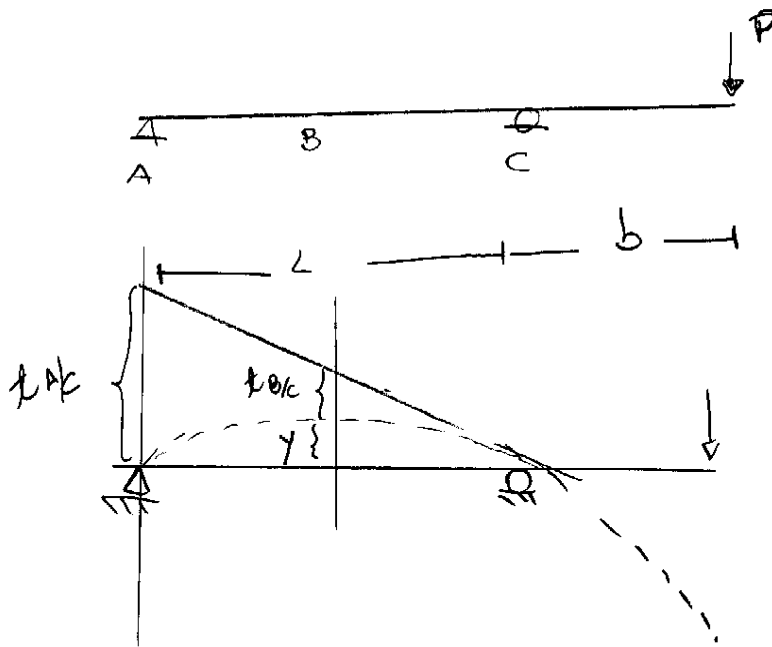


①



$$R_A + R_C = P$$

$$R_C = \frac{P(L+b)}{L}$$

$$R_A = -\frac{Pb}{L}$$

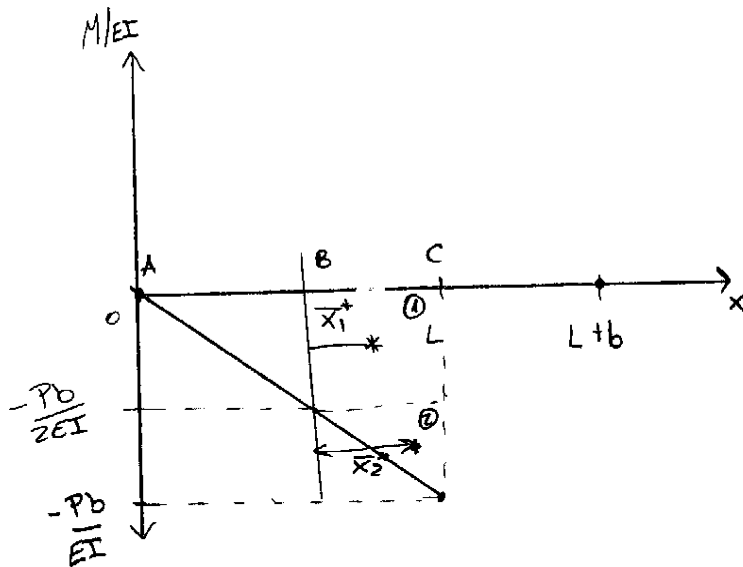
$$\frac{\Delta_{A/C}}{L} = \frac{y + \Delta_{B/C}}{L/2}$$

$$\boxed{\frac{\Delta_{A/C} - \Delta_{B/C}}{2} = y}$$

Cortando:

$$\Rightarrow M = -R_A \cdot x = -\frac{Pb}{L}x$$

R_A (Al poner la flecha hacia abajo queda +)



$$\Delta_{A/C} = \text{Area} \cdot \bar{x}$$

$$= -\frac{Pb}{EI} \cdot \frac{L}{2} \cdot \frac{2L}{3}$$

$$= -\frac{PbL^2}{3EI}$$

$$\Delta_{B/C} = \text{Area}_{BC} \cdot \bar{x}_{BC}$$

$$= \text{Area}_{BC} \cdot \frac{\sum A_i \cdot \bar{x}_i^*}{\sum A_i}$$

$$= \sum A_i \cdot \frac{\sum A_i \bar{x}_i^*}{\sum A_i}$$

$$\Delta_{B/C} = \sum A_i \cdot \bar{x}_i$$

$$\Delta_{B/C} = \underbrace{A_1}_{\frac{PbL}{2}} \cdot \underbrace{\bar{x}_1^*}_{\frac{L}{4}} + \underbrace{A_2}_{-\frac{PbL}{2}} \cdot \underbrace{\bar{x}_2^*}_{\frac{2L}{3}}$$

$$= \frac{PbL^2}{16EI} - \frac{PbL^2}{24EI} = -\frac{5PbL^2}{48EI}$$

$$\Rightarrow \boxed{y = -\frac{1}{16} \frac{PbL^2}{EI}}$$

$$\Delta_{A/C} = \int_0^L -\frac{Pbx^2}{EI} dx = -\frac{PbL^2}{3EI}$$

(2)

$$\Delta_{B/C} = \int_{L/2}^L -\frac{Pbx}{EI} \left(x - \frac{L}{2}\right) dx = \int_{L/2}^L -\frac{Pb}{EI} \left\{x^2 - \frac{xL}{2}\right\} dx$$

$$= -\frac{Pb}{EI} \left\{ \frac{x^3}{3} - \frac{x^2 L}{2} \right\} \Big|_{L/2}^L = -\frac{Pb}{EI} \left\{ \frac{L^3}{3} - \frac{L^3}{4} - \frac{L^3}{24} + \frac{L^3}{16} \right\}$$

$$\Rightarrow \Delta_{B/C} = -\frac{5PbL^2}{48EI}$$

$$\Rightarrow \boxed{y = -\frac{1PbL^2}{16EI}}$$

$$\therefore \Delta_{B/C} = \int_{B}^C \frac{M}{EI} (x - B) dx$$

Para tomar tramos que comienzan fuera de $x=0$ se debe desplazar el x de la integral.