Yes    |
| Finland (FIN)       | Meyerhof             | Meyerhof             | Hansen                                  | Yes      | –              | –      |
| Ireland (IRL)       | Meyerhof             | Meyerhof             | Hansen                                  | No       | Yes            | No     |
| Norway (N)          | Meyerhof             | Meyerhof             | Hansen                                  | No       | No             | No     |
| Portugal (P)        | Terzaghi<br>Meyerhof | Terzaghi<br>Meyerhof | Terzaghi<br>Meyerhof<br>Hansen<br>Vesic | Yes      | Yes            | Yes    |
| Sweden (S)          | Meyerhof             | Meyerhof             | Specific                                | Yes      | No             | No     |
| Slovenia (SLO)      | –                    | Meyerhof             | E7                                      | No       | $N_c-N_\gamma$ | No     |
| Eurocode 7          | Meyerhof             | Meyerhof             | Specific                                | Yes      | No             | No     |

that Slovenia uses explicitly only two bearing capacity factors. After transformation of equation (3) into the classical form, we obtain

$$N_q = 1 + N_c \tan \phi \quad (7)$$

or also

$$N_c = (N_q - 1) \cot \phi \quad (8)$$

which is clearly Terzaghi's formulation.

#### Comparison of results

14.  $N_q$  and  $N_c$  values are shown in Fig. 2(a). Note that Austria uses bearing capacity factors which are systematically lower than the ones used by the other countries. The largest values are given by Terzaghi.

15. Concerning  $N_\gamma$  (Fig. 2(b)), the values given by the Eurocode are near those used by France. Values issued from the Eurocode are located between Hansen's and the Austrian values, which are the highest.

#### Eccentricity correction

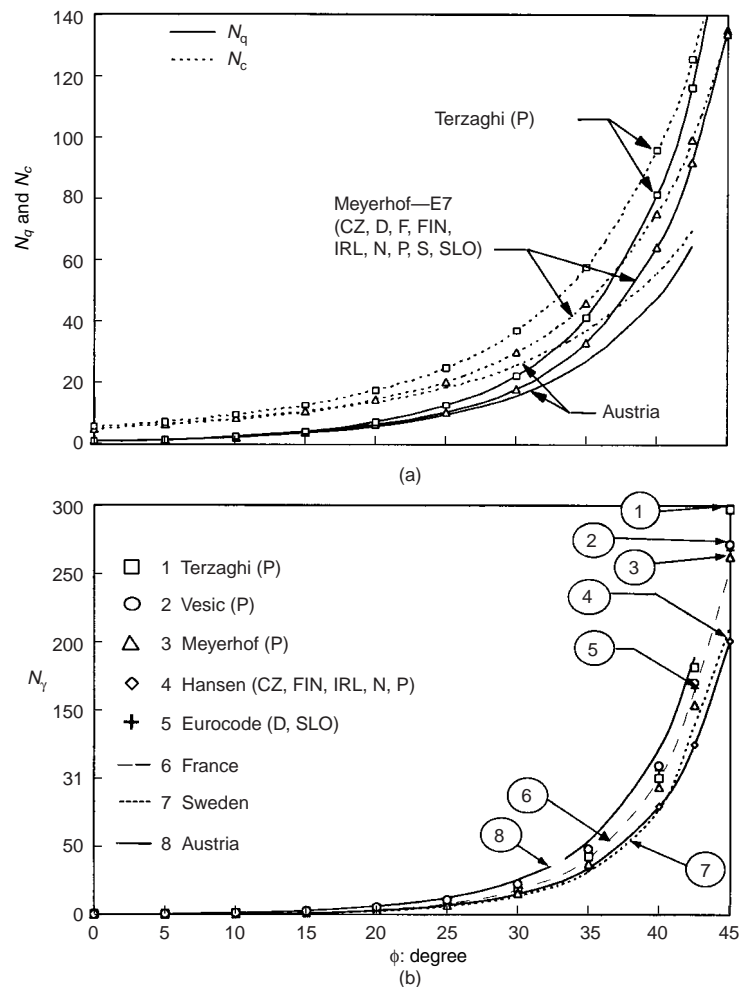
16. All countries use the method proposed by Meyerhof, which consists of replacing the footing by an effective footing with width  $B'$  centred on the external load (Fig. 3), where  $B'$  is given by

$$B' = B - 2e \quad (9)$$

where  $e$  is the eccentricity of the load measured from the symmetry plane of the footing.

17. For a rectangular footing, a double eccentricity in the direction of the width and in the direction of the length can exist: in this case, the footing is replaced by a footing with a

Fig. 2. Bearing capacity factors plotted against  $\phi$ :  
(a)  $N_q$  and  $N_c$ ; (b)  $N_\gamma$



double reduced dimension according to equation (9), taking into account the eccentricity in both directions.

### Shape factors

18. The bearing capacity factors presented above are defined in the case of a strip footing. To take into account the non-infinite length of a rectangular footing, a shape factor  $s_i$  is introduced for each bearing capacity factor:

$$q_u = 0.5B\gamma N_\gamma s_\gamma + \bar{q}N_q s_q + cN_c s_c \quad (10)$$

The footing has width  $B$  and length  $L$ , and we assume that  $B \leq L$ .

