$$F_{\text{resistiva}} = - \gamma \mathbf{v} \text{ siempre?}$$
 No

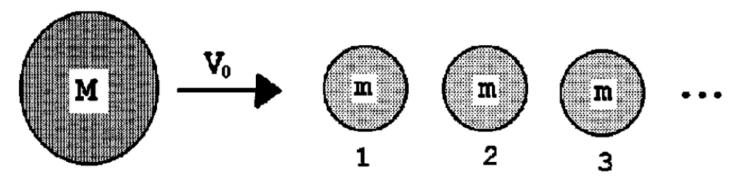


Fig. 1. A body of mass M, speed  $V_0$ , undergoes a one-dimensional collision with an array of identical molecules of mass m at rest, with m < M. The momentum lost by the body as it moves forward is exchanged among the molecules away from the body in an orderly manner, without backscattering.

$$V_1 = V_0 - \left(\frac{2m}{M+m}\right)(V_0 - v_0),$$

$$v_1 = V_0 + \left(\frac{M-m}{M+m}\right)(V_0 - v_0).$$

Despues de la primera colision

Suponer v0=0

$$V_1 = \left(\frac{M-m}{M+m}\right) V_0$$
  $v_1 = \frac{2M}{M+m} V_0 > V_1$ .

it is easy to calculate the speed of the body after an arbitrary number, N, of collision events (all of them with molecule #1):

$$V_N = \left(\frac{M-m}{M+m}\right)^N V_0. \tag{5}$$

Assuming an average density of medium molecules  $\rho$ , the number of collisions after traversing a distance x will be  $\rho x$ , and Eq. (5) can be cast as

$$V(x) = \left(\frac{1-r}{1+r}\right)^{\rho x} V_0, \tag{6}$$

where we have defined r=m/M as the mass ratio. In going over to the continuum, we have to assume that an infinitesimal interval dx contains very many molecules, as in Hydrodynamics. Equation (6) means an exponential decay of speed with distance traversed inside the medium, since it can be rewritten as  $V(x) = V_0 \exp(-\alpha x)$  with  $\alpha = \rho \log[(1+r)/(1-r)]$ .

We can define a characteristic distance, the *half-range* R, as the distance traveled inside the medium necessary to reduce the kinetic energy of the body to a half. This implies  $V = V_0/\sqrt{2}$ . After equating Eq. (6) (with x = R) to  $V_0/\sqrt{2}$  and solving for R, we obtain:

$$R = \frac{1}{2\rho} \log(2) / \log\left(\frac{1+r}{1-r}\right). \tag{7}$$

Let us now calculate the force acting on the body. According to Newton's second law: F = Ma and a  $= dV/dt = (\partial V/\partial x)(\partial x/\partial t) = (\partial V/\partial x)V(x)$ . Using  $dA^x/dx$  $=A^{x} \log(A)$ , we obtain

$$a = -\rho \log \left(\frac{1+r}{1-r}\right) V^2 \tag{8}$$

which implies,
$$F = Ma = -\gamma V^2,$$
(9)

where

$$\gamma \equiv m\rho \log \left(\frac{1+r}{1-r}\right) / r \tag{10}$$

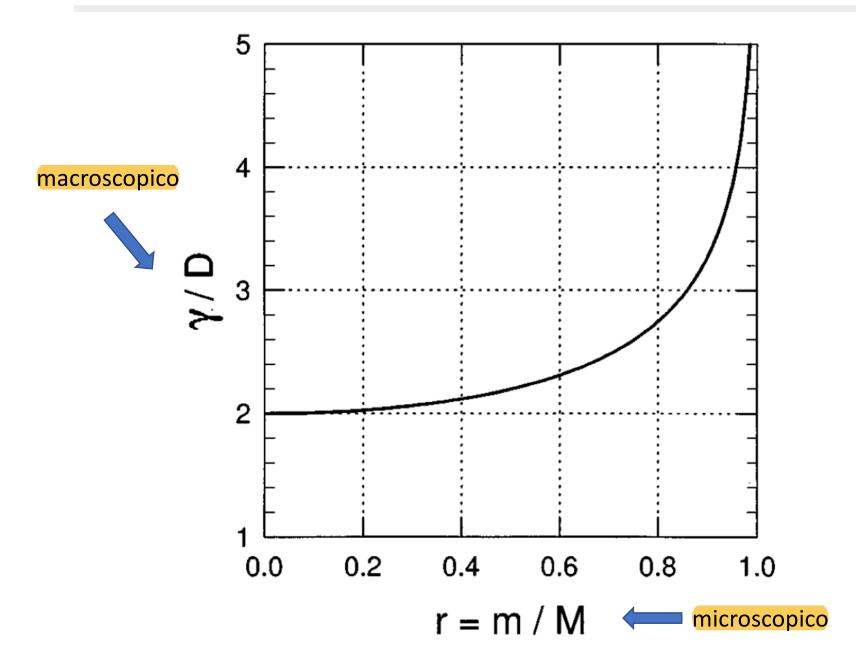


Fig. 3. Resistive coefficient  $\gamma$  as a function of molecule/body mass ratio.