

b) Probar $A \cap B \cap C = \emptyset \Rightarrow (A \cup B) \cup (B \cup C) \cup (C \cup A) = A \cup B \cup C$

Por exprocaion: $A \cap B \cap C = \emptyset \Leftrightarrow \neg \forall$

PVQ $(A \cup B) \cup (B \cup C) \cup (C \cup A) = A \cup B \cup C$

$$(A \cap B^c) \cup (B \cap C^c) \cup (C \cap A^c)$$

$$[(A \cup B) \cap (A \cup C^c) \cap (B^c \cup B) \cap (B^c \cup C^c)] \cup (C \cap A^c)$$

$$[(A \cup B) \cap (A \cup C^c) \cap \top \cap (B^c \cup C^c)] \cup (C \cap A^c)$$

$$[(A \cup B) \cap (A \cup C^c) \cap (B^c \cup C^c)] \cup (C \cap A^c)$$

$$[(A \cup B) \cup (C \cap A^c)] \cap [(A \cup C^c) \cup (C \cap A^c)] \cap [(B^c \cup C^c) \cup (C \cap A^c)]$$

$$[B \cup [(A \cup C) \cap (A \cup A^c)]] \cap [A \cup [(C^c \cup C) \cap (C^c \cup A^c)]] \cap [B^c \cup [(C^c \cup C) \cap (C^c \cup A^c)]]$$

~~$(B \cup A \cup C) \cap$~~

$$(B \cup [(A \cup C) \cap \top]) \cap [A \cup [\top \cap (C^c \cup A^c)]] \cap (B^c \cup [\top \cap (C^c \cup A^c)])$$

$$(B \cup A \cup C) \cap (A \cup (C^c \cup A^c)) \cap (B^c \cup C^c \cup A^c)$$

$$(B \cup A \cup C) \cap \top \cap (B \cap C \cap A)^c$$

$$(A \cup B \cup C) \cap (A \cap B \cap C)^c$$

Asumimos que $A \cap B \cap C = \emptyset$

$$\Rightarrow (A \cap B \cap C)^c = \top$$

$$(A \cup B \cup C) \cap \top$$

$$A \cup B \cup C$$