

**vigas hiperestáticas  
ESTRUCTURAS 2**

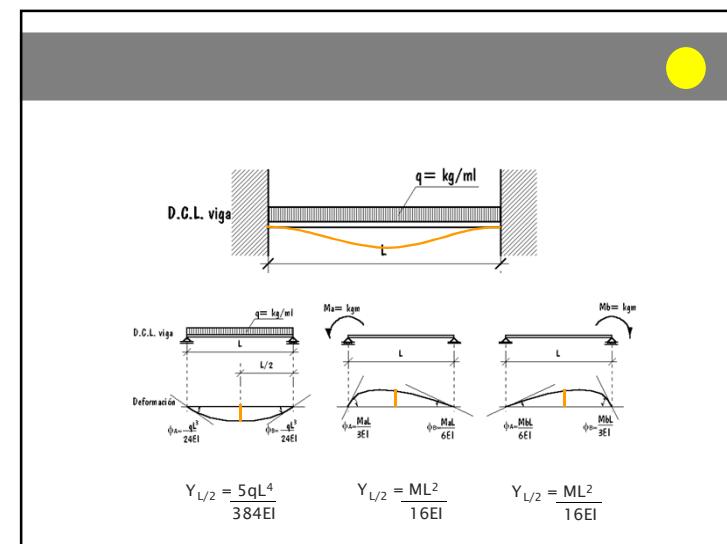
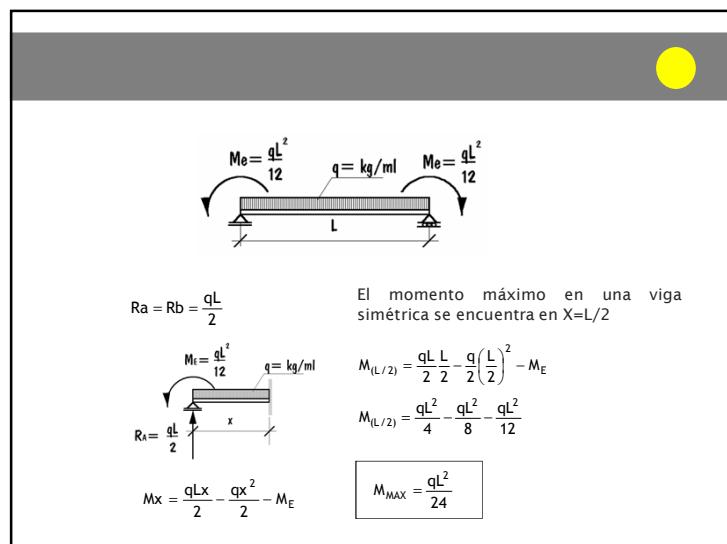
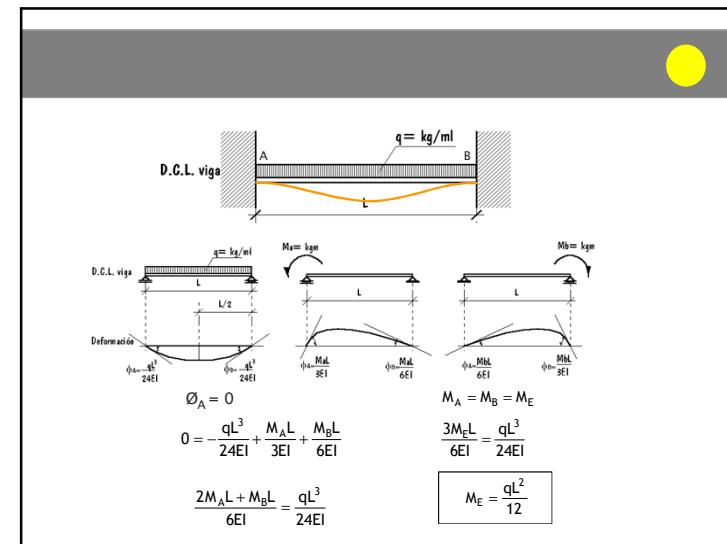
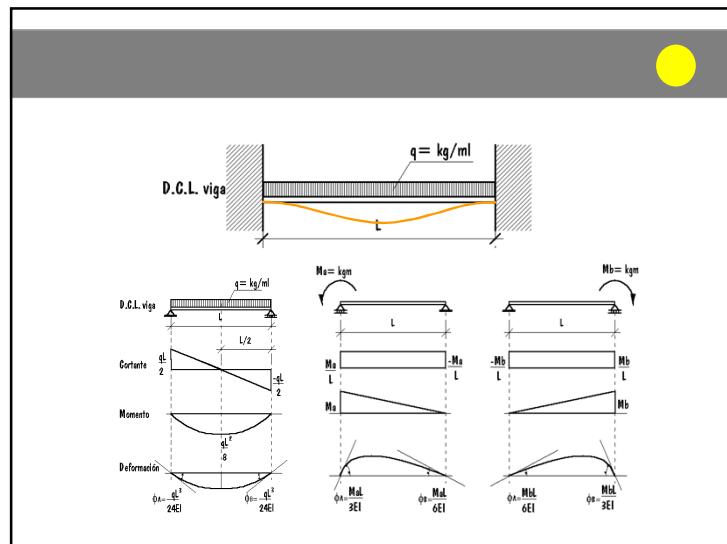
profesora: Verónica Veas      ayudante: Preeti Bellani

