

P4

$$x(t) = A \cos(\omega t - \phi_0)$$

Cond Ini:  $x(0) = x_0$  (1)

$$\dot{x}(0) = v_0$$
 (2)

$$(1) \Rightarrow A \cos \phi_0 = x_0$$
 (3)

$$\dot{x}(t) = -A\omega \sin(\omega t - \phi_0)$$

$$(2) \Rightarrow +A\omega \sin \phi_0 = v_0$$
 (4)

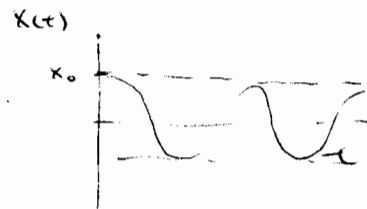
$$(4)/(3) \Rightarrow \omega \tan \phi_0 = \frac{v_0}{x_0}$$

$$\Rightarrow \boxed{\tan \phi_0 = \frac{v_0}{\omega x_0}}$$

$$(3)^2 + ((4)/\omega)^2 \Rightarrow A^2 = x_0^2 + \left(\frac{v_0}{\omega}\right)^2$$

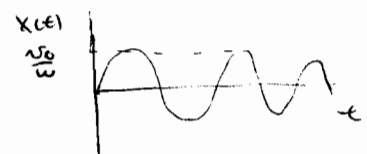
$$\therefore x(t) = \sqrt{x_0^2 + \left(\frac{v_0}{\omega}\right)^2} \cos\left(\omega t - \tan^{-1}\left(\frac{v_0}{\omega x_0}\right)\right)$$

• Si  $v_0 = 0 \Rightarrow x(t) = x_0 \cos(\omega t)$

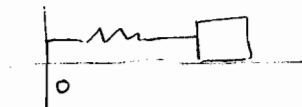


• Si  $x_0 = 0 \Rightarrow x(t) = \frac{v_0}{\omega} \cos(\omega t - \pi/2)$

$$= \frac{v_0}{\omega} \sin(\omega t)$$



P2  $\ddot{x} + \omega^2 x + b = 0$



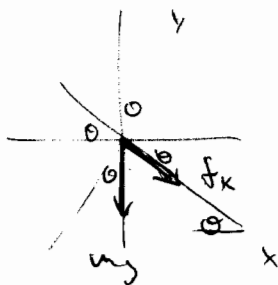
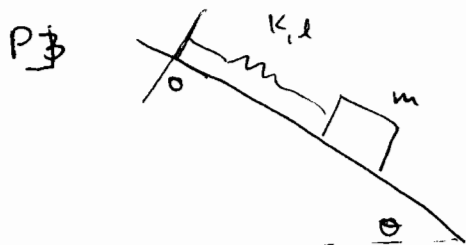
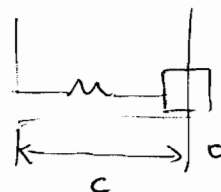
$x(t) = z(t) + c$   $c$  por determinar

$\Rightarrow \ddot{z} + \omega^2 (z + c) + b = 0$

$\Rightarrow \ddot{z} + \omega^2 z + \underbrace{\omega^2 c + b}_{=0 \text{ (se impone)}} = 0$

$\Rightarrow \ddot{z} + \omega^2 z = 0$

con  $c = -\frac{b}{\omega^2}$



x)  $\underbrace{f_K + mg \sin \theta}_{-K(x-l_0)} = m \ddot{x}$

$\Rightarrow m \ddot{x} + K(x-l_0) - mg \sin \theta = 0$

$\ddot{x} + \frac{K}{m} x + \underbrace{-g \sin \theta - \frac{K}{m} l_0}_b = 0 \quad (1)$

caso variable  $\ddot{z} = \ddot{x} - g \sin \theta - \frac{K}{m} l_0$   
 $\Rightarrow \ddot{z} + \omega_0^2 z = 0 \quad \omega_0 = \sqrt{\frac{K}{m}}$

$$\ddot{x} + \omega x + b = 0 \quad \omega = \sqrt{\frac{k}{m}}$$

$$b = -(g \sin \theta + \frac{k}{m} l_0)$$

change variable  $z = x + \frac{b}{\omega^2}$

$$z = x + \left( g \sin \theta + \frac{k}{m} l_0 \right) \frac{m}{k}$$

$$z = x + \left( \frac{mg \sin \theta}{k} + l_0 \right)$$

$$\Rightarrow \ddot{z} + \omega^2 z = 0$$

$$\Rightarrow z(t) = A \cos(\omega t + \phi)$$

$$\Rightarrow \boxed{x(t) = A \cos(\omega t + \phi) + l_0 + \frac{mg \sin \theta}{k}}$$

pos. eq  $\dot{x} = \ddot{x} = 0$

$$(1) \Rightarrow \cancel{0 = x + l_0} \quad \frac{k}{m} x - \left( g \sin \theta + \frac{k}{m} l_0 \right) = 0$$

$$\boxed{x_{eq} = l_0 + \frac{mg \sin \theta}{k}}$$