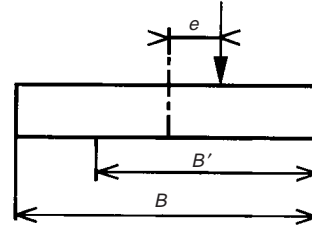


Fig. 3. Effective width

### Shape factors according to the authors

19. The shape factors used by the mentioned authors are listed in Table 4. Terzaghi's results given for a square footing can be extended to a rectangular footing by a linear function of  $B/L$ . We can also see that  $s_\gamma \leq 1$  for

Table 4. Shape factors according to the authors

| Authors   | $s_q$  | $s_c$   | $s_\gamma$   |
|---|--|---|--|
| Terzaghi (square)   | 1  | 1.2   | 0.8  |
| Meyerhof<br>$K_p = \tan^2\left[\frac{\pi}{4} + \frac{\phi}{2}\right]$ | $1 + 0.1K_p \frac{B}{L} \quad \phi > 10^\circ$<br>$1 \quad \phi = 0$ | $1 + 0.2K_p \frac{B}{L}$  | $1 + 0.1K_p \frac{B}{L} \quad \phi > 10^\circ$<br>$1 \quad \phi = 0$ |
| Hansen  | $1 + \frac{B}{L} \sin \phi$  | $1 + \frac{N_q B}{N_c L} \quad \phi \neq 0$<br>$1 + 0.2 \frac{B}{L} \quad \phi = 0$ | $1 - 0.4 \frac{B}{L} \geq 0.6$                                       |
| Vesic   | $1 + \frac{B}{L} \tan \phi$  | $1 + \frac{N_q B}{N_c L}$   | $1 - 0.4 \frac{B}{L} \geq 0.6$                                       |

Table 5. Shape factors according to the countries

| Countries           | $s_q$   | $s_c (\phi \neq 0)$           | $s_c (\phi = 0)$      | $s_\gamma$            |
|---------------------|---|-------------------------------|-----------------------|-----------------------|
| Austria (A)         | $1 + \frac{B}{L} \sin \phi$                       | $\frac{s_q N_q - 1}{N_q - 1}$ | $1 + 0.2 \frac{B}{L}$ | $1 - 0.3 \frac{B}{L}$ |
| Czech Republic (CZ) | $1 + \frac{B}{L} \sin \phi$                       | $1 + 0.2 \frac{B}{L}$         | $1 + 0.2 \frac{B}{L}$ | $1 - 0.3 \frac{B}{L}$ |
| Germany (D)         | $1 + \frac{B}{L} \sin \phi$                       | $\frac{s_q N_q - 1}{N_q - 1}$ | $1 + 0.2 \frac{B}{L}$ | $1 - 0.3 \frac{B}{L}$ |
| France (F)          | 1   | $1 + 0.2 \frac{B}{L}$         | $1 + 0.2 \frac{B}{L}$ | $1 - 0.2 \frac{B}{L}$ |
| Finland (FIN)       | $1 + 0.2 \frac{B}{L}$                             | $1 + 0.2 \frac{B}{L}$         | $1 + 0.2 \frac{B}{L}$ | $1 - 0.4 \frac{B}{L}$ |
| Ireland (IRL)       | $1 + 0.2 \frac{B}{L}$                             | $1 + 0.2 \frac{B}{L}$         | $1 + 0.2 \frac{B}{L}$ | $1 - 0.4 \frac{B}{L}$ |
| Norway (N)          | $1 + \frac{B}{L} \sin \phi$                       | $1 + \frac{N_q B}{N_c L}$     | $1 + 0.2 \frac{B}{L}$ | $1 - 0.4 \frac{B}{L}$ |
| Sweden (S)          | $1 + \frac{B}{L} \tan \phi$                       | $1 + \frac{N_q B}{N_c L}$     | $1 + 0.2 \frac{B}{L}$ | $1 - 0.4 \frac{B}{L}$ |
| Slovenia (SLO)      | $\frac{1 + s_c N_c \tan \phi}{1 + N_c \tan \phi}$ | $1 + 0.2 \frac{B}{L}$         | $1 + 0.2 \frac{B}{L}$ | $1 - 0.4 \frac{B}{L}$ |
| Eurocode 7          | $1 + \frac{B}{L} \sin \phi$                       | $\frac{s_q N_q - 1}{N_q - 1}$ | $1 + 0.2 \frac{B}{L}$ | $1 - 0.3 \frac{B}{L}$ |

all authors except Meyerhof. On the other hand, other forms are usual for the factor  $s_c$ . If we introduce into the formulation given in Table 4 equation (7) between  $N_c$  and  $N_q$  and Vesic's factor  $s_q$ , we obtain

$$s_c = 1 + \frac{N_q B}{N_c L} = 1 + \frac{N_q(s_q - 1)}{N_q - 1} = \frac{N_q s_q - 1}{N_q - 1} \quad (11)$$

#### Shape factors according to the countries

20. The shape factors used by the mentioned countries are listed in Table 5. A comparison of the Tables 4 and 5 shows which author's formulations are effectively used by each country.