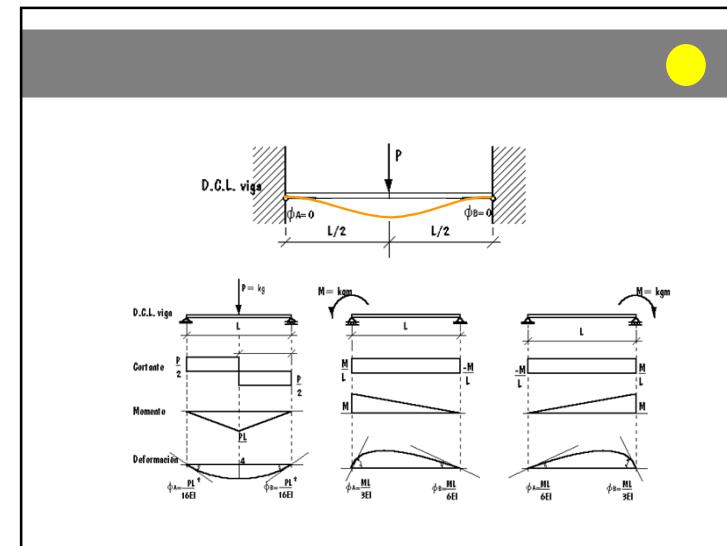
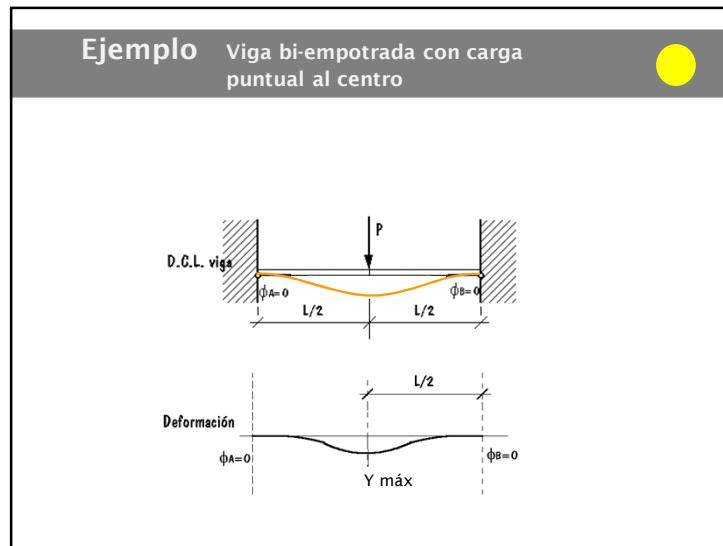
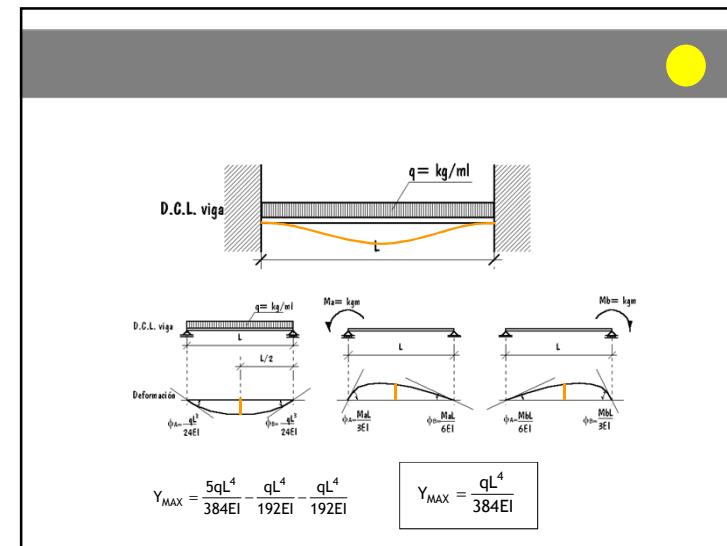
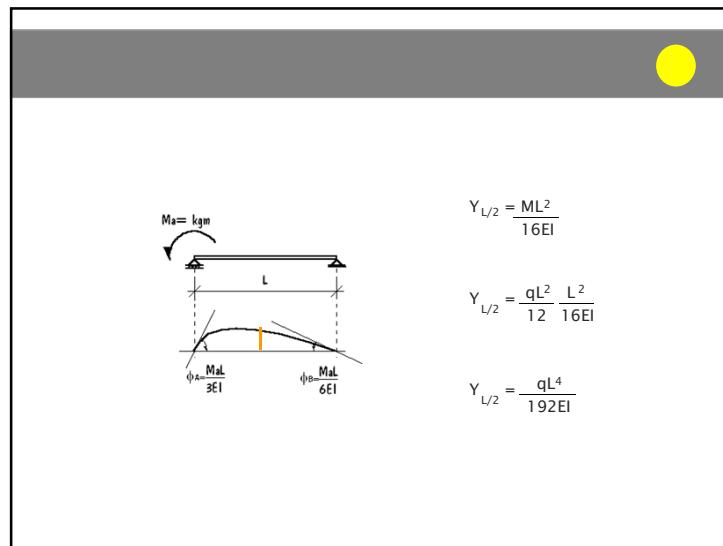
**Vigas Hiperestáticas**

