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▼ PAUTA Tarea 2

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▼ Inicialización

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> restart;  
> with(DEtools):  
> with(plots):  
> with(linalg):  
> with(PDEtools):  
>
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▼ P1 i

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> p1 := diff(y(t), t$6) + 72·diff(y(t), t$2) - 1720·y(t) = 0;  

$$p1 := \frac{d^6}{dt^6} y(t) + 72 \left( \frac{d^2}{dt^2} y(t) \right) - 1720 y(t) = 0 \quad (3.1)$$

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> solu1 := rhs(dsolve(p1, y(t)))  

$$\begin{aligned} solu1 := & _C1 e^{\sqrt{10} t} + _C2 e^{-\sqrt{10} t} \\ & + _C3 e^{-\frac{1}{2} \sqrt{-10 + 4\sqrt{43}} t} \sin\left(\frac{1}{2} \sqrt{10 + 4\sqrt{43}} t\right) \end{aligned} \quad (3.2)$$

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$$- _C4 e^{\frac{1}{2} \sqrt{-10 + 4\sqrt{43}} t} \sin\left(\frac{1}{2} \sqrt{10 + 4\sqrt{43}} t\right)$$

$$+ _C5 e^{-\frac{1}{2} \sqrt{-10 + 4\sqrt{43}} t} \cos\left(\frac{1}{2} \sqrt{10 + 4\sqrt{43}} t\right)$$

$$+ _C6 e^{\frac{1}{2} \sqrt{-10 + 4\sqrt{43}} t} \cos\left(\frac{1}{2} \sqrt{10 + 4\sqrt{43}} t\right)$$

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> evalf(solu1);  

$$\begin{aligned} & _C1 e^{3.162277660 t} + _C2 e^{-3.162277660 t} \\ & + _C3 e^{-2.014308448 t} \sin(3.009557862 t) - 1. _C4 e^{2.014308448 t} \sin(3.009557862 t) \\ & + _C5 e^{-2.014308448 t} \cos(3.009557862 t) + _C6 e^{2.014308448 t} \cos(3.009557862 t) \end{aligned} \quad (3.3)$$

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P1 ii

$$\begin{aligned} > p2 := & \text{diff}(y(t), t\$3) - 15 \cdot \text{diff}(y(t), t\$2) - 33 \cdot \text{diff}(y(t), t) + 847 \cdot y(t) = 0; \\ & p2 := \frac{d^3}{dt^3} y(t) - 15 \left(\frac{d^2}{dt^2} y(t) \right) - 33 \left(\frac{d}{dt} y(t) \right) + 847 y(t) = 0 \end{aligned} \quad (4.1)$$

$$\begin{aligned} > solu2 := & \text{rhs}(\text{dsolve}(p2, y(t))) \\ & solu2 := _C1 e^{-7t} + _C2 e^{11t} + _C3 e^{11t} t \end{aligned} \quad (4.2)$$

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P2 i

$$\begin{aligned} > p3 := & \text{diff}(y(t), t\$2) = 10 \cdot \text{diff}(y(t), t) - 25 \cdot y(t); \\ & p3 := \frac{d^2}{dt^2} y(t) = 10 \left(\frac{d}{dt} y(t) \right) - 25 y(t) \end{aligned} \quad (5.1)$$

$$\begin{aligned} > solu1 := & \text{rhs}(\text{dsolve}(p3, y(t))) \\ & solu1 := _C1 e^{5t} + _C2 e^{5t} t \end{aligned} \quad (5.2)$$

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P2 ii

$$\begin{aligned} > p4 := & \text{diff}(y(t), t\$3) + 3 \cdot \text{diff}(y(t), t\$2) - 4 \cdot \text{diff}(y(t), t) - 12 \cdot y(t) = 0; \\ & p4 := \frac{d^3}{dt^3} y(t) + 3 \left(\frac{d^2}{dt^2} y(t) \right) - 4 \left(\frac{d}{dt} y(t) \right) - 12 y(t) = 0 \end{aligned} \quad (6.1)$$

$$\begin{aligned} > solu1 := & \text{rhs}(\text{dsolve}(p4, y(t))) \\ & solu1 := _C1 e^{-2t} + _C2 e^{-3t} + _C3 e^{2t} \end{aligned} \quad (6.2)$$

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P2 iii

$$\begin{aligned} > p5 := & \text{diff}(y(t), t\$4) - 2 \cdot \text{diff}(y(t), t\$2) + y(t) = 0; \\ & p5 := \frac{d^4}{dt^4} y(t) - 2 \left(\frac{d^2}{dt^2} y(t) \right) + y(t) = 0 \end{aligned} \quad (7.1)$$

$$\begin{aligned} > solu1 := & \text{rhs}(\text{dsolve}(p5, y(t))) \\ & solu1 := _C1 e^t + _C2 e^t t + _C3 e^{-t} + _C4 e^{-t} t \end{aligned} \quad (7.2)$$

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▼ P2 iv

$$\begin{aligned} > p6 &:= 2 \cdot \text{diff}(y(t), t\$5) - 7 \cdot \text{diff}(y(t), t\$4) + 12 \cdot \text{diff}(y(t), t\$3) + 8 \cdot \text{diff}(y(t), t\$2) = 0; \\ &p6 := 2 \left(\frac{\text{d}^5}{\text{d}t^5} y(t) \right) - 7 \left(\frac{\text{d}^4}{\text{d}t^4} y(t) \right) + 12 \left(\frac{\text{d}^3}{\text{d}t^3} y(t) \right) + 8 \left(\frac{\text{d}^2}{\text{d}t^2} y(t) \right) = 0 \end{aligned} \quad (8.1)$$

$$\begin{aligned} > solu1 &:= \text{rhs}(\text{dsolve}(p6, y(t))) \\ &solu1 := _C1 + _C2 t + _C3 e^{-\frac{1}{2}t} + _C4 e^{2t} \sin(2t) + _C5 e^{2t} \cos(2t) \end{aligned} \quad (8.2)$$