21. Only the shape factor  $s_c$  corresponding to a soil without internal friction is used by all countries. For some countries, the other factors depend only on the size of the footing, and for other countries, also on the internal friction.

22. Slovenia uses a specific equation (equation (12)) according to the specific bearing equation (equation (3)), so only two factors ( $S_c$  and  $S_\gamma$ ) appear explicitly:

$$q_u = 0.5B\gamma N_\gamma S_\gamma + \bar{q} + (c + \bar{q} \tan \phi) N_c S_c \quad (12)$$

After comparison with equation (11) and the introduction of equation (7), one obtains

$$s_\gamma = S_\gamma \quad (13)$$

$$s_q = \frac{1 + s_c N_c \tan \phi}{1 + N_c \tan \phi}$$

$$s_c = S_c$$

The numerical results are given in Fig. 4. These results show great variation from one country to another. Germany and Austria use the same formulation to evaluate the shape factor  $s_c$  ( $\phi \neq 0$ ), but the values of the bearing capacity  $N_q$  are different. Nevertheless, the numerical values obtained for  $s_c$  by both countries remain very close.

23. Meyerhof's method is the least used. We see also that a lot of countries use a different method for each factor: for example, the Czech Republic calculates  $s_q$  with Hansen, and  $s_c$  with Terzaghi, and has a specific method for determining  $s_\gamma$ .

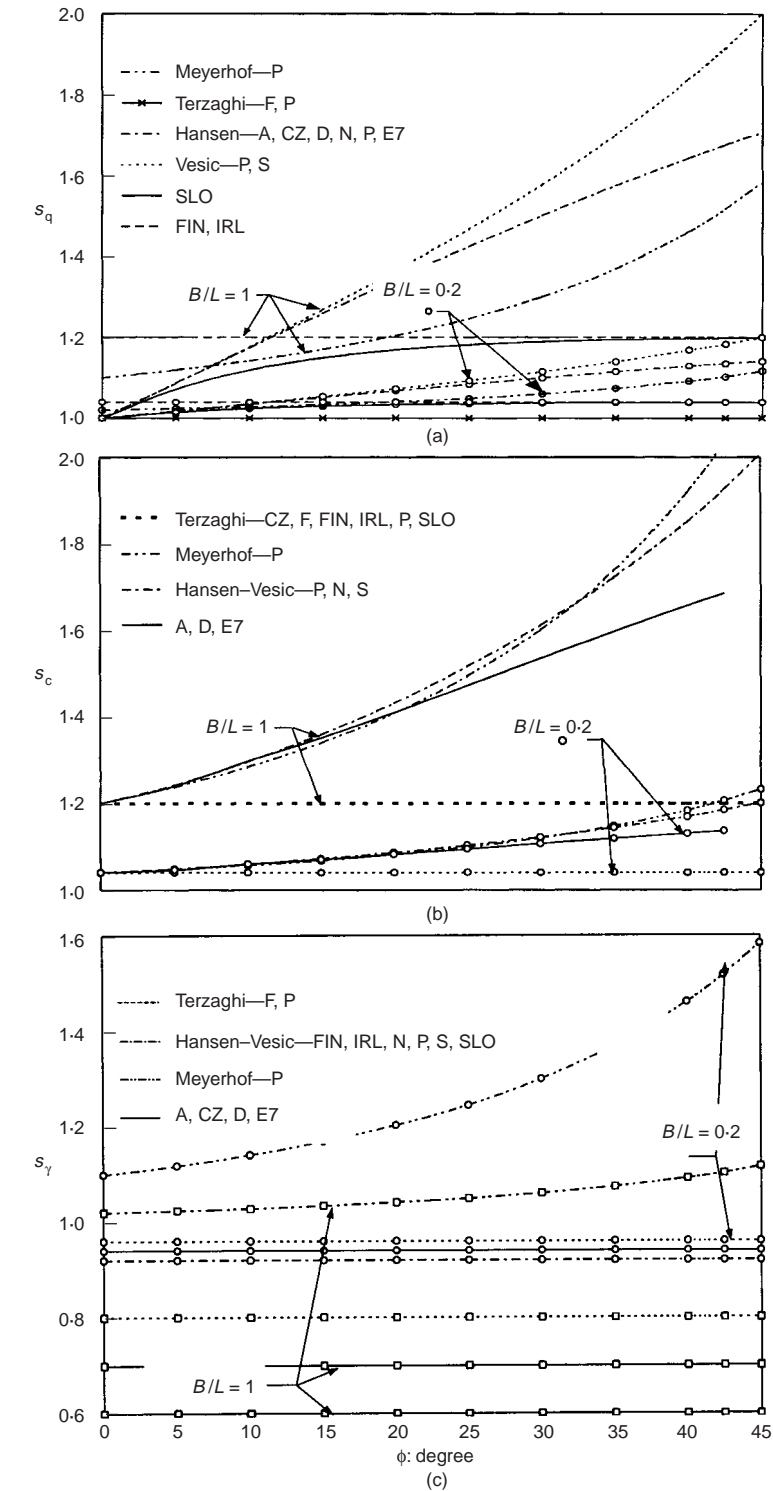
#### Inclination factors

24. The bearing capacity factors presented above are defined for a vertical load. To take into account the inclination of the load, an inclination factor  $i_i$  is introduced in each bearing capacity factor:

$$q_u = 0.5B\gamma N_\gamma i_\gamma + \bar{q} N_q i_q + c N_c i_c \quad (14)$$

#### Parameters

25. Two parameters can be defined to characterize the inclination of the load. The external force has a vertical component  $V$  and a horizontal component  $H$  (Fig. 6). Therefore, the



inclination is naturally introduced as a parameter using the angle  $\delta$  defined as follows:

$$\tan \delta = \frac{H}{V} \quad (15)$$

Fig. 4. Shape factor plotted against  $\phi$  and  $B/L$ : (a)  $s_q$ ; (b)  $s_c$ ; (c)  $s_\gamma$

26. Another possibility consists of introducing the adhesion  $a$  between the soil and the base of the footing. However, this adhesion must be smaller than (or equal to) the cohesion  $c$  of the soil, and depends on the roughness of

the footing. Consequently, a second form to describe the inclination of the load consists of introducing an angle  $\theta$  defined by

$$\tan \theta = \frac{H}{V + Aa \cot \phi} \quad (16)$$

in which  $A$  is the effective soil–footing contact area.

27.  $\delta$  and  $\theta$  are equal for a cohesionless soil ( $c = 0$ ) or for a perfectly smooth footing. This last case is not realistic in practice.

28. The classical formulations are listed in Table 6.

29. The Eurocode assumes that the adhesion  $a$  is equal to the cohesion  $c$  of the soil.

30. It can be seen that Vesic also introduces the shape of the footing into the inclination factor.

31. Hansen published at the same time tables and curves, but he did not specify the values of  $\alpha_1$  and  $\alpha_2$  corresponding to these curves. After analysis of his curves, one obtains the following values:

$$\alpha_1 \approx 4.8 \quad (17a)$$

$$\alpha_2 \approx 5.5 \quad (17b)$$

We will use these values later, although the second one is out of the range given by Hansen himself.

#### Formulations

32. The formulations used by the mentioned countries are listed in Table 7. Some countries directly use Meyerhof's, Hansen's or Vesic's formulations, and others introduce different coefficients or exponents.

33. Results given by Austria include directly the inclination factors in the bearing capacity factors: these can be calculated by division by the values obtained without inclination.

34. Slovenia also proposes a specific formulation according to the bearing capacity equation (equation (3)) and explicitly uses only two factors ( $I_c$  and  $I_\gamma$ ):

$$q_u = 0.5\gamma B N_\gamma I_\gamma + \bar{q} + (c + \bar{q} \tan \phi) N_c I_c \quad (18)$$

After comparison with equation (10) and introduction of equation (7), one obtains

$$i_\gamma = I_\gamma \quad (19a)$$

$$i_q = \frac{1 + (N_q - 1)i_c}{N_q} \quad (19b)$$

$$i_c = I_c = \frac{N_q i_q - 1}{N_q - 1} \quad (19c)$$

#### Comparison of results

35. We will have to separate comparisons for the methods using  $\delta$  and those using  $\theta$ . It does not make sense to compare both methods within a general case. But in order to simplify the presentation of the results, the curves in