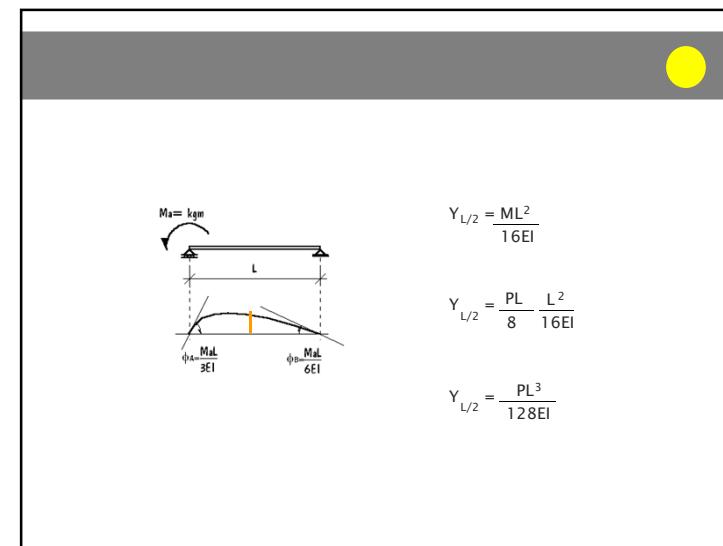
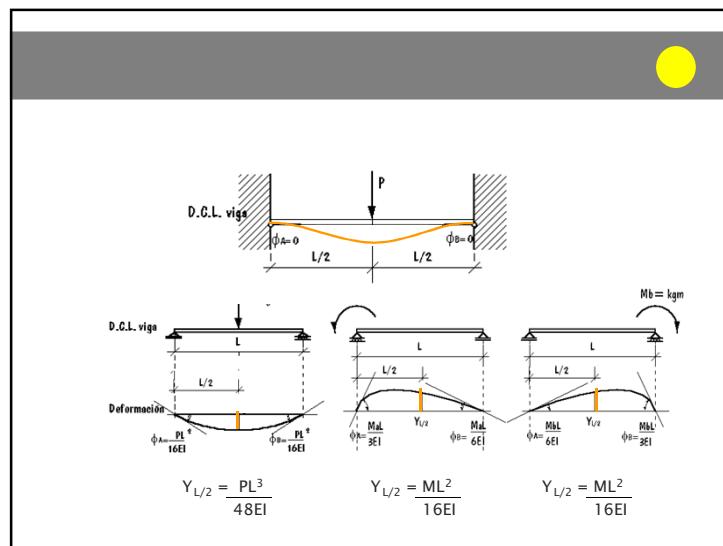
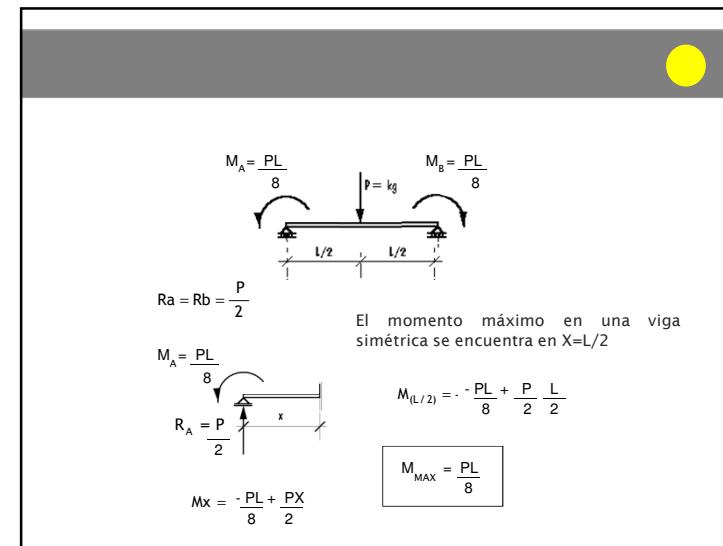
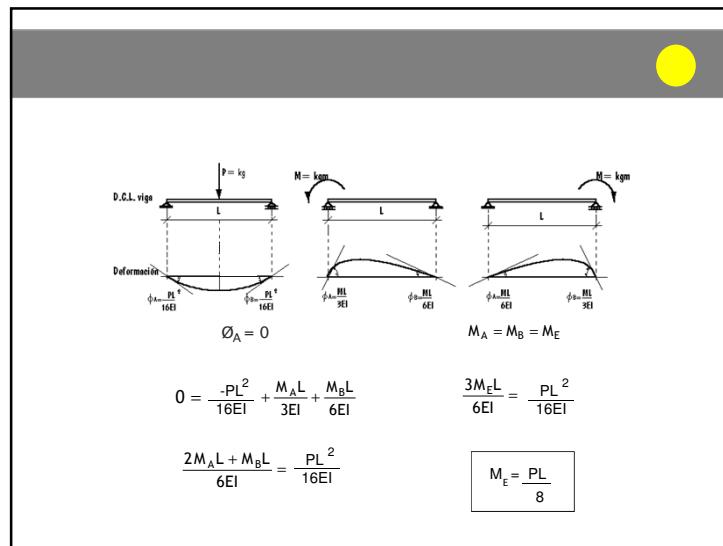
**Concepto de vigas hiperestáticas por empotramiento**

