

Pauta Problema 1 CTP1

(Parte b)

$$E[\pi] = E[p_{t+1}]E[A_{t+1}]K_{t+1}^\alpha \left(\frac{E[p_{t+1}]E[A_{t+1}]K_{t+1}^{\alpha-1}\beta}{\exp(w_0 + \sigma_w^2/2)} \right) - E[w_{t+1}] \left(\frac{(E[p_{t+1}]E[A_{t+1}](\beta)K_{t+1}^\alpha)^{1/\beta}}{E[p_{t+1}]E[A_{t+1}]} \right) - rK_{t+1}$$

al derivar con respecto a K_{t+1} nos queda:

$$\frac{(p_0 A_0)^2 2\alpha K_{t+1}^{2\alpha-1}\beta}{\exp(w_0 + \sigma_w^2/2)} - \left(\frac{\alpha \exp(w_0 + \sigma_w^2/2)}{\beta} \right) \left(\frac{A_0 p_0 (\beta)}{\exp(w_0 + \sigma_w^2/2)} \right)^{1/\beta} (K_{t+1}^{(\alpha/\beta)-1}) = r$$

(Parte c)

Como $1/\beta = 1/(1 - \beta)$ entonces $\alpha/(1 - \beta) = (\alpha/\beta) - 1$

así el capital que se obtiene es: $K^* = \left(\left(\frac{(p_0 A_0)^2 2\alpha\beta}{\exp(w_0 + \sigma_w^2/2)} - \frac{(\alpha)\exp(w_0 + \sigma_w^2/2)}{\beta} \right) \left(\frac{(p_0 A_0)\beta}{\exp(w_0 + \sigma_w^2/2)} \right)^{1/\beta} (1/r) \right)^{-1/C_0}$