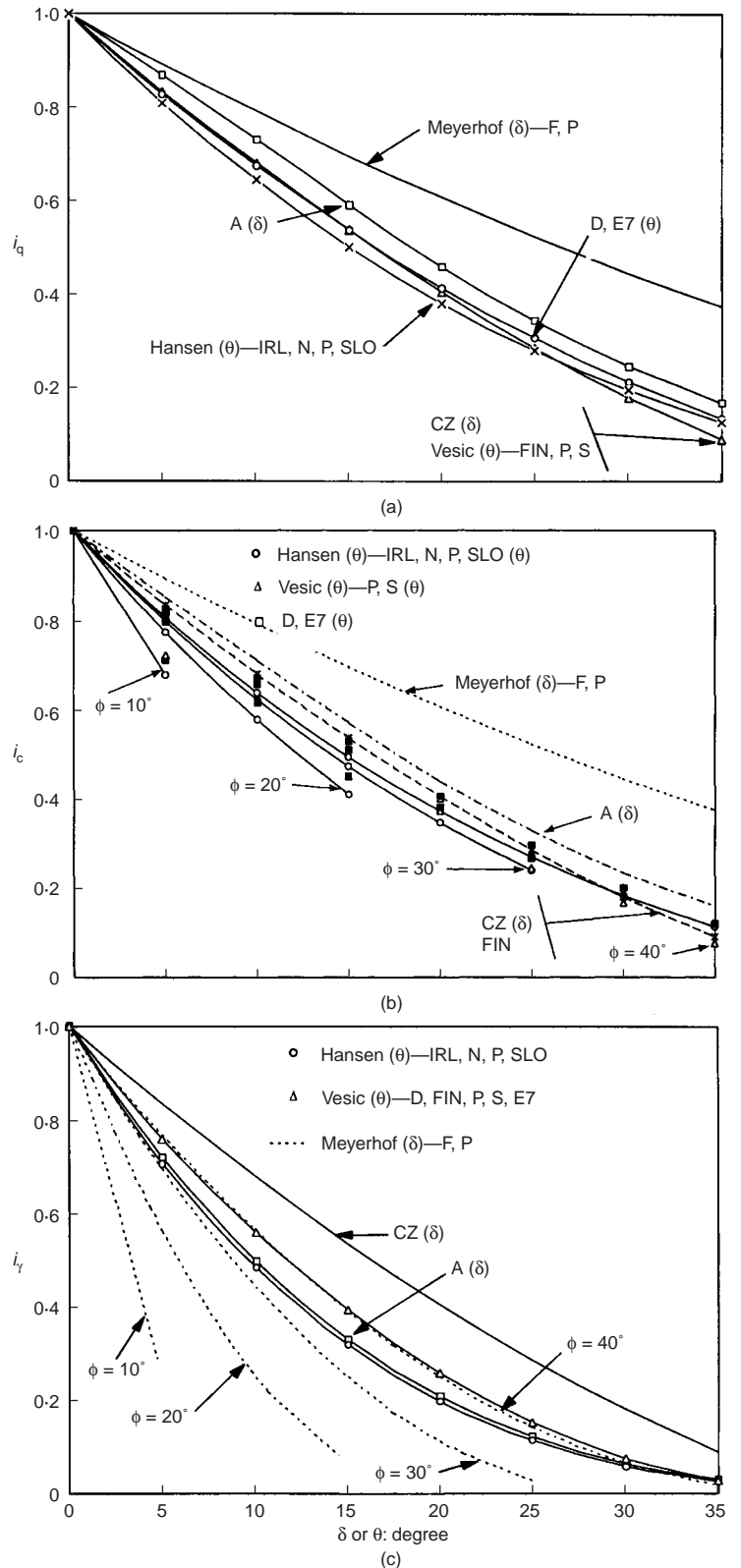


Fig. 5 show the values obtained with both methods (for Vesic's analysis, the presented results concern only a strip footing).

36. Comparison of results for methods using  $\delta$ . The calculated results of the three factors concerning Austria are not significantly depen-

Fig. 5. Inclination factor plotted against  $\delta$ ,  $\theta$  and  $\phi$ : (a)  $i_q$  against  $\delta$  and  $\theta$ ; (b)  $i_c$  against  $\delta$ ,  $\theta$  and  $\phi$ ; (c)  $i_\gamma$  against  $\delta$ ,  $\theta$  and  $\phi$

Table 6. Classical formulations for inclination factors

| Authors    | $i_q$                                    | $i_c (\phi \neq 0)$                      | $i_c (\phi = 0)$  | $i_\gamma$                               | Comments   |
|------------|--|--|---|--|--|
| Meyerhof   | $\left(1 - \frac{2\delta}{\pi}\right)^2$ | $\left(1 - \frac{2\delta}{\pi}\right)^2$ | $\left(1 - \frac{2\delta}{\pi}\right)^2$                        | $\left(1 - \frac{\delta}{\phi}\right)^2$ | –  |
| Hansen     | $(1 - 0.5 \tan \theta)^{\alpha_1}$       | $\frac{i_q N_q - 1}{N_q - 1}$            | $0.5 - \sqrt{\left(1 - \frac{H}{Aa}\right)}$                    | $(1 - 0.7 \tan \theta)^{\alpha_2}$       | $2 \leq \alpha_1 \leq 5$<br>$2 \leq \alpha_2 \leq 5$ |
| Vesic      | $(1 - \tan \theta)^m$                    | $\frac{i_q N_q - 1}{N_q - 1}$            | $1 - \frac{mH}{AaN_c}$  | $(1 - \tan \theta)^{m+1}$                | $m = \frac{2 + B/L}{1 + B/L}$                        |
| Eurocode 7 | $1 - \frac{H}{V + Ac' \cot \phi'}$       | $\frac{i_q N_q - 1}{N_q - 1}$            | $0.5 \left[ 1 + \sqrt{\left(1 - \frac{H}{Ac_u}\right)} \right]$ | $1 - \frac{H}{V + Ac' \cot \phi'}$       | –  |