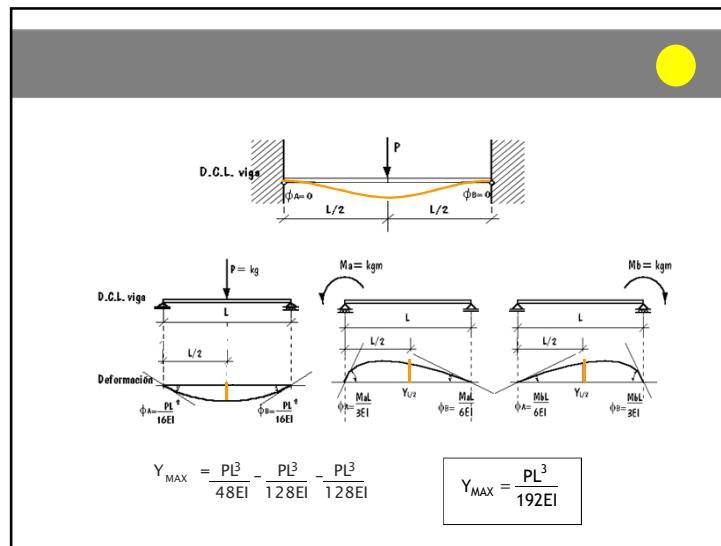
$\emptyset_{\text{empotramiento}} = 0$

**Ejemplo** Viga bi-empotrada con carga uniformemente repartida

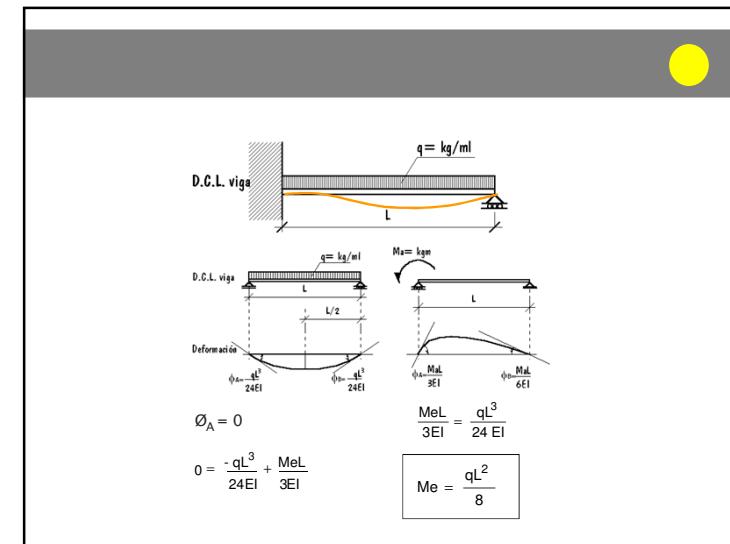
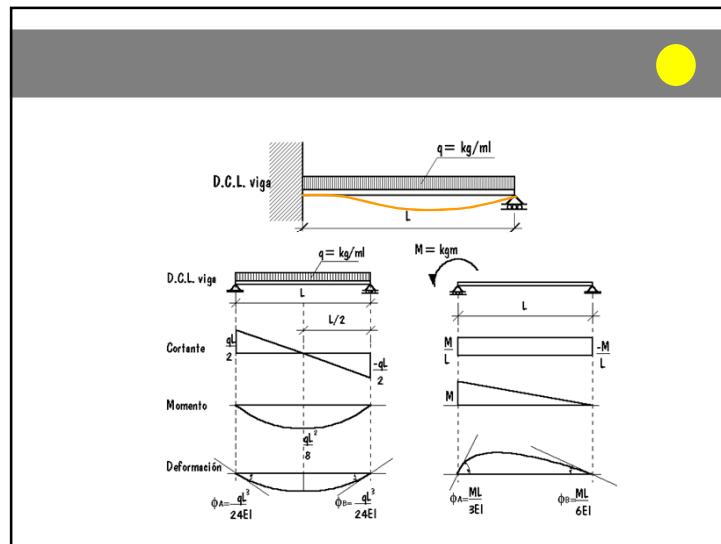
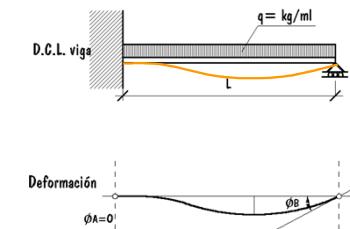


