

B) Se observa que  $B = B^T = \begin{bmatrix} 2 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 2 \end{bmatrix}$

$\Rightarrow B$  es simétrico  $\Rightarrow B$  es diagonalizable.

$$\det(A - \lambda I) = \det \begin{vmatrix} 2-\lambda & 0 & 0 & 0 \\ 0 & 1-\lambda & 1 & 0 \\ 0 & 1 & 1-\lambda & 0 \\ 0 & 0 & 0 & 2-\lambda \end{vmatrix} = \cancel{(2-\lambda)^2 (2-\lambda)^2}$$

$$= (2-\lambda) [(1-\lambda)^2 (2-\lambda) - (2-\lambda)] = (2-\lambda)^2 [(1-\lambda)^2 - 1]$$

$$\Rightarrow \lambda_1 = 2 \quad \text{mult alg} = 3.$$

$$\lambda_2 = 0 \quad \text{mult alg} = 1.$$

$$\underline{\lambda_1 = 2}$$

$$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & -1 & 1 & 0 \\ 0 & 1 & -1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \begin{pmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

$$\rightarrow \begin{aligned} 0 &= 0 \\ v_2 &= v_3 \\ v_2 &= v_3 \\ 0 &= 0 \end{aligned}$$