Table 7. Inclination factors

| Countries                   | $i_q$                     | $i_c (\phi \neq 0)$   | $i_c (\phi = 0)$                                 | $i_\gamma$                 |
|-----------------------------|---------------------------|-----------------------|--|----------------------------|
| Austria ( $\delta$ )        | Integrated into $N_q$     | Integrated into $N_c$ | Integrated into $N_c$                            | Integrated into $N_\gamma$ |
| Czech Republic ( $\delta$ ) | $(1 - \tan \delta)^2$     | $(1 - \tan \delta)^2$ | $(1 - \tan \delta)^2$                            | $(1 - \tan \delta)^2$      |
| Germany ( $\theta$ )        | $(1 - 0.7 \tan \theta)^3$ | Hansen and Vesic      | $0.5 + 0.5 \sqrt{\left(1 - \frac{H}{Aa}\right)}$ | Vesic<br>$m = 2$           |
| France ( $\delta$ )         | Meyerhof                  | Meyerhof              | Meyerhof   | Meyerhof                   |
| Finland ( $\theta$ )        | Vesic<br>$m = 2$          | $(1 - \tan \theta)^2$ | Vesic<br>$m = 2$                                 | Vesic<br>$m = 2$           |
| Ireland ( $\theta$ )        | Hansen                    | Hansen                | Hansen   | Hansen                     |
| Norway ( $\theta$ )         | Hansen                    | Hansen                | Hansen   | Hansen                     |
| Sweden ( $\theta$ )         | Vesic                     | Vesic                 | Vesic  | Vesic                      |
| Slovenia ( $\theta$ )       | –                         | Hansen                | Hansen   | Hansen                     |
| Eurocode 7 ( $\theta$ )     | $(1 - 0.7 \tan \theta)^3$ | Hansen                | $0.5 + 0.5 \sqrt{\left(1 - \frac{H}{Aa}\right)}$ | $(1 - \tan \theta)^3$      |

dent on the value of  $\phi$ , so it seems reasonable to consider these factors as being non-dependent on the internal friction angle of the soil.

37. It appears also that the differences between the results obtained by Austria and the Czech Republic are not very important for  $i_q$  and  $i_c$ . In general, the results given by Meyerhof and used by France are significantly different from those used by Austria and the Czech Republic, except for  $i_\gamma$  with  $\phi = 40^\circ$ , which is near to the values used by Austria.

38. *Comparison of results for methods using  $\theta$ .* It can be seen that the results used by the mentioned countries are very close, and that the differences between the methods using  $\theta$  are more limited than those obtained with the methods using  $\delta$ .

39. *General comparison.* For all authors and countries,  $i_q$  is non-dependent on  $\phi$ . At the same time, Hansen, Vesic and Eurocode 7 consider that  $i_c$  is dependent on  $\phi$ , and Meyerhof

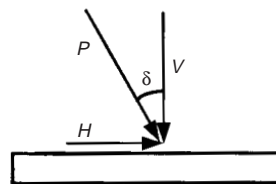


Fig. 6. Inclined load

considers that this factor is not dependent on  $\phi$ . In contrast, all authors and countries except Meyerhof use a factor  $i_\gamma$  not dependent on  $\phi$ .

40. In the particular case of a cohesionless soil,  $\delta$  and  $\theta$  are equal. The comparison is limited to  $i_q$  and  $i_\gamma$ , because the factor  $i_c$  is not directly relevant to cohesionless soil. Concerning  $i_q$ , the results obtained by all countries except France using Meyerhof's formulation are similar. Concerning  $i_\gamma$ , all countries obtain similar results (but only for  $\phi = 40^\circ$  for France), except for the Czech Republic, which uses larger coefficients than the other countries.



### Examples

41. To clarify the differences obtained with all these methods, two examples will illustrate the application of the bearing capacity factors and correction factors discussed previously.

#### Example 1

42. The first example concerns a shallow foundation for which bearing capacity tests were performed on the centrifuge of the University of Bochum. The characteristics of soil and footing (prototype) are listed in Table 8.

43. *Numerical bearing capacity.* Values of the more important factors are listed in Table 9. This example illustrates the large difference between the results. Only Meyerhof considers a shape factor  $s_\gamma$  larger than 1, so his result can be considered as a specific case. Concerning the other authors and countries, the bearing capacity varies from 160 to 321 kN (ratio 1:2). Using the smallest bearing capacity factors, it is easy to see that Sweden obtains the smallest bearing capacity load.

44. *Comparison with experimental bearing capacity.* Load tests were performed on the centrifuge of the University of Bochum. The load–displacement curve presented in Fig. 7 could be analysed in terms of failure criterion with three different methods: (a) load corresponding to a ratio displacement  $d \leq 10\%$ ; (b) load determined using Hansen's failure criterion; and (c) load obtained by linear regression of the end of the load–displacement curve.

45. In the first method,  $d = w/B$ , where  $w$  is the vertical displacement of the footing. In the second method, the loading is considered as the failure loading when the load corresponding to half the displacement is very close to this loading (difference less than 10%), as shown in Fig. 8. With the third method, we obtain an initial value and the slope of the end of the load–displacement curve. The initial value found is used as the ultimate load in the initial experimental conditions of the tests.