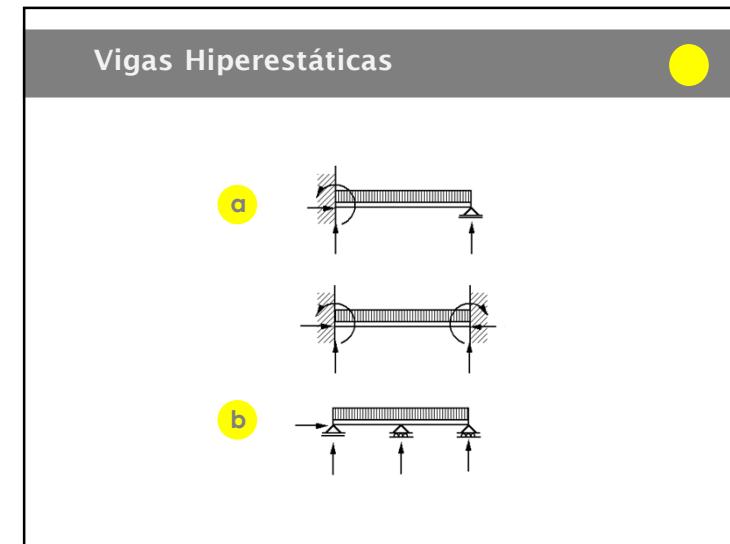
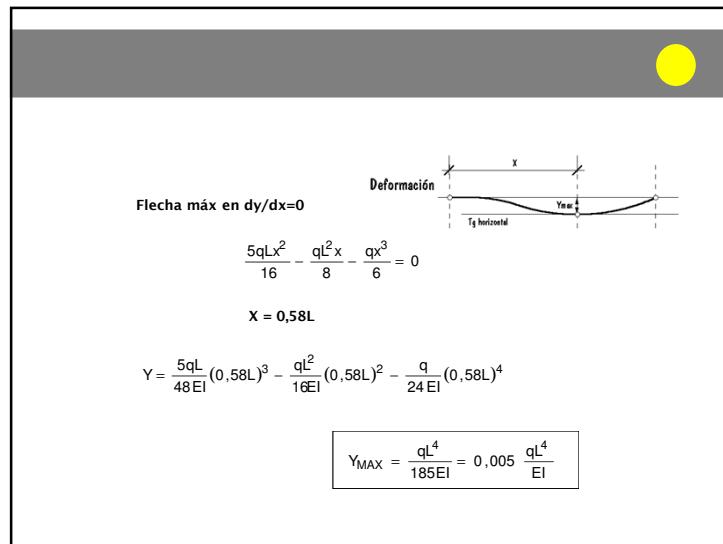
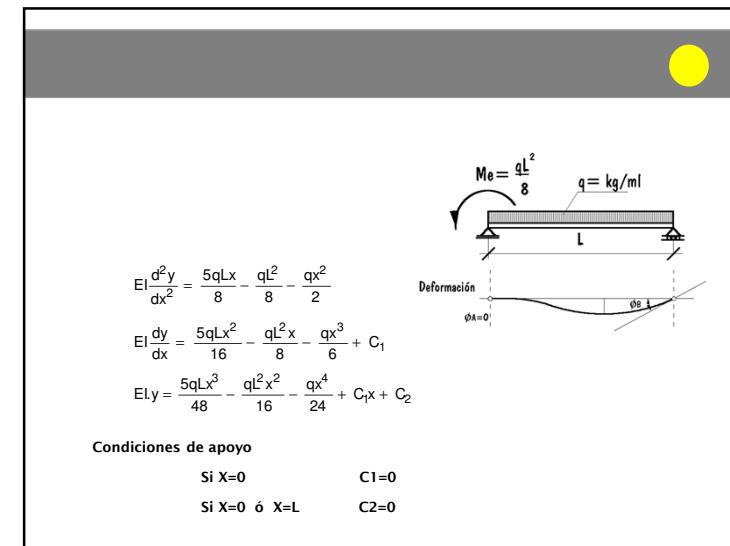
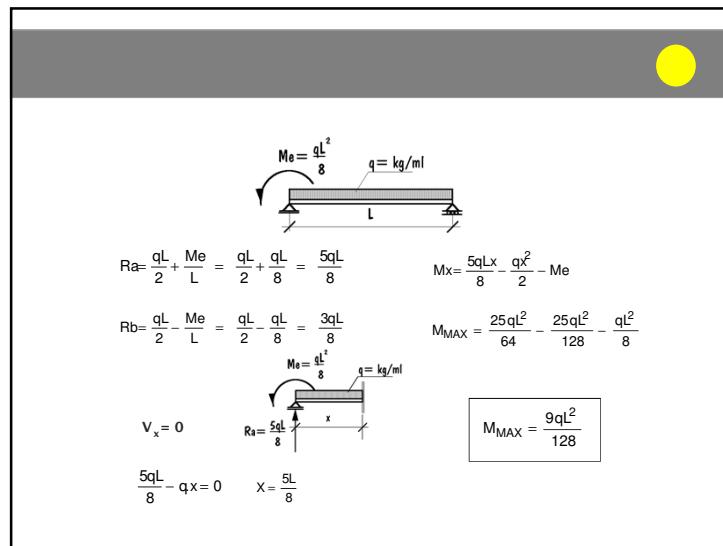