46. Table 10 shows the results obtained for four tests. For each method, the error does not exceed 6%; this attests to the quality of the tests. This example also proves that the bearing capacity value depends on the method used: the mean value for each method fluctuates from 307 to 423 kN (ratio 1:1.4).

47. In comparison with the numerical bearing capacity values which are in the range 160–443 kN (321 kN when excluding the Meyerhof results), it is clear that the experimental values are systematically larger than the numerical values. The third method gives results which are closer to the numerical analysis, because the calculation takes into account only the initial conditions, as the third analysis does. From this point of view, the

Table 8. Soil and footing characteristics

| Soil     | $\phi$ : degree | $c$ : kPa | $\gamma$ : kN/m <sup>3</sup> | Footing | $B$ : m | Embedment, $D/B$ |
|----------|-----------------|-----------|------------------------------|---------|---------|------------------|
| Dry sand | 35              | 0         | 17.0                         | Square  | 1       | 0                |

Table 9. Factors and bearing capacity

| Authors and countries | $N_\gamma$ | $s_\gamma$ | $V_u$ : kN |
|-----------------------|------------|------------|------------|
| Terzaghi              | 42.4       | 0.8        | 288        |
| Meyerhof              | 37.2       | 1.4        | 443        |
| Hansen                | 33.9       | 0.6        | 173        |
| Vesic                 | 48.0       | 0.6        | 245        |
| Sweden                | 31.4       | 0.6        | 160        |
| Finland               | 33.9       | 0.6        | 173        |
| Ireland               | 33.9       | 0.6        | 173        |
| Norway                | 33.9       | 0.6        | 173        |
| Czech Republic        | 33.9       | 0.7        | 202        |
| Slovenia              | 45.2       | 0.6        | 245        |
| Germany               | 45.2       | 0.7        | 269        |
| France                | 41.1       | 0.8        | 279        |
| Austria               | 54.0       | 0.7        | 321        |
| Eurocode 7            | 45.2       | 0.7        | 269        |

Fig. 7. Load–displacement curve

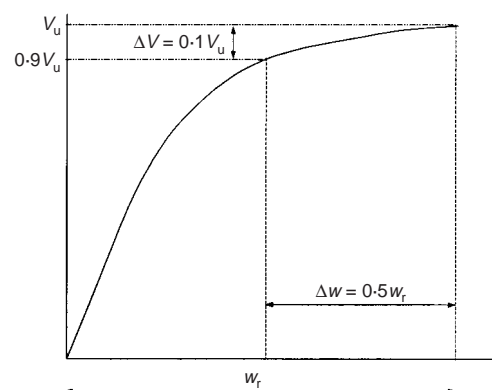
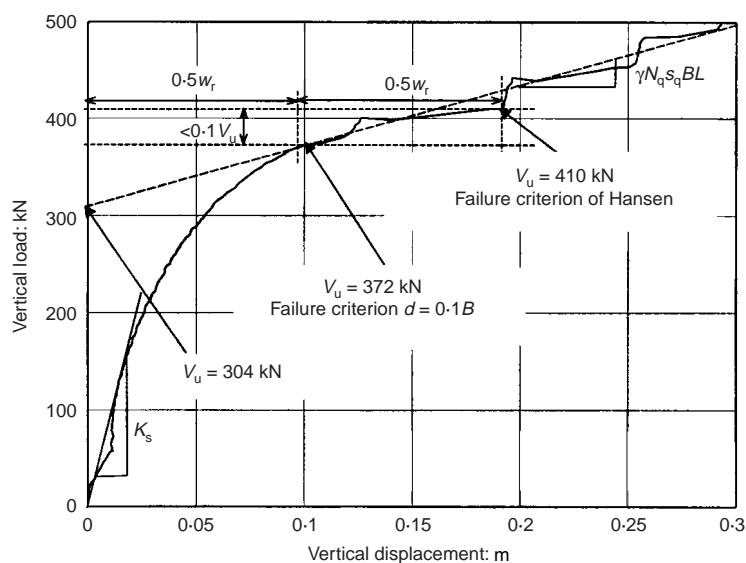


Fig. 8. Hansen's failure criterion



Table 10. Experimental ultimate load with several interpretation methods for the failure criterion

| Test | Ultimate vertical loading: kN |                          |                   |
|------|-------------------------------|--------------------------|-------------------|
|      | $d \leq 10\%$                 | Hansen failure criterion | Linear regression |
| 2    | 384                           | 440                      | 302               |
| 19   | 372                           | 410                      | 304               |
| 25   | 384                           | 428                      | 310               |
| 31   | 384                           | 414                      | 314               |

Table 11. Soil and footing characteristics

| Soil             | $\phi$ : degree | $c$ : kPa | $\gamma$ : kN/m <sup>3</sup> | Footing | $B$ : m | Embedment, $D/B$ | Load inclination: degree |
|------------------|-----------------|-----------|------------------------------|---------|---------|------------------|--------------------------|
| Unsaturated sand | 35              | 10        | 19.0                         | Square  | 1       | 0.6              | $\delta = 10$            |

Table 12. Values of bearing capacity factors

| Authors and countries | $N_\gamma$ | $s_\gamma$ | $i_\gamma$ | $N_q$ | $s_q$ | $i_q$ | $N_c$ | $s_c$ | $i_c$ |
|-----------------------|------------|------------|------------|-------|-------|-------|-------|-------|-------|
| Meyerhof              | 37.2       | 1.4        | 0.51       | 33.3  | 1.37  | 0.79  | 46.1  | 1.74  | 0.79  |
| Hansen                | 33.9       | 0.6        | 0.48       | 33.3  | 1.57  | 0.64  | 46.1  | 1.73  | 0.63  |
| Vesic                 | 48         | 0.6        | 0.56       | 33.3  | 1.7   | 0.68  | 46.1  | 1.72  | 0.67  |
| Ireland               | 33.9       | 0.6        | 0.48       | 33.3  | 1.2   | 0.64  | 46.1  | 1.2   | 0.63  |
| Slovenia              | 45.2       | 0.6        | 0.48       | 33.3  | 1.19  | 0.64  | 46.1  | 1.2   | 0.63  |
| Finland               | 33.9       | 0.6        | 0.56       | 33.3  | 1.2   | 0.68  | 46.1  | 1.2   | 0.68  |
| Austria               | 27.8       | 0.7        | —          | 19.5  | 1.57  | —     | 26.5  | 1.6   | —     |
| France                | 41.1       | 0.8        | 0.51       | 33.3  | 1     | 0.79  | 46.1  | 1.2   | 0.79  |
| Czech Republic        | 33.9       | 0.7        | 0.68       | 33.3  | 1.57  | 0.68  | 46.1  | 1.2   | 0.68  |
| Norway                | 33.9       | 0.6        | 0.48       | 33.3  | 1.57  | 0.64  | 46.1  | 1.72  | 0.63  |
| Germany               | 45.2       | 0.7        | 0.56       | 33.3  | 1.57  | 0.67  | 46.1  | 1.59  | 0.66  |
| Sweden                | 31.4       | 0.6        | 0.62       | 33.3  | 1.7   | 0.68  | 46.1  | 1.72  | 0.67  |
| Eurocode 7            | 45.2       | 0.7        | 0.56       | 33.3  | 1.57  | 0.67  | 46.1  | 1.59  | 0.66  |

Austrian method provides results closer to the experimental values.

#### Example 2

48. The second example concerns the same shallow foundation but embedded in a frictional soil with cohesion and loaded by an inclined load. The characteristics of soil and footing and load are listed in Table 11. It is assumed that  $\tan \delta$  and  $\tan \theta$  are not significantly different.

49. Values of the more important factors are shown in Table 12, and the bearing capacities in Fig. 9.

50. This example shows the large differences between the results: the bearing capacity fluctuates from 734 to 1297 kN (ratio 1:1.8). Concerning the mentioned countries, we conclude that the largest values for the ultimate load are obtained by Sweden and Germany

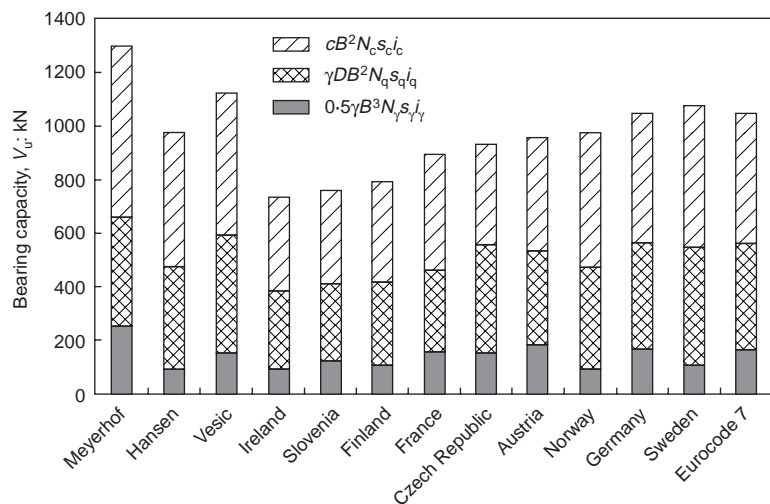


Fig. 9. Bearing capacities

(Eurocode 7), and the smallest by Ireland, Slovenia and Finland.

### Conclusion

51. The most important conclusion is that the evaluated bearing capacity depends highly on the method used, and therefore on the country. Only the eccentricity correction is accepted unanimously: however, this does not mean that this correction is more accurate. The previous illustrations show that the results obtained by a country are not systematically the smallest or the largest. Sweden obtains the smallest bearing capacity value in example 1 (Table 8) and the largest in example 2 (Fig. 9). Although Meyerhof largely overestimates bearing capacity values in both examples, we can conclude that the results calculated with Eurocode 7 stay in the high mean of results found from the European methods used here.

52. Thus, bearing capacity needs to be better understood using new parametric and numerical analyses. Another question is the definition and the experimental or numerical determination of the bearing capacity of a shallow foundation in relation to its displacement.

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