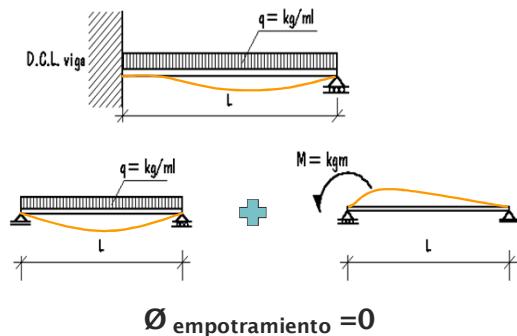
## Ejemplo Viga empotrada-apoyada con carga uniformemente repartida





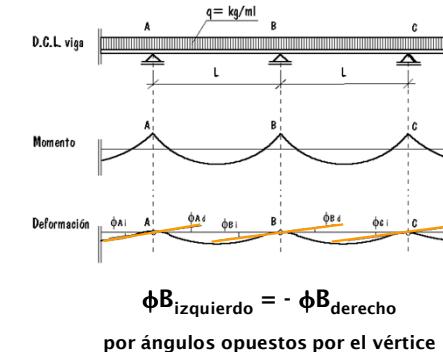
### Concepto de vigas hiperestáticas por empotramiento

a



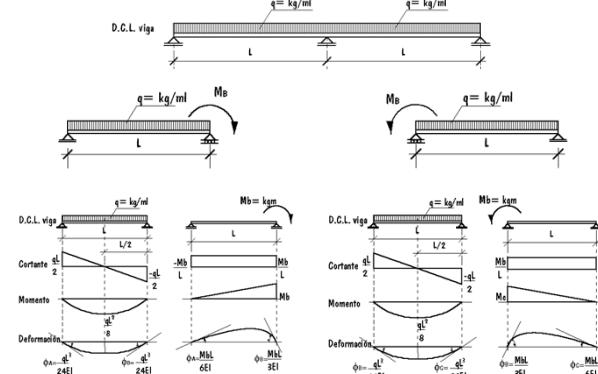
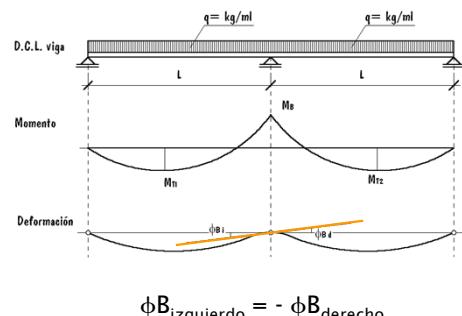
### Concepto de vigas hiperestáticas por continuidad

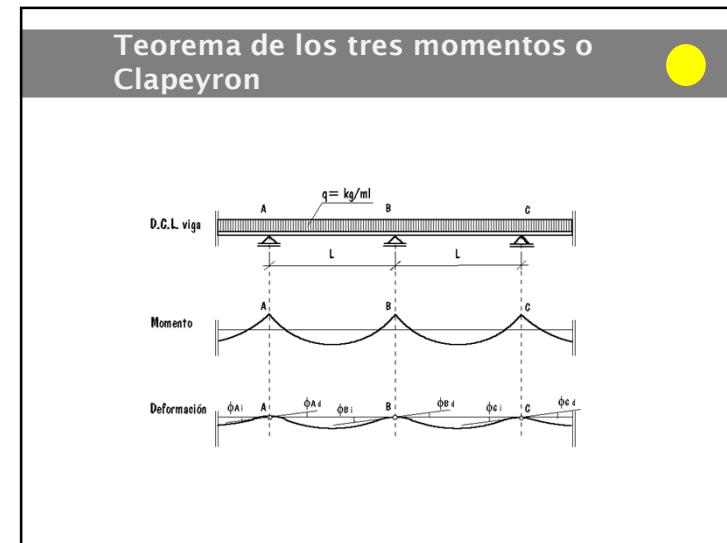
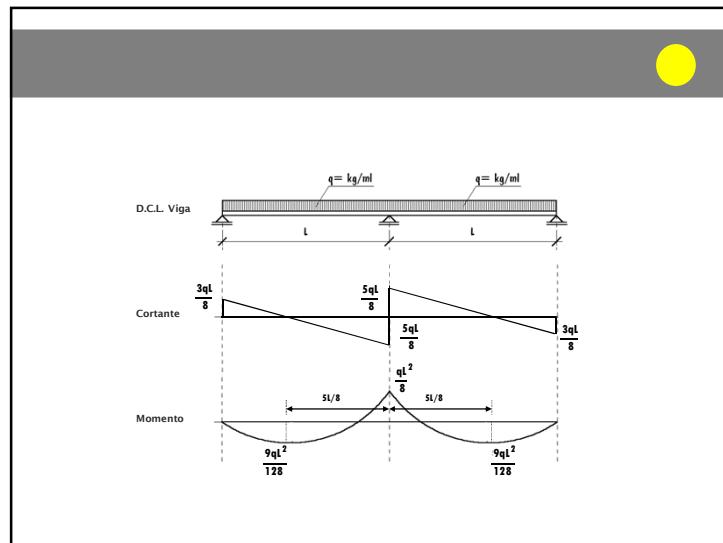
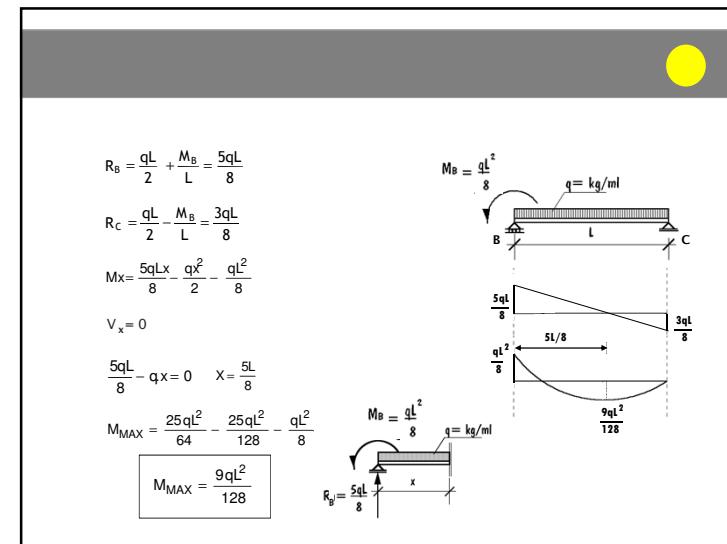
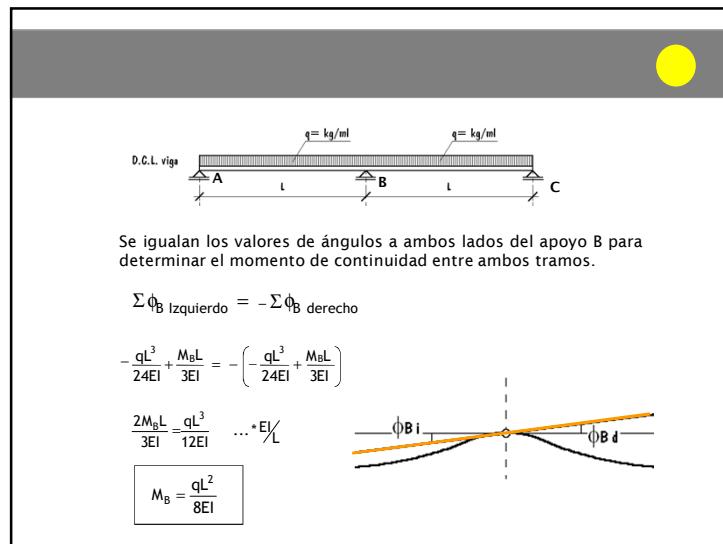
b

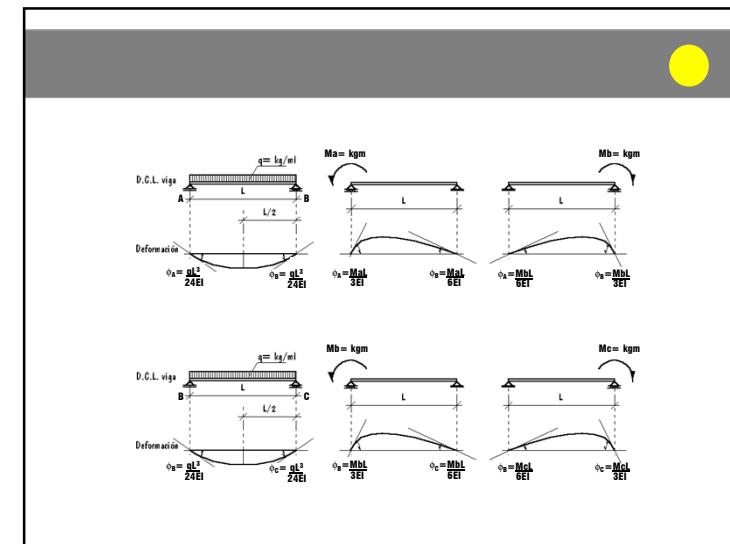
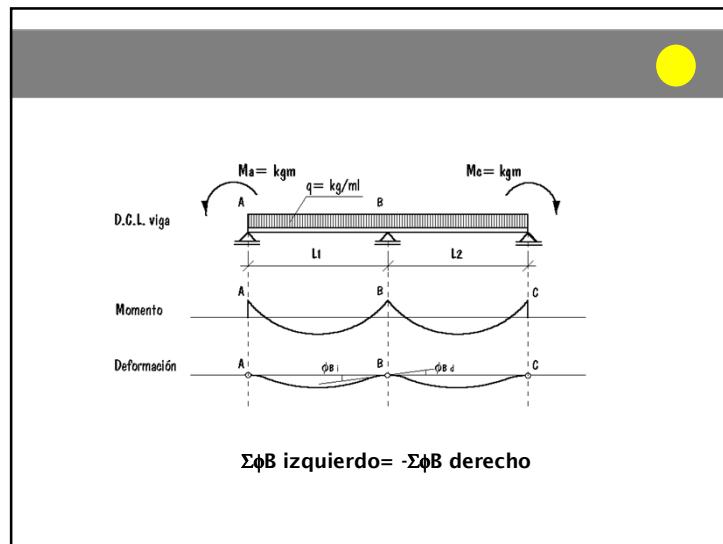


### Ejemplo Viga de dos tramos con carga uniformemente repartida

b







$\Sigma \phi_B \text{ izquierdo} = -\Sigma \phi_B \text{ derecho}$

$$-\frac{qL_1^3}{24EI} + \frac{MaL_1}{6EI} + \frac{MbL_1}{3EI} = -\left[ -\frac{qL_2^3}{24EI} + \frac{MbL_2}{3EI} + \frac{McL_2}{6EI} \right]$$

$$\frac{MaL_1}{6EI} + \frac{MbL_1}{3EI} + \frac{MbL_2}{3EI} + \frac{McL_2}{6EI} = \frac{qL_1^3}{24EI} + \frac{qL_2^3}{24EI}$$

Reemplazando  $L/EI$  por  $\lambda$  (módulo de flexibilidad)

$$\frac{Ma\lambda_1}{6} + \frac{Mb\lambda_1}{3} + \frac{Mb\lambda_2}{3} + \frac{Mc\lambda_2}{6} = \frac{qL_1^2\lambda_1}{24} + \frac{qL_2^2\lambda_2}{24} /*6$$

Al amplificar la expresión 6 veces se obtiene

$$\frac{Ma\lambda_1}{6} + 2Mb\lambda_1 + 2Mb\lambda_2 + \frac{Mc\lambda_2}{6} = 6 \left[ \frac{qL_1^2\lambda_1}{24} + \frac{qL_2^2\lambda_2}{24} \right]$$

$$\frac{Ma\lambda_1}{6} + 2Mb(\lambda_1 + \lambda_2) + \frac{Mc\lambda_2}{6} = 6 \left[ \frac{qL_1^2\lambda_1}{24} + \frac{qL_2^2\lambda_2}{24} \right]$$

Si  $EI = \text{constante}$  y  $\lambda = L/EI$   $\lambda = L$

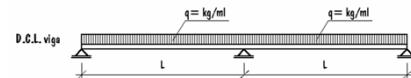
Reemplazando  $\lambda = L$  en la ecuación se tiene:

$$MaL_1 + 2Mb(L_1 + L_2) + McL_2 = 6 \left[ \frac{qL_1^3}{24} + \frac{qL_2^3}{24} \right]$$

Reemplazando  $\frac{qL_1^3}{24}$  por  $Tc_1$  y  $\frac{qL_2^3}{24}$  por  $Tc_2$

$MaL_1 + 2Mb(L_1 + L_2) + McL_2 = 6(Tc_1 + Tc_2)$

### Ejemplo Viga de dos tramos con carga uniformemente repartida



$$MaL_1 + 2Mb(L_1+L_2) + McL_2 = 6(Tc_1 + Tc_2)$$

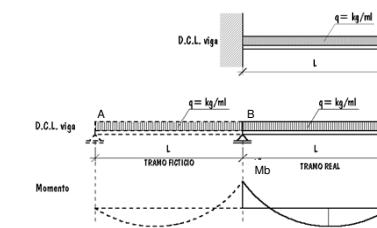
$$0L_1 + 2Mb(L_1+L_2) + 0L_2 = 6 \left[ \frac{qL_1^3}{24} + \frac{qL_2^3}{24} \right]$$

$$2Mb(L_1+L_2) = \frac{qL_1^3}{4} + \frac{qL_2^3}{4} \quad \text{Si } L_1=L_2$$

$$2Mb 2L = \frac{qL^3}{2}$$

$$Mb = \frac{qL^2}{8}$$

### Ejemplo Viga empotrada en un extremo y apoyada en el otro con carga uniformemente repartida



$$MaL_1 + 2Mb(L_1+L_2) + McL_2 = 6(Tc_1 + Tc_2)$$

$$00 + 2Mb(0+L) + 0L = 6 \left[ 0 + \frac{qL^3}{24} \right]$$

$$2Mb L = \frac{qL^3}{4}$$

$$Mb = \frac{qL^2}